The Study of the Anomalous Acceleration of Pioneer 10 and 11

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Journées du GREX 2004 Nice, France, 29 October 2004 Pioneer Collaboration: John D. Anderson, Philip A. Laing, Eunice L. Lau, Michael Martin Nieto and Slava G. Turyshev



Conclusions & Outline:



• The Pioneer 10/11 anomalous acceleration: $a_P = (8.74 \pm 1.33) \times 10^{-8} \text{ cm/s}^2$



A line-of-sight constant acceleration towards the Sun:

- We find no mechanism or theory that explains the anomaly
- Most plausible cause is systematics, yet to be demonstrated

Phys. Rev. D 65 (2002) 082004, gr-qc/0104064

Possible Origin?

- Conventional Physics [not yet understood]:
 - Gas leaks, heat reflection, drag force, etc...
- New Physics [many proposals exist, some interesting]



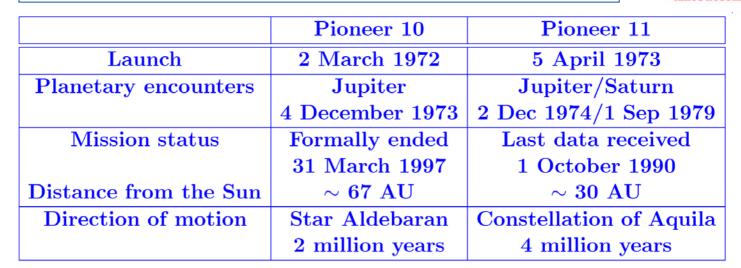
- Both are important a "win-win" situation:
 - CONVENTIONAL explanation: improvement of spacecraft engineering for precise navigation & attitude control
 - NEW physics: would be truly remarkable...



Pioneer 10/11 Mission

- Built: **TRW** (Northrop-Grumman Space Technology)
- Navigation: Jet Propulsion Laboratory, Caltech
- Project management: NASA Ames Research Center





Position of Pioneer 10 on 29 October 2004:

Distance from Sun	86.91 AU
Position, SE_lat SE_lon	$(3.0^{\circ},\ 77.4^{\circ})$
Speed relative to the Sun	$12.24 \mathrm{\ km/sec}$
Distance from Earth	13.14 Gkm
Round-Trip Light Time	$pprox 24 { m hr} 22 { m min}$

Last successful precession maneuver to point the spacecraft to Earth was accomplished on 11 Feb 2000 (distance from the Sun of 75 AU)











Pioneer 10/11 Spacecraft









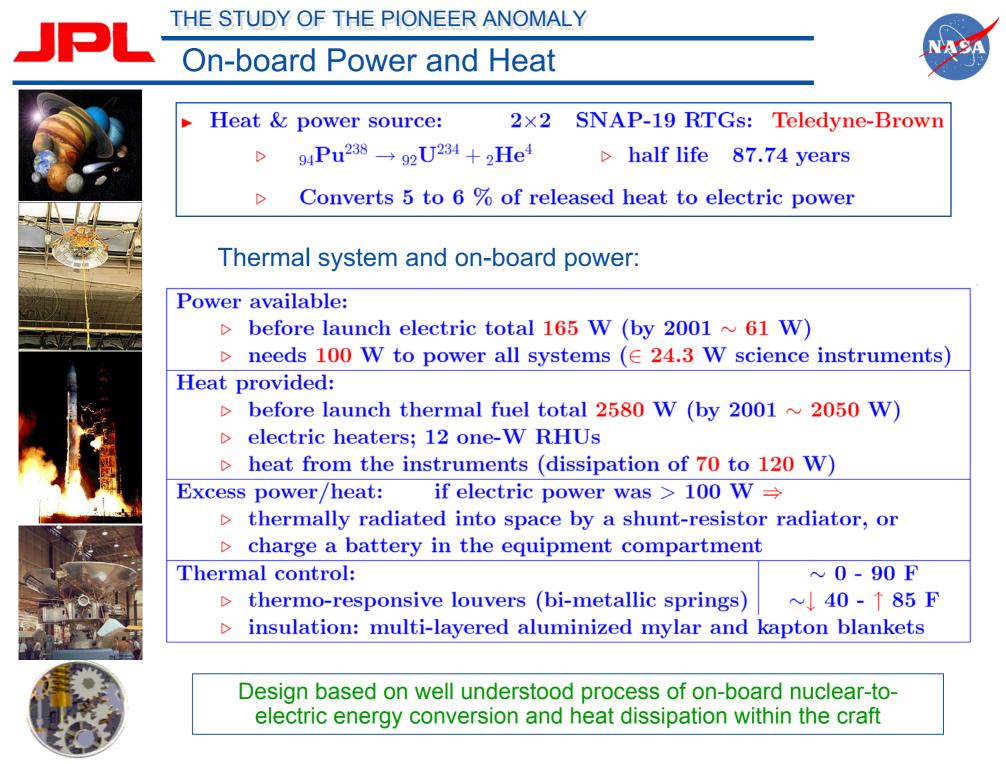




Parameter (ide	Pioneer 10/11		
Main bus	$259\ (224{+}36)$		
2×2 SNAP-19 RTG Mass/distance, kg/m		13.6/3	
Magnetometer Mass/distance, kg/m		5/6	
Moment of in	588.3		
High Gain Antenane	${f Diameter/depth, m}$	2.74/0.46	
Maximal cro	5.914		
Attitude control Spin-stabilization, rpn		${\sim}4.28/7.8$	

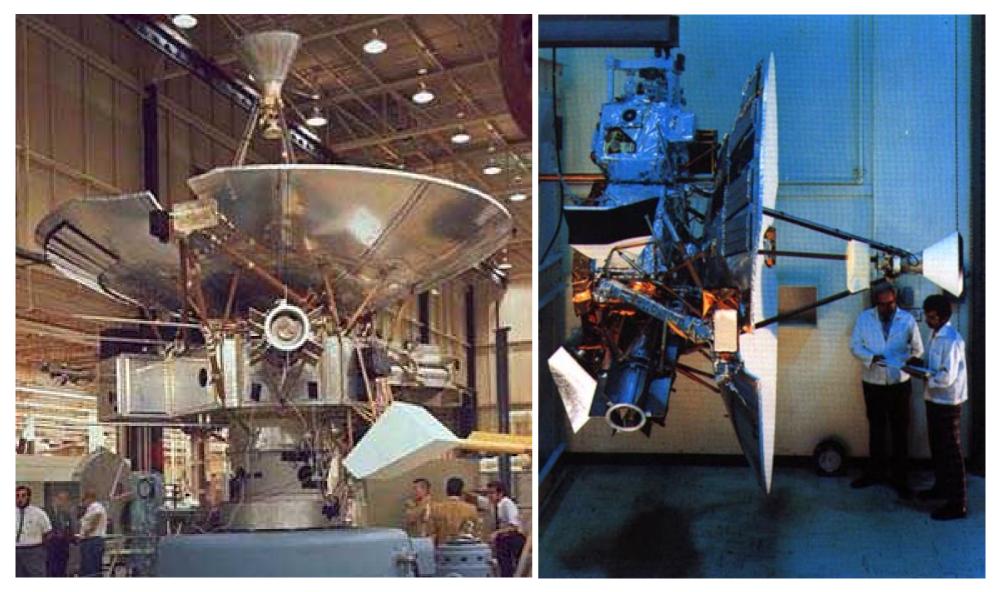
Communica	Data available			
S-up, MHz	S-up, MHz S-down, MHz transp.ratio			
2110	2292	240/221	Doppler	
Provide initial position, velocity, magnitudes of maneuvers				

- Pioneer 10/11 were excellent for dynamical astronomy:
 - Spacecraft design permits precise acceleration estimations, ~10⁻⁸ cm/s², unlike a Voyager-type 3-axis stabilization
- Accurate celestial mechanics experiments one of the main objectives of the Pioneer extended missions



Pioneer F during checkout tests





The Pioneer F spacecraft during a checkout with the launch vehicle third stage at Cape Kennedy. Pioneer F became Pioneer 10.

