

# From molecular clouds to protostellar cores

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Many thanks to: G. Chabrier, P. Marchand, J. Masson (CRAL Lyon)  
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N. Vaytet (NBI Copenhagen), R. Teyssier (Zurich)

# Outline

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## 1. Introduction

## 2. Molecular clouds

- formation
- evolution