Pioneer 10 Launch: 2 March 1972







JP



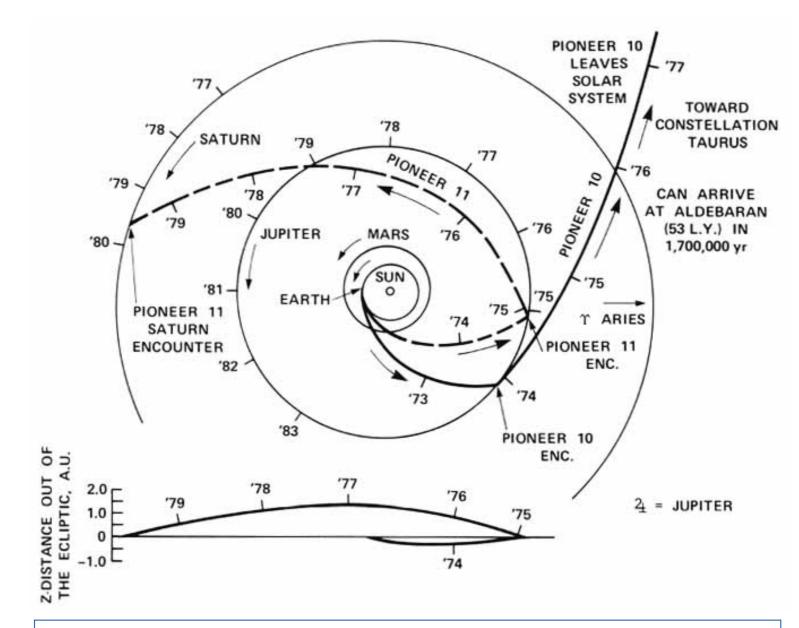






Pioneer 10/11: Main Missions

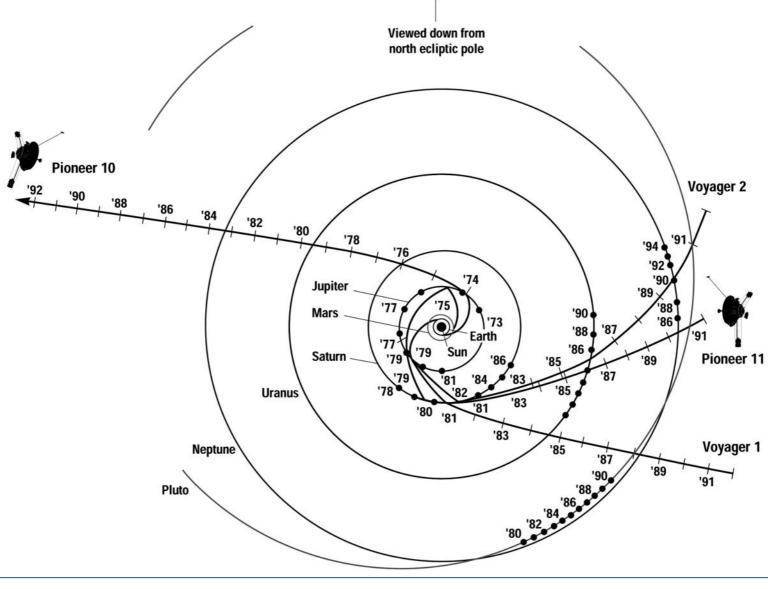




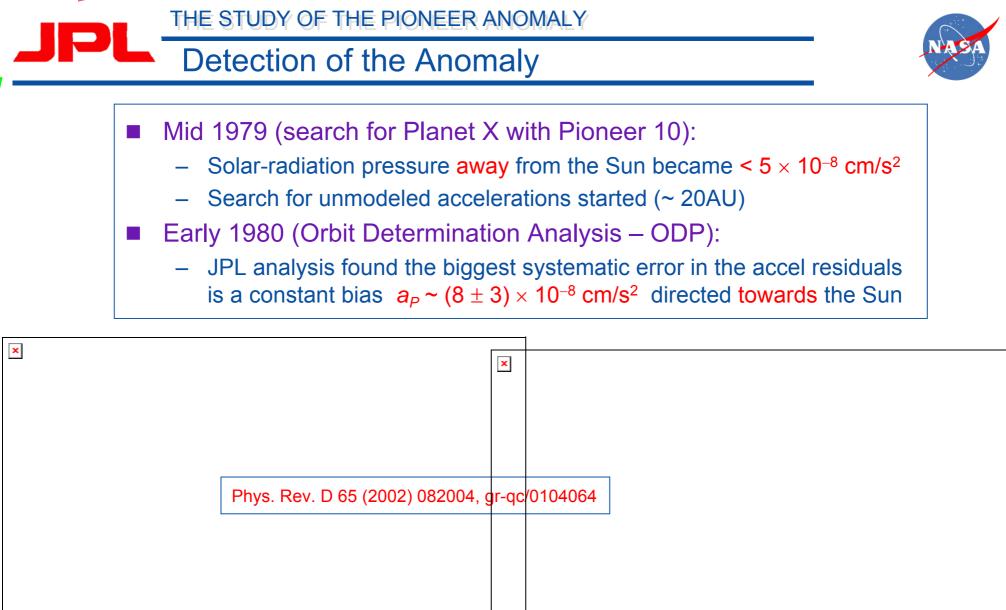
Trajectories for Pioneer 10 and 11 during the main mission phase

Trajectories of Pioneers and Voyagers





Ecliptic pole view of Pioneer 10, Pioneer 11, and Voyager trajectories. Digital artwork by T. Esposito. NASA ARC Image # AC97-0036-3.



An ODP plot of the early unmodeled accelerations of Pioneer 10 and Pioneer 11, from about 1981 to 1989 and 1977 to 1989, respectively



The Observed Anomaly





- There is an un-modeled acceleration towards the Sun

 $(8.09 \pm 0.20) \times 10^{-8} \text{ cm/s}^2$ for Pioneer 10

(8.56 \pm 0.15) \times 10^{-8} cm/s^2 for Pioneer 11

- The error is determined with a 5-day BSF with radial accel as a stochastic parameter subject to white Gaussian noise (~500 independent 5-day samples of radial acceleration).
- NO magnitude variation with distance over a range of 40 to 70 AU

PRL 81(1998) 2858-2861, gr-qc/9808081

 $a_P = (8.65 \pm 0.03) \times 10^{-8} \text{ cm/s}^2$

The two-way Doppler anomaly to first order in (v/c) behaves as:

$$\begin{aligned} \nu_{\text{obs}}(t) - \nu_{\text{model}}(t) &= -\nu_0 \frac{2 \, a_P \cdot t}{c} \qquad \nu_{\text{model}} = \nu_0 \left[1 - \frac{2 \, v_{\text{model}}(t)}{c} \right] \\ v_{\text{obs}}(t) - v_{\text{model}}(t) &= -2 \, a_P \cdot t \end{aligned}$$

Equivalent forms of the Anomaly:

- Steady frequency drift: $-6 \times 10^{-9} \text{ Hz/s} (\approx 1.5 \text{ Hz/8 yrs})$
- Anomalous acceleration:
- Clock acceleration: $a_t = -2.8 \times 10^{-18} \text{ s/s}^2$, $a_P \equiv a_t c$

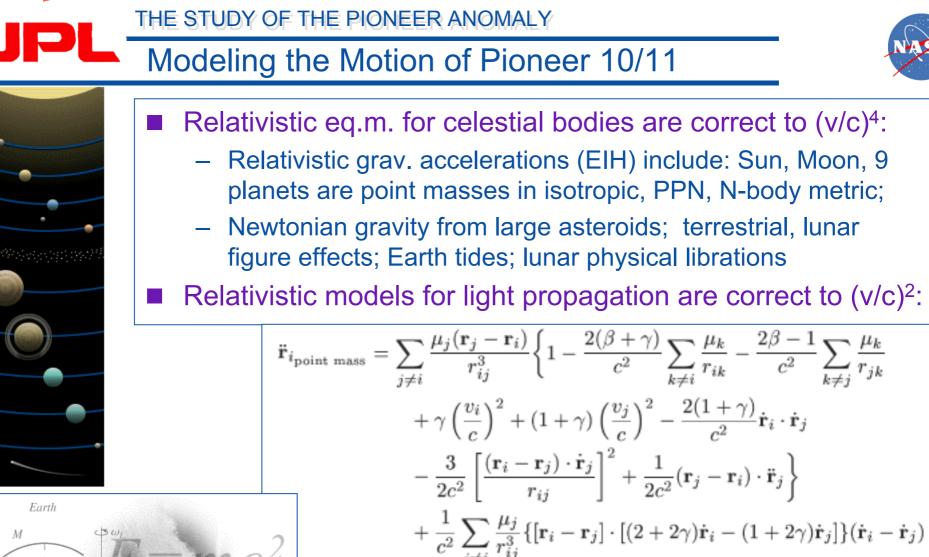












$$M = \frac{a \sin \theta}{a \sin \theta} \frac{b}{r}$$

$$+ \frac{(3+4\gamma)}{2c^2} \sum_{j \neq i} \frac{\mu_j \ddot{\mathbf{r}}_j}{r_{ij}} \quad + \sum_{m=1}^3 \frac{\mu_m (\mathbf{r}_m - \mathbf{r}_i)}{r_{im}^3} \quad + \sum_{c,s,m} \mathbf{F}$$

$$t_2 - t_1 = \frac{r_{21}}{c} + \frac{(1+\gamma)\mu_{\odot}}{c^3} \ln\left[\frac{r_1^{\odot} + r_2^{\odot} + r_{12}^{\odot}}{r_1^{\odot} + r_2^{\odot} - r_{12}^{\odot}}\right] + \sum_i \frac{(1+\gamma)\mu_i}{c^3} \ln\left[\frac{r_1^i + r_2^i + r_{12}^i}{r_1^i + r_2^i - r_{12}^i}\right]$$



Standard Models of Non-Gravitational Forces



- Model accounts for many sources of non-grav. forces, including:
 - Solar radiation and wind pressure; the interplanetary media
 - Attitude-control propulsive maneuvers; gas leakage from the propulsion system
 - DSN antennae contributions to the spacecraft radio tracking data
 - Torques produced by above mentioned forces
 - Orbit determination procedure, includes:
 - Models of precession, nutation, sidereal rotation, polar motion, tidal effects, and tectonic plates drift;
 - Model values of the tidal deceleration, non-uniformity of rotation, polar motion, Love numbers, and Chandler wobble are obtained observationally via LLR, SLR and VLBI (from ICRF):
 - Now [after Pioneer] model can be adjusted to include:
 - Effects of the recoil force due to emitted radio power
 - Anisotropic thermal radiation of spacecraft

- Unknown forces are routinely modeled as stochastic accels:
 - Exponentially correlated in time, with a variable time constant
 - Stochastic variable was sampled in 0-, 5-,10-day batches



Models Used to Explain the Anomaly









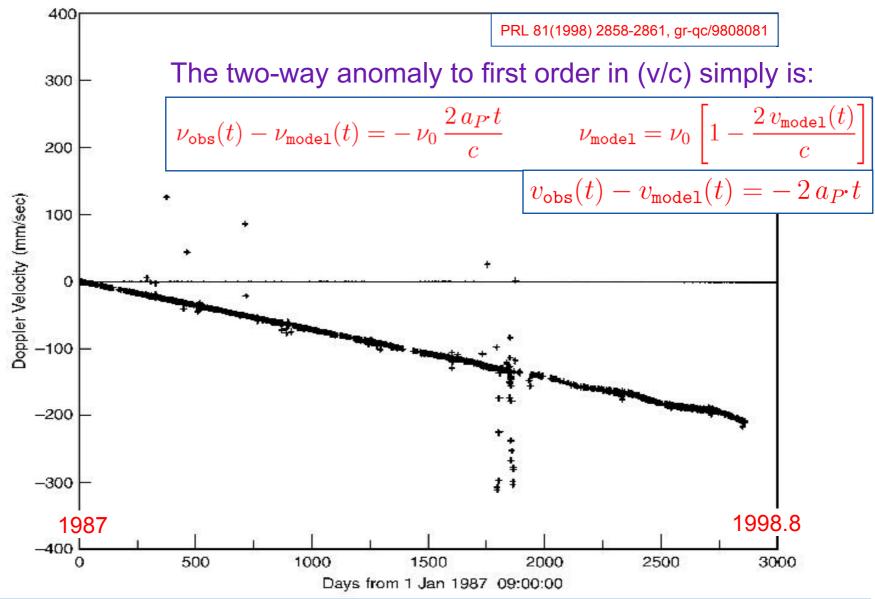




- Models and suggestions that failed to explain the anomaly:
 - Non-gravitational effects:
 - Solar pressure, solar wind, interplanetary medium
 - Precessional attitude control maneuvers and "gas leaks"
 - Nominal thermal radiation, plutonium half life
 - Some viscous drag force (ULY: solar radiation, maneuvers)
 - Gravity from the Kuiper belt; gravity from the Galaxy
 - Dark Matter distributed in a halo around the solar system
 - Drifting clocks, general relativity, the "speed of gravity"
 - Hardware problems at the DSN tracking stations
 - Errors in the planetary ephemerides
 - Errors in the values of the EOP, precession, and nutation;
 - Identical design of Pioneer 10/11 spacecraft (GLL, ULY: solar radiation, maneuvers)
- Error in JPL's ODP?
 - Numerous internal checks
 - NASA Grant to The Aerospace Corporation: 1996-1998

The Pioneer Anomaly

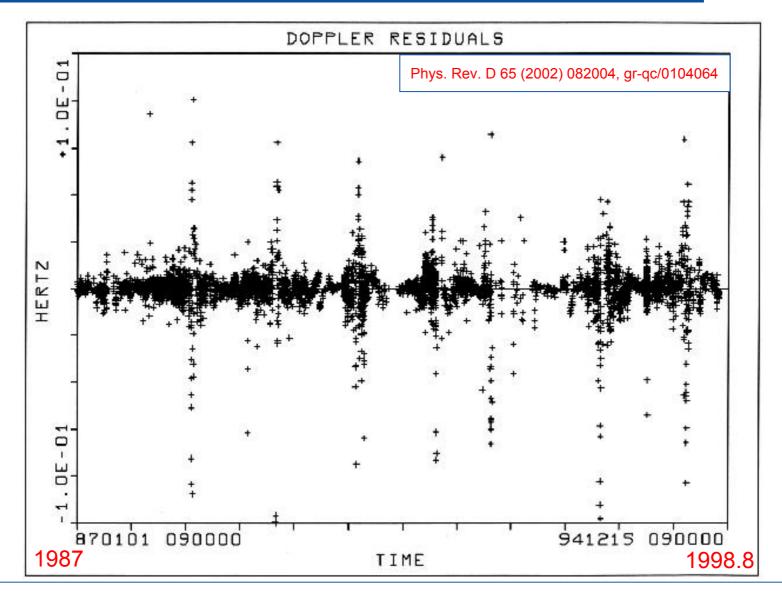




CHASMP two-way Doppler residuals (observed Doppler velocity minus model Doppler velocity) for Pioneer 10 vs time. [1 Hz is equal to 65 mm/s range change per second]

The Pioneer Anomaly





Adding one more parameter to the model – a constant radial acceleration – led to residuals distribution ~ zero Doppler velocity with a systematic variation ~3.0 mm/s. The quality of the fit may be determined by the ratio of residuals to the downlink carrier frequency, $v_0 \approx 2.29$ GHz.

Sources of External Systematic Error [PRD, 2002]



	Error b	udget constituents	$\frac{\textbf{Bias}}{10^{-8} \text{ cm/s}^2}$	Uncertainty, 10^{-8} cm/s^2
⇒		diation pressure n the mass uncertainty	+0.03	$egin{array}{c} \pm \ 0.001 \\ \pm \ 0.01 \end{array}$
	Solar wi		+0.05	\pm 0.01 \pm < 10 ⁻⁵
		ects of the solar corona		\pm 0.02
		magnetic Lorentz forces		\pm 0.02 \pm < 10 ⁻⁴
		e of the Kuiper belt's gravity		\pm 0.03
		e of the Earth orientation		\pm 0.001
\Rightarrow		ical and phase stability of DSN antenna	e	$\pm < 0.001$
⇒		tability and clocks	Č.	$\pm < 0.001$
⇒		ation location		$\pm < 10^{-5}$
⇒		ohere and ionosphere		$\pm < 0.001$
·	rr			
_				
_		Error budget constituents	$\frac{\mathbf{Bias}}{10^{-8} \ \mathbf{cm/s}^2}$	$\begin{array}{c} {\bf Uncertainty,}\\ {\bf 10}^{-8} {\bf cm/s}^2 \end{array}$
	F	Error budget constituents Numerical stability of		
	F	Numerical stability of		
		Numerical stability of least-squares estimation		
	\Rightarrow P \Rightarrow A	Numerical stability of least-squares estimation Accuracy of consistency/model tests		10^{-8} cm/s^{2} ± 0.02
	\Rightarrow P \Rightarrow A	Numerical stability of least-squares estimation Accuracy of consistency/model tests Mismodeling of maneuvers		$\begin{array}{c} 10^{-8} \text{ cm/s}^2 \\ \pm 0.02 \\ \pm 0.13 \\ \pm 0.01 \end{array}$
	$ \Rightarrow \mathbf{N} $ $ \Rightarrow \mathbf{A} $ $ = $	Numerical stability of least-squares estimation Accuracy of consistency/model tests ⇒ Mismodeling of maneuvers ⇒ Mismodeling of the solar corona		10^{-8} cm/s^2 ± 0.02 ± 0.13
	$ \Rightarrow \mathbf{N} $ $ \Rightarrow \mathbf{A} $ $ = $	Numerical stability of least-squares estimation Accuracy of consistency/model tests Mismodeling of maneuvers		10^{-8} cm/s^2 ± 0.02 ± 0.13 ± 0.01 ± 0.02



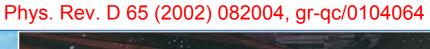
Sources of On-board Systematic Error [PRD, 2002]

		Error budget constituents	Bias	Uncertainty,	
_			$10^{-8} { m ~cm/s}^2$	$10^{-8} \mathrm{~cm/s}^2$	
-	⇒	Radio beam reaction force	+1.10	\pm 0.11	
	⇒	Thermal/propulsion effects from RTGs:	,		
		\Rightarrow RTG heat reflected off the craft	-0.55	\pm 0.55	
		\Rightarrow Differential emissivity of the RTGs		\pm 0.85	
7		\Rightarrow Non-isotropic radiative cooling of s/c		\pm 0.16	
		\Rightarrow Expelled He produced within the RTGs	+0.15	± 0.16	
	⇒	Propulsive mass expulsion: gas leakage		± 0.56	
Ξ	⇒	Variation between s/c determinations	+0.17	± 0.17	



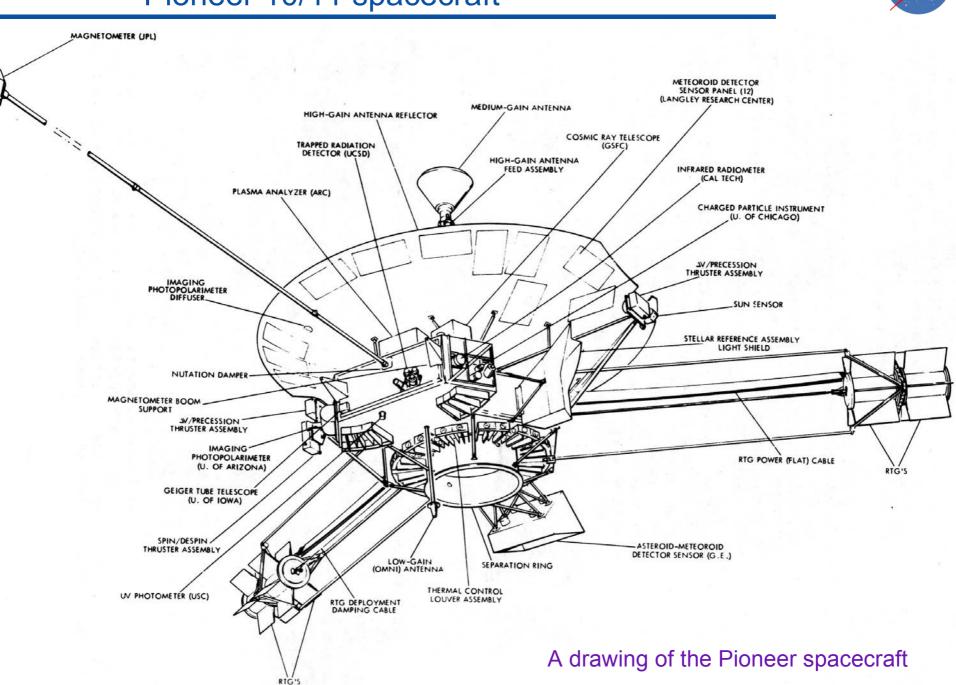
EV2

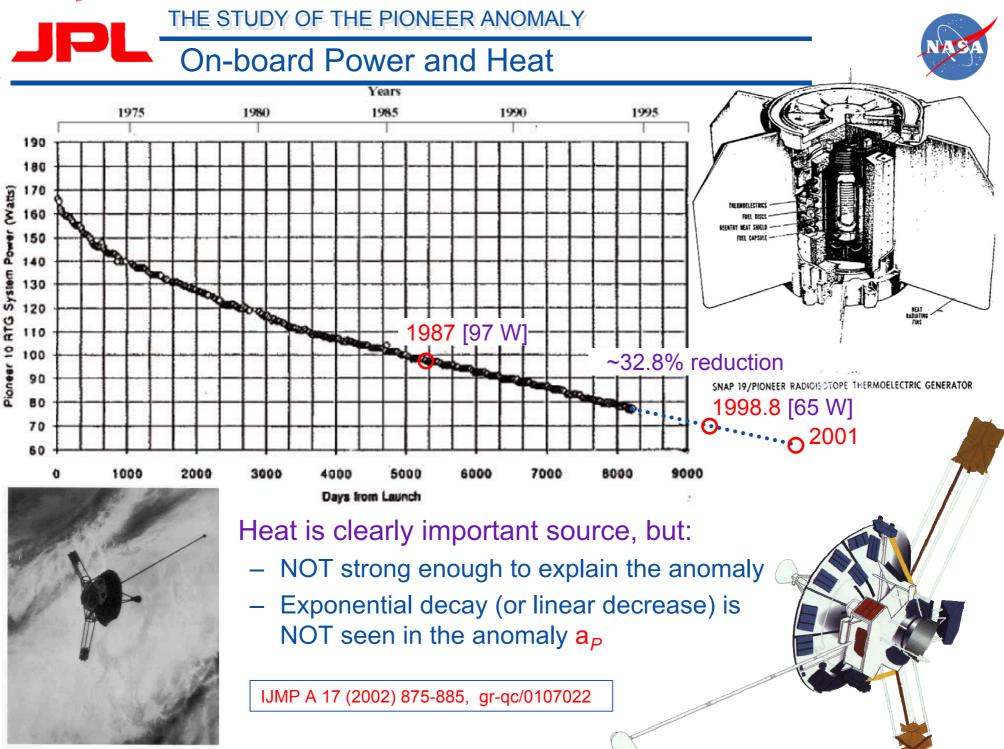
Pioneer DSN antenna at Goldstone





Pioneer 10/11 spacecraft



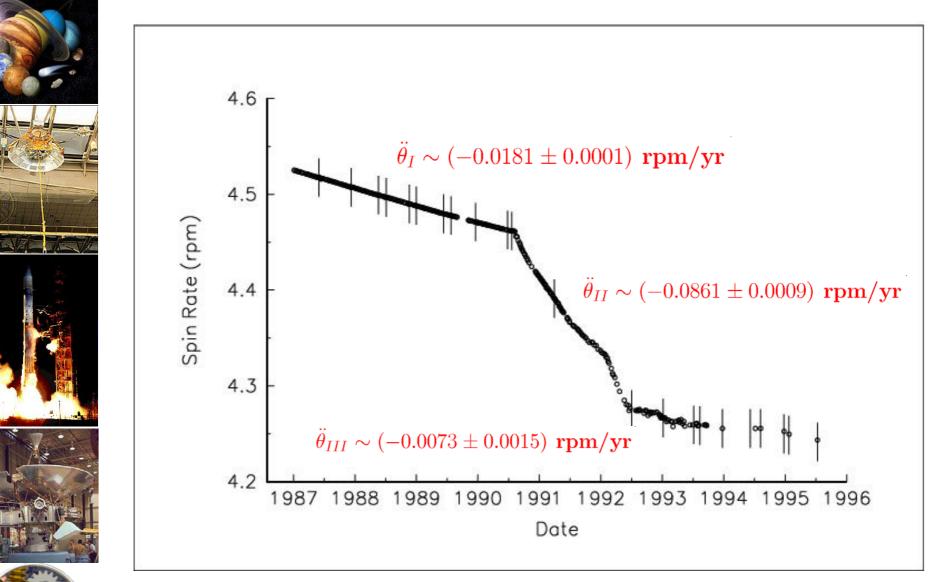


Pioneer 10



New Focus: the Pioneer 10 Spin History



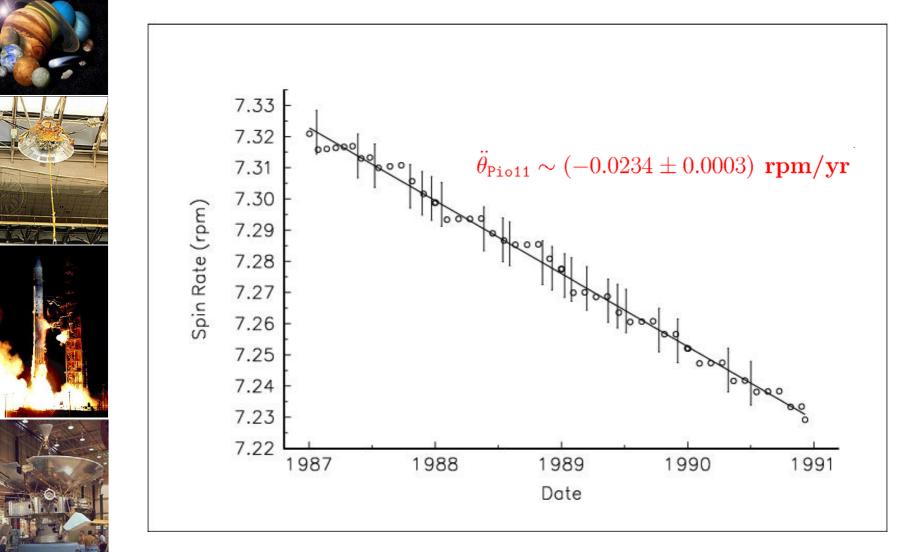


Most spacecraft show "spin-down" behavior usually due to structure tiredness, connection loosening, etc.



Pioneer 11 Spin History

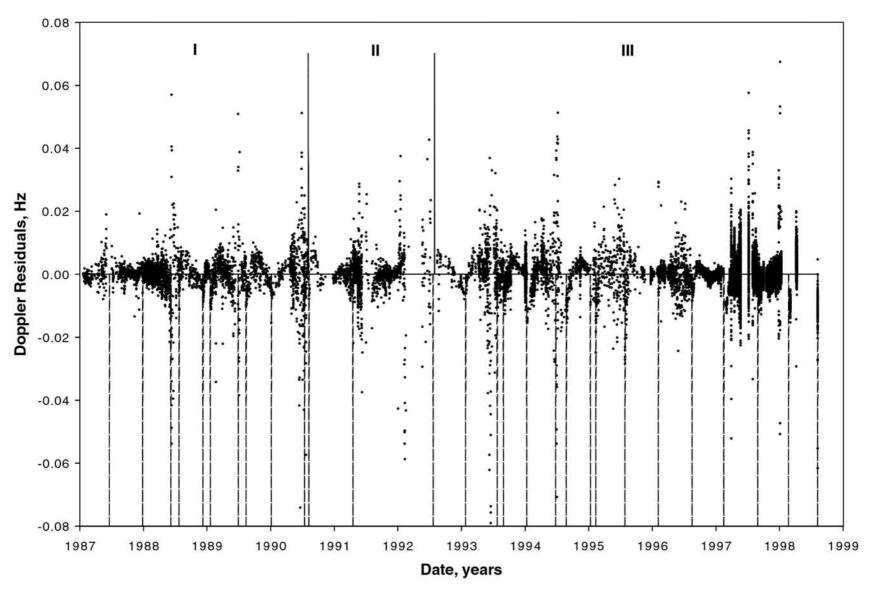






Causes for "de-spin" are different: Pioneer 11 spin increases in between the maneuvers, leaking thruster?

ODP/Sigma residuals



ODP/Sigma Doppler residuals in Hz for the entire Pioneer 10 data span. The two solid vertical lines indicate the boundaries between data Intervals I/II and II/III. Maneuver times are indicated by the vertical dashed lines.





The Pioneer Anomaly: Summary







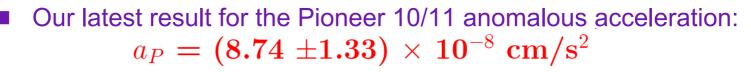




Observations Attempts at Explanations Further Exploration



ZARM, Bremen 18 - 19 May 2004

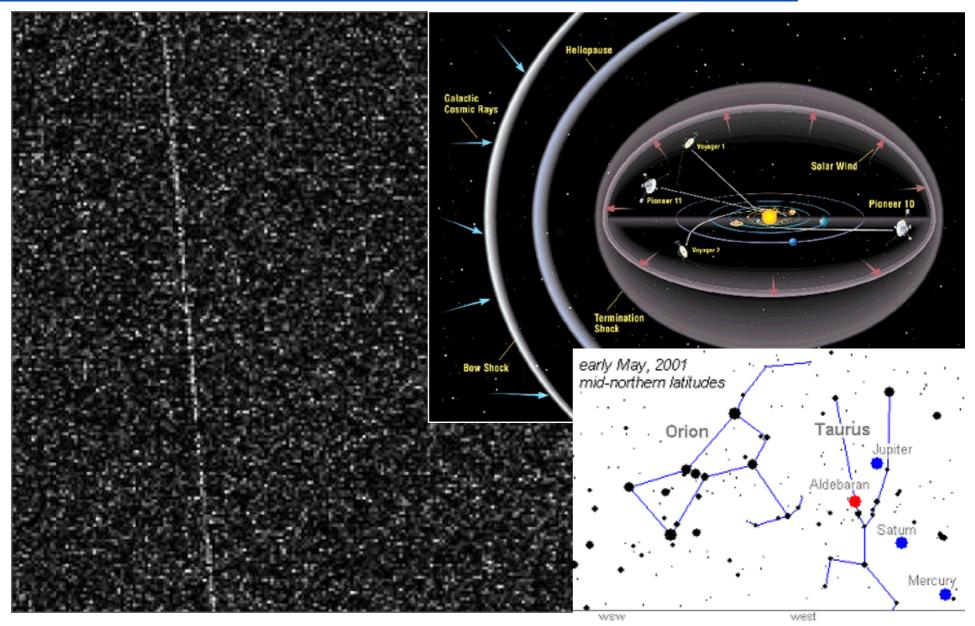


A line of sight constant acceleration of the s/c toward the Sun:

- We find no mechanism or theory that explains the anomaly;
- The most plausible cause is a systematic, yet to be demonstrated.
- Behavior of the Anomaly:
 - We have no real idea how far out the anomaly goes;
 - a_P continues out roughly as a constant from ~10 AU;
 - Constancy: temporal and spatial variations less then 3.4%;
 - Amplified (or turned on) for hyperbolic, escape trajectories (?)
- Three Different Codes Used:
 - JPL Orbit Determination Program [DPODP various generations];
 - Aerospace Corp [CHASPM/POEAS];
 - GSFC ["brewed" by Craig Markward in 2003, data from NSSDC].
 - Next Steps:
 - Early data processing [work initiated at JPL: fly-byes, entire data set]
 - A European study of the PA recently initiated (ZARM, Bremen)

Meanwhile... Pioneer 10 @ Arecibo



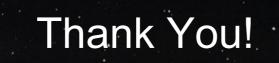


Pioneer 10, as seen by 305 m antenna at Arecibo Observatory, Puerto Rico

One "data point"... we need more!













Solutions for Different Data Intervals



Determinations of the anomalous value for a_P from Intervals of Pioneer 10 and Pioneer 11 data in units of 10^{-8} cm/s²

Program/Estimation method	Pio 10 (I)	Pio 10 (II)	Pio 10 (III)	Pio 11
Sigma, WLS, no solar corona model	8.02 ± 0.01	8.65 ± 0.01	7.83 ± 0.01	8.46 ± 0.04
Sigma, WLS, with solar corona model	8.00 ± 0.01	8.66 ± 0.01	7.84 ± 0.01	8.44 ± 0.04
Sigma, BSF, 1-day batch,	7.82 ± 0.29	8.16 ± 0.40	7.59 ± 0.22	8.49 ± 0.33
with solar corona model		7.77 ± 0.16		
CHASMP, WLS, no solar corona model	8.25 ± 0.02	8.86 ± 0.02	7.85 ± 0.01	8.71 ± 0.03
CHASMP, WLS, with solar corona model	8.22 ± 0.02	8.89 ± 0.02	7.92 ± 0.01	8.69 ± 0.03
CHASMP, WLS, with corona, weighting, and F10.7	8.25 ± 0.03	8.90 ± 0.03	7.91 ± 0.01	8.91 ± 0.04



A Mission to Test the Pioneer Anomaly





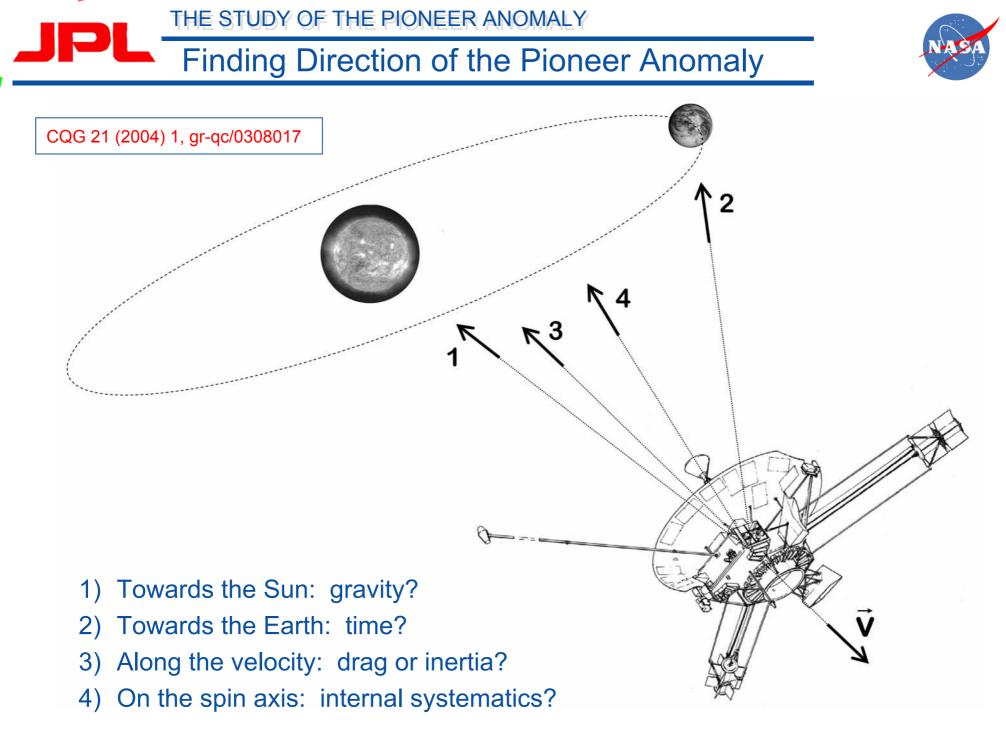






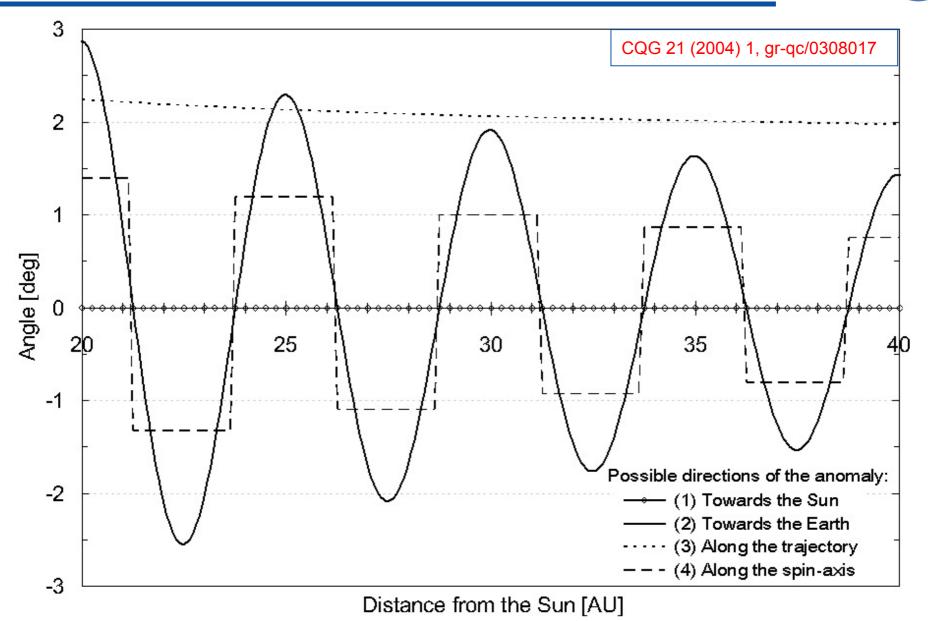
- Mission Objectives:
 - To search for any unmodeled small acceleration affecting the spacecraft motion at the level of <0.1 ×10⁻⁸ cm/s²
 - Determine the physical origin of any anomaly, if found.
- Unique Features:
 - A standard spacecraft bus that allows thermal louvers to be on the sides for symmetric fore/aft thermal rejection.
 - Fore/aft symmetric design with twin antennae (``yo-yo" concept).
- With Off-the-Shelf Technology:
 - Accuracy $\sigma_a \sim 0.06 \times 10^{-8}$ cm/s² is achievable in about 5 years
 - GIVEN THAT the thrusters are reliable and gas leaks can be eliminated or monitored to a high enough accuracy
- New Technology?
 - FAST ORBIT TRANSFER using solar sails, nuclear propulsion
 - DRAG-FREE systems would help, but are not sufficient
 - DC ACCELEROMTERS are very useful
 - OPTICAL COMM very good, but currently very expensive
 - THRUSTERS: good performance and high repeatability are needed

Minimal investment in new technologies would enable not only to test the Anomaly, but also to uniquely determine its Origin.



THE STUDY OF THE PIONEER ANOMALY

Directional Modulation of the Anomaly



Clearly different behavior; easy to separate.



Lessons Learned from the Pioneers



- Attitude Control:
 - 3D ACCELERATION SENSITIVITY: <0.01 \times 10⁻⁸ cm/s² for each axis
 - Spin-stabilized (preferred)
 - If 3D stabilization use of DC accelerometers and reaction wheels
- Navigation & Communication:
 - 3D ACCELERATION SENSITIVITY: <0.01 \times 10⁻⁸ cm/s² for each axis
 - POINTING: control 6 μrad; knowledge 3 μrad; stability 0.1 μrad/s
 - COMM: X and Ka band with significant dual-band tracking
 - DATA TYPES: Doppler, range, $\triangle DOR$, and VLBI
- Thermal Design:
 - ENTIRE SPACECRAFT: heat-balanced & heat-symmetric
 - KNOWLEDGE of all heat sources RTGs, electronics, thrusters, etc
 - ACTIVE CONTROL of all heat dissipation channels within & outward
 - PRECISE KNOWLEDGE of 3D vector of thermal recoil force
 - If spin-stabilized thermal louvers are on the sides of the bus
 - If 3D stabilization harder to balance recoil forces and torques



Investigation emphasized effects previously thought to be insignificant: rejected thermal radiation, gas leaks, radio beam.



Lessons Learned from the Pioneers (2)





- LOCATION: must provide thermal and inertial balance & stability
- If spin-stabilized position as farther as practical from the bus
- If 3D stabilization balance, balance, balance! (see below)
- Propulsion System:
 - Precisely calibrated thrusters, propellant lines & fuel gauges
 - AUTONOMOUS real-time control of their performance
- Symmetric Design ("Yo-Yo" concept):
 - FORE/AFT SYMMETRIC design with TWO identical Cassegrain antennae transmitting in opposite directions, and
 - ROTATE the craft once in a while (done for Pioneer "Earth acquisition maneuver", took ~2.5 hours and 0.5 kg of fuel)

Mission Design:

- TRAJECTORY: a hyperbolic solar system escape trajectory >15 AU from the Sun – possibly in the plane of ecliptic, co-moving with the solar system's direction within the galaxy
- FAST TRANSFER ORBIT spacecraft moving with a velocity of 5 AU or more per year, reaching 15 AU in 3 years time or less
- Heavy class launch vehicle (Delta IV, Proton, Ariane class)
- Solar sail, or nuclear propulsion at least to 15 AU

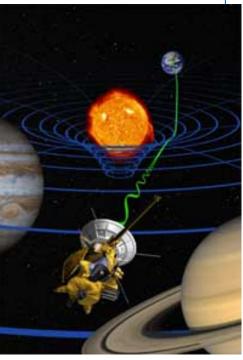


Other Possibilities to Study the Anomaly

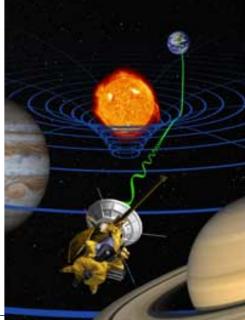




- The 305-meter antenna of the Arecibo Observatory in Puerto Rico might be able to detect Pioneer's signal for a longer time
- The existing data for Pioneer 10 [complete to July 2000]
 - High-rate data from 1978 to Jan 1987: not used in our analysis:
 - Study FLYBYS!
- Current or near future missions:
 - Cassini [RTGs very close]:
 - Heat recoil force ~40×10⁻⁸ cm/s²
 - GP-B [in orbit]
 - Acceleration resolution at ~ 1×10^{-8} m/s²
 - Earth polar circular ~ 92 min orbit,
 - LISA Pathfinder [launch 2006]
 - Acceleration resolution at ~ 1×10⁻¹² cm/s²
 - Multiple noise cancellation strategies







JPL

THE STUDY OF THE PIONEER ANOMALY

Are There Any Other Possibilities?

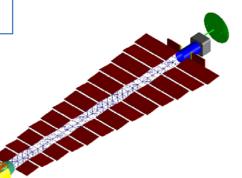


Future missions:

- JIMO [~2012]:
 - Nuclear reactor [unlimited power / weight]
 - Focus on technology, very minimal science
- Pluto-Kiuper [>2014]:
 - The launch data is uncertain at the moment
 - A mission from the Prometheus family?
- Solar Probe [>2016]:
 - a low-mass module may be ejected during solar flyby out of the plane of the ecliptic
- Interstellar Probe [>2020]
- Today's reality:
 - The anomaly source is still unknown
 - Analysis of early data (and the entire set)
 - Needs a wider community support
 - Pioneer is a low priority for NASA
 - Designated mission today is hard, but...



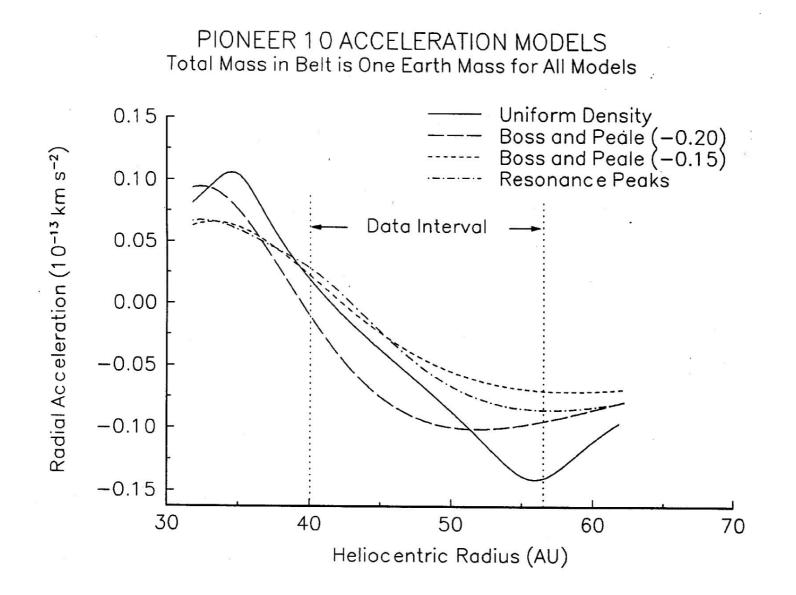
GP-B Launch 04-20-2004



JIMO spacecraft

THE STUDY OF THE PIONEER ANOMALY Dust in the Kuiper Belt





Possible acceleration caused by dust in the Kuiper belt.



Suggested Explanations: Familiar Physics













- A new manifestation of known physics? Interplanetary dust:
 - i) additional gravitational frequency shift; ii) resistance of s/c antennae as they transverse the dust
 - Contradicts to known properties of the interplanetary medium. Density varies greatly within the KB; not large enough to produce acceleration $\sim a_P$
- Dark matter hard to understand:
 - A spherically-symmetric distribution of matter, with $\rho \sim r^{-1}$ produces a constant acceleration inside the distribution.
 - To produce a_P even only out to 50 AU would require the total dark matter $> 3 \times 10^{-4} M_{\odot}$
 - Ephemeris accuracy allows $\sim 10^{-6} M_\odot$ of DM within orbit of Uranus
- Modification of gravity a Yukawa force:

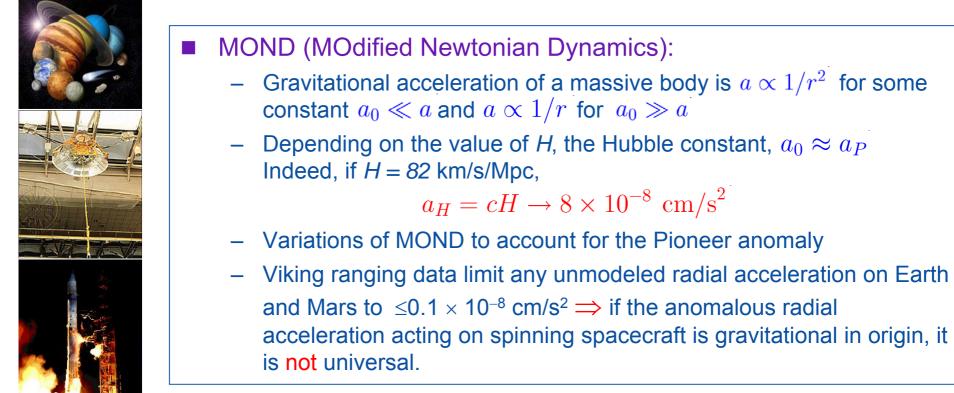
$$V(r) = -\frac{GMm}{(1+\alpha)r} \left[1 + \alpha e^{-r/\lambda} \right] \quad \Rightarrow \quad a_P = -\frac{\alpha a_{\texttt{Newtonian}@\texttt{1AU}}}{2(1+\alpha)} \left(\frac{1AU}{\lambda} \right)^2$$

- α is the new coupling strength relative to Newtonian gravity, and λ is the new force's range. For instance, $\alpha = -1 \times 10^{-3}$ for $\lambda = 200$ AU



Suggested Explanations: MOND & New Physics









- Observation $a_P \sim cH$, stimulated many suggestions:
 - Gravity of the solar system is not static w.r.t. the cosmic expansion
 - 5-D Kaluza-Klein with a time-varying scale factor for 5-th dimension
 - Effect of a scale-dependent cosmological term in the Grav. action
 - Cosmological models with a time-varying Newtonian G(t)



Suggested Explanations: New Physics

















- Long-range scalar field, with oscillatory decline in a_P , d> \approx 100 AU
- Self-interactions of a scalar condensate could be the origins of both Milgrom's inertia modification and also of the Pioneer effect.
- Flavor oscillations of neutrinos in the Brans-Dicke theory of gravity may produce a QM phase shift of neutrinos
- A theory of conformal gravity with dynamical mass generation
- Phenomenological time models:
 - Drifting Clocks; Quadratic Time Augmentation; Carrier Frequency Drift; Speed of Gravity
 - Rejected: poor fits / inconsistent solutions among spacecraft
- Quadratic in time model (pseudo-acceleration, less likely):

$$\Delta \mathtt{TAI} = \mathtt{TAI}_{\mathtt{received}} - \mathtt{TAI}_{\mathtt{sent}} \rightarrow \Delta \mathtt{TAI} + \frac{1}{2}a_{\mathtt{quad}} \cdot \left(\mathtt{TAI}_{\mathtt{received}}^2 - \mathtt{TAI}_{\mathtt{sent}}^2\right)$$

Mimics a line of sight acceleration of s/c, and could be thought of as an expanding space model. Note that a_{quad} affects only the data.

Initial PRL paper was cited ~108 times, including ~ 78 papers with suggested mechanisms to explain the anomaly.

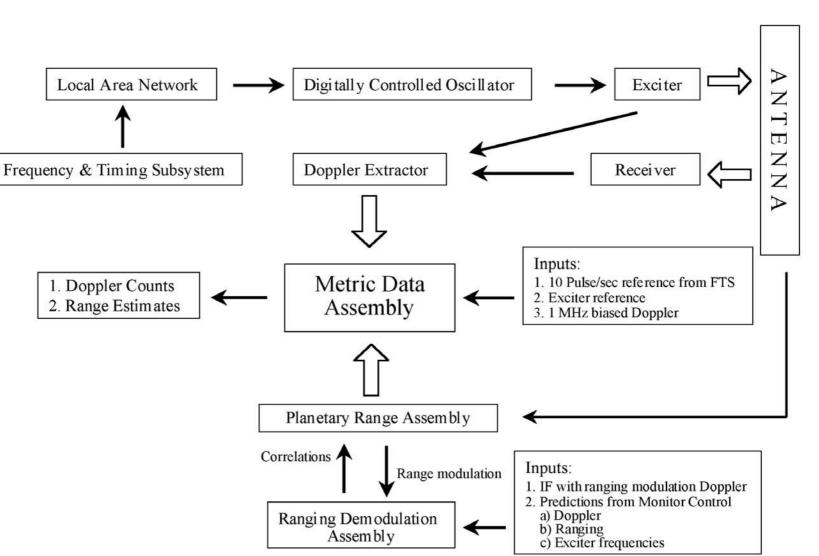


Data Acquisition and Preparation



- Data acquisition with JPL's Deep Space Network (DSN):
 - Goldstone, California; Robledo de Chavela, near Madrid, Spain; Tidbinbilla, near Canberra, Australia.
 - The DSN Frequency and Timing System: At its center is an H-maser that produces a precise and stable reference frequency with Allan deviations of $(1.3 1.0) \times 10^{-12}$, for a 10³ sec Doppler integration time (for the S-band)
- Radio Doppler and range techniques, the most common for navigation
 - Calculations of the motion of a spacecraft are made on the basis of the range time-delay and/or the Doppler shift in the signals
- Data types: ⇒ Pioneer craft have only 2-and 3-way S-band Doppler
 - GLL has S-band range data near the Earth. ULY has 2-/3-way S-up/X-down Doppler and range, S-up/S-down: processed S-up/X-down Doppler and range
- Data preparation and data weighting
 - Considerable effort has gone into estimating measurement errors: to provide the data weights necessary to accurately estimate the parameter adjustments and their associated uncertainties
 - To correct for the Earth's tropospheric refraction (affects Doppler observable) the data can be deweighted for low DSN antennae elevation angles
- Spin calibration of the data:
 - to correct for a Doppler bias due to spinning antennae

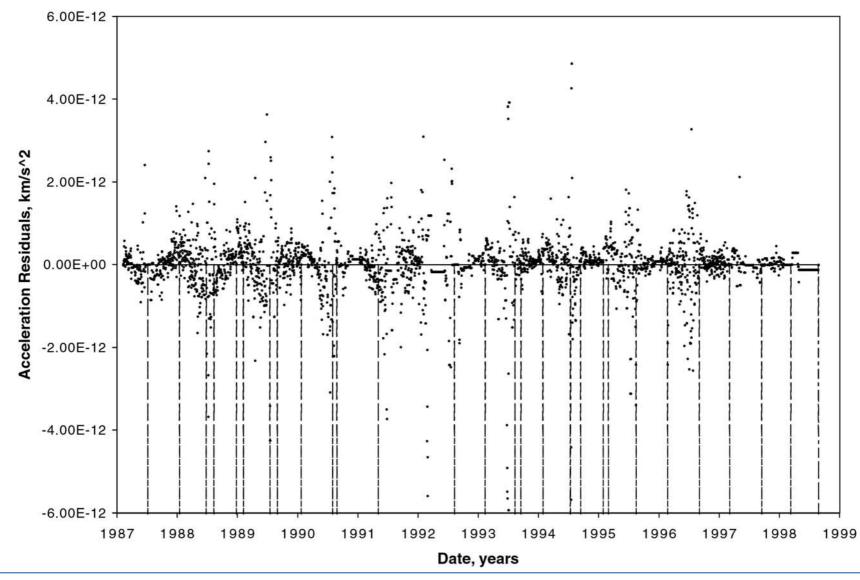






QDP/Sigma 1-day batch residuals





ODP/Sigma 1-day batch-sequential acceleration residuals using the entire Pioneer 10 data set. Maneuver times are indicated by the vertical dashed lines.

The Observed Anomaly





$$\nu_{\text{obs}}(t) - \nu_{\text{model}}(t) = -\nu_0 \frac{2 a_P t}{c} \qquad \nu_{\text{model}} = \nu_0 \left[1 - \frac{2 v_{\text{model}}(t)}{c} \right]$$

$$v_{\text{obs}}(t) - v_{\text{model}}(t) = -2 a_P t$$

Equivalent forms (PRL, 1997):

- Steady frequency drift: $-6 \times 10^{-9} \text{ Hz/s} (\approx 1.5 \text{ Hz/8 yrs})$
- Anomalous acceleration: $a_P = (8.65 \pm 0.03) \times 10^{-8} \ \mathrm{cm/s^2}$
- Clock acceleration: $a_t = -2.8 \times 10^{-18} \text{ s/s}^2$ $a_P \equiv a_t c^2$
- Unknown forces are routinely modeled as stochastic accels:
 - Exponentially correlated in time, with a variable time constant
 - Stochastic variable was sampled in 0-, 5-,10-day batches



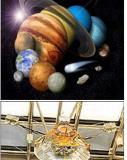


- Basic methods of spacecraft navigation
 - Relativistic equations of motion;
 - Small non-gravitational forces;
 - Data acquisition and preparation.
- The latest (2002) results:
 - An error budget for the anomaly.



Outline for This Talk:









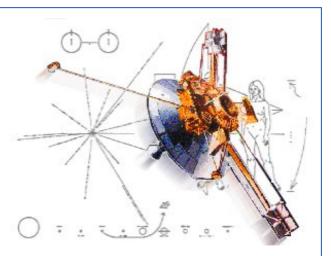


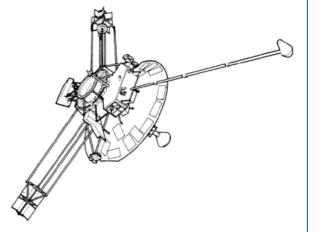


- Pioneer spacecraft and missions
- JPL OD process: data and models
- Initial detection for PA
- How unique these condition?
- Recent Analysis:
 - JPL ODP process
 - Aerospace Corporation
 - Error budget
 - Attempts to explain
- Lessons Learned & Next Steps:
 - Missions of interest
 - A designated mission concept
 - How to get support? NASA? ESA?



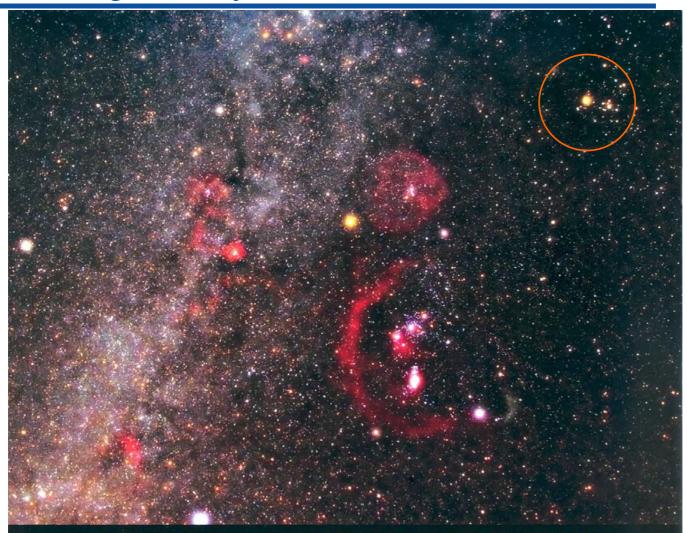
- PA history, analysis, lessons learned, and mission to test the PA











This wide-range time exposure taken from the island of La Palma in the Canary Islands reveals an incredible view of stars, nebulae, the constellation Orion, and the Milky Way. Stretching across the image from the bottom left, faint stars compose the luminous band of the Milky Way. A group of yellowish stars at the upper right is dominated by the red giant Aldebaran, where

A group of yellowish stars at the upper right is dominated by the red giant Aldebaran, where Pioneer 10 is heading.



NR

Typical JPL ODP Output



One data point of Pioneer 10 (spacecraft #23)

		TAG = 18-DEC-1993 16:56:30.0000 = 63 RCVR2 = 0 SC = 2	23 OUASAR= 0 LOCOMP= 0
		= 0 MODFLG= 0 SC = 2	
		= 0 DPLCNL= 0 ODFMT =	0
		FREQCY= 2.19865100000000D+07	•
MOD = 0.0	TA4RNG= 0.0	TB4RNG= 0.0	DDELAY= 0.0
TRAXAZ= 0.0	UDELAY= 0.0	ibildio oto	DDDDDD 010
	LITMT1=-1.905516152720878D+08	T.TTMT2=-1.905228831559969D+08	LITMT3=-1.904941498164381D+0
	DECLIN= 2.565385670180101D+01		ELVATN= 1.220495211596171D+0
	GAMDT3= 2,918020389117413D-03		FOT1S = 2.11070112000000D+0
FOT1E = 2.11070112000000D+09		FOT2E = 0.0	ANOMLY= 1.163801170878523D+(
- L	- <u>-</u>	LTDELE= 5.746549668210349D+04	
WEIGHT= 3.745337887958535D+04	CRESID=-1.653446623261535D-01		Y#23 =-1.258727585963877D-0
Z#23 =-6.132324405729323D-06	DX#23 = 6.153009628897003D+03		DZ#23 = 6.341103997247869D+0
IDLX01= 0.0	IDLX02= 0.0	IDLX03= 0.0	IDLX04= 0.0
IDLX05= 0.0	IDLX06= 0.0	IDLX07= 0.0	IDLX08= 0.0
IDLX09= 0.0	IDLX10= 0.0	IDLX11= 0.0	IDLX12= 0.0
IDLX13= 0.0	IDLX14=-1.470455681092811D+02	IDLX15=-1.208706351258538D+02	IDLX16=-1.115625759316213D+0
IDLX17= 0.0	IDLX18= 0.0	IDLX19= 0.0	IDLX20= 0.0
IDLX21= 0.0	IDLX22= 0.0	IDLX23= 0.0	IDLX24= 0.0
IDLX25= 0.0	IDLX26= 0.0	IDLX27= 0.0	IDLX28= 0.0
IDLY01= 0.0	IDLY02= 0.0	IDLY03= 0.0	IDLY04= 0.0
IDLY05= 0.0	IDLY06= 0.0	IDLY07= 0.0	IDLY08= 0.0
IDLY09= 0.0	IDLY10= 0.0	IDLY11= 0.0	IDLY12= 0.0
IDLY13= 0.0	IDLY14=-1.286147747152502D+03	IDLY15=-8.315020516699011D+02	IDLY16=-7.983072615565676D+0
IDLY17= 0.0	IDLY18= 0.0	IDLY19= 0.0	IDLY20= 0.0
IDLY21= 0.0	IDLY22= 0.0	IDLY23= 0.0	IDLY24= 0.0
IDLY25= 0.0	IDLY26= 0.0	IDLY27= 0.0	IDLY28= 0.0
IDL201= 0.0	IDL202= 0.0	IDLZ03= 0.0	IDLZ04= 0.0
IDL205= 0.0	IDL206= 0.0	IDL207= 0.0	IDLZ08= 0.0
IDLZ09= 0.0	IDLZ10= 0.0	IDLZ11= 0.0	IDLZ12= 0.0
IDLZ13= 0.0		IDLZ15= 1.526356368098403D+04	
IDLZ17= 0.0	IDLZ18= 0.0	IDLZ19= 0.0	IDLZ20= 0.0
IDLZ21= 0.0	IDLZ22= 0.0	IDLZ23= 0.0	IDLZ24= 0.0
IDLZ25= 0.0	IDLZ26= 0.0	IDLZ27= 0.0	IDLZ28= 0.0
		DQB = 7.430250199658943D+03	
LO15 = 0.0	LO45 = 0.0	LO65 = 0.0	CV15 = 0.0
CV45 = 0.0	CV65 = 0.0	CU15 = 0.0	CU45 = 0.0
CU65 = 0.0	TROPD1= 0.0	TROPD4= 0.0	TROPD6=-7.762295546211375D-0
TROPW1= 0.0	TROPW4= 0.0	TROPW6=-8.198786392866827D-03	
IONOD4= 0.0	IONOD6= 1.473019617742985D-03		IONON4= 0.0
IONON6= 1.164612155473165D-03		CORONB= 0.0	CORONC= 0.0
ATAX =-6.427129029451515D+09	ATAY =-5.168770634162122D+10	ARESID=-5.167094074983632D-01	



Typical CHASPM Output



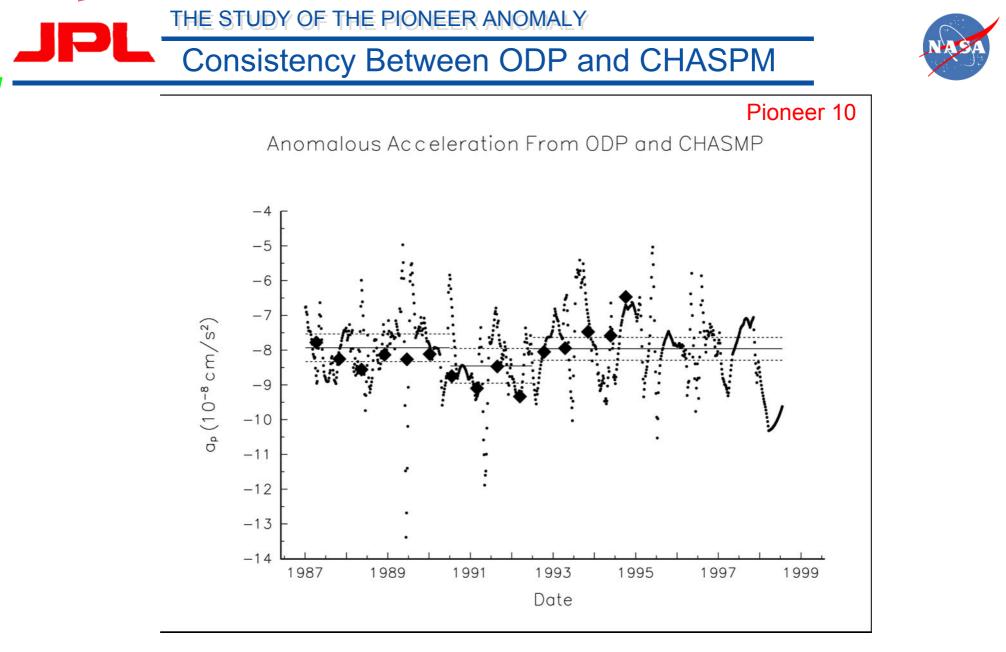






Several data points of Pioneer 10 (spacecraft #23)

1	88/ 4/17,17,56, 0 1980.00	23	43	63	0	0 1 13	21987700. 52.0 0.510827173879D+06 0.3030D-03	-0.0008
;	88/ 4/18, 2,24, 0 1980.00	23	63	43	0	0 1 13	21987690. 20.0 0.504492409138D+06 0.3030D-03	-40.7520*
;	88/ 4/18, 2,57, 0 1980.00	23	63	43	0	0 1 13	21987690. 23.7 0.505005776239D+06 0.3030D-03	0.0113
1	88/ 4/18, 3,30, 0 1980.00	23	63	43	0	0 1 13	21987690. 26.5 0.505558847051D+06 0.3030D-03	0.0031
1	88/ 4/18, 4, 3, 0 1980.00	23	63	43	0	0 1 13	21987690. 28.5 0.506137439698D+06 0.3030D-03	-0.0018
;	88/ 4/18, 4,36, 0 1980.00	23	63	43	0	0 1 13	21987690. 29.5 0.506726840179D+06 0.3030D-03	-0.0005
1	88/ 4/18, 5, 9, 0 1980.00	23	63	43	0	0 1 13	21987690. 29.6 0.507312108399D+06 0.3030D-03	-0.0003
;	88/ 4/18, 5,47, 0 1980.00	23	63	43	0	0 1 13	21987690. 28.4 0.507961620275D+06 0.3030D-03	0.0020
;	88/ 4/18, 6,20, 0 1980.00	23	63	43	0	0 1 13	21987690. 26.3 0.508488162344D+06 0.3030D-03	-0.0035
;	88/ 4/18, 6,53, 0 1980.00	23	63	43	0	0 1 13	21987690. 23.3 0.508965482866D+06 0.3030D-03	-0.0073
;	88/ 4/18, 7,26, 0 1980.00	23	63	43	0	0 1 13	21987690. 19.7 0.509380968958D+06 0.3030D-03	-0.0047
;	88/ 4/18, 7,59, 0 1980.00	23	63	43	0	0 1 13	21987690. 15.3 0.509723294729D+06 0.3030D-03	0.0004
;	88/ 4/18, 8,32, 0 1980.00	23	63	43	0	0 1 13	21987690. 10.5 0.509982656658D+06 0.3030D-03	-0.0084
;	88/ 4/19,16,27, 0 1980.00	23	43	63	0	0 1 13	21987650. 66.5 0.498147871473D+06 0.3030D-03	-0.0034
1	88/ 4/19,17, 0, 0 1980.00	23	43	63	0	0 1 13	21987650. 60.9 0.498718348338D+06 0.3030D-03	0.0027
;	88/ 4/19,17,33, 0 1980.00	23	43	63	0	0 1 13	21987650. 54.9 0.499271982352D+06 0.3030D-03	-0.0038
1	88/ 4/19,18, 6, 0 1980.00	23	43	63	0	0 1 13	21987650. 48.7 0.499794517663D+06 0.3030D-03	-0.0090
;	88/ 4/19,18,39, 0 1980.00	23	43	63	0	0 1 13	21987650. 42.4 0.500272344269D+06 0.3030D-03	-0.0012
;	88/ 4/19,19,12, 0 1980.00	23	43	63	0	0 1 13	21987650. 36.1 0.500692782808D+06 0.3030D-03	0.0074
;	88/ 4/20, 8,26, 0 1980.00	23	63	43	0	0 1 13	21987640. 10.2 0.497548795704D+06 0.3030D-03	0.0008
1	88/ 4/21, 3,54,50 1980.00	23	63	43	0	0 1 13	21987610. 28.6 0.487972894111D+06 0.3030D-03	27.6121*
1	38/ 4/21, 4,27,50 1980.00	23	63	43	0	0 1 13	21987610. 29.6 0.488557137090D+06 0.3030D-03	0.0008
1	88/ 4/21, 5, 0,50 1980.00	23	63	43	0	0 1 13	21987610. 29.5 0.489136159058D+06 0.3030D-03	-0.0051
-								



ODP: 5-day sample averages of using BSF with a 200-day correl time (dots). Solid lines – mean values of a_P in three Intervals; dashed lines – large BSF computational error bounds. CHASMP: The 200-day accel values using CHASMP – solid squares.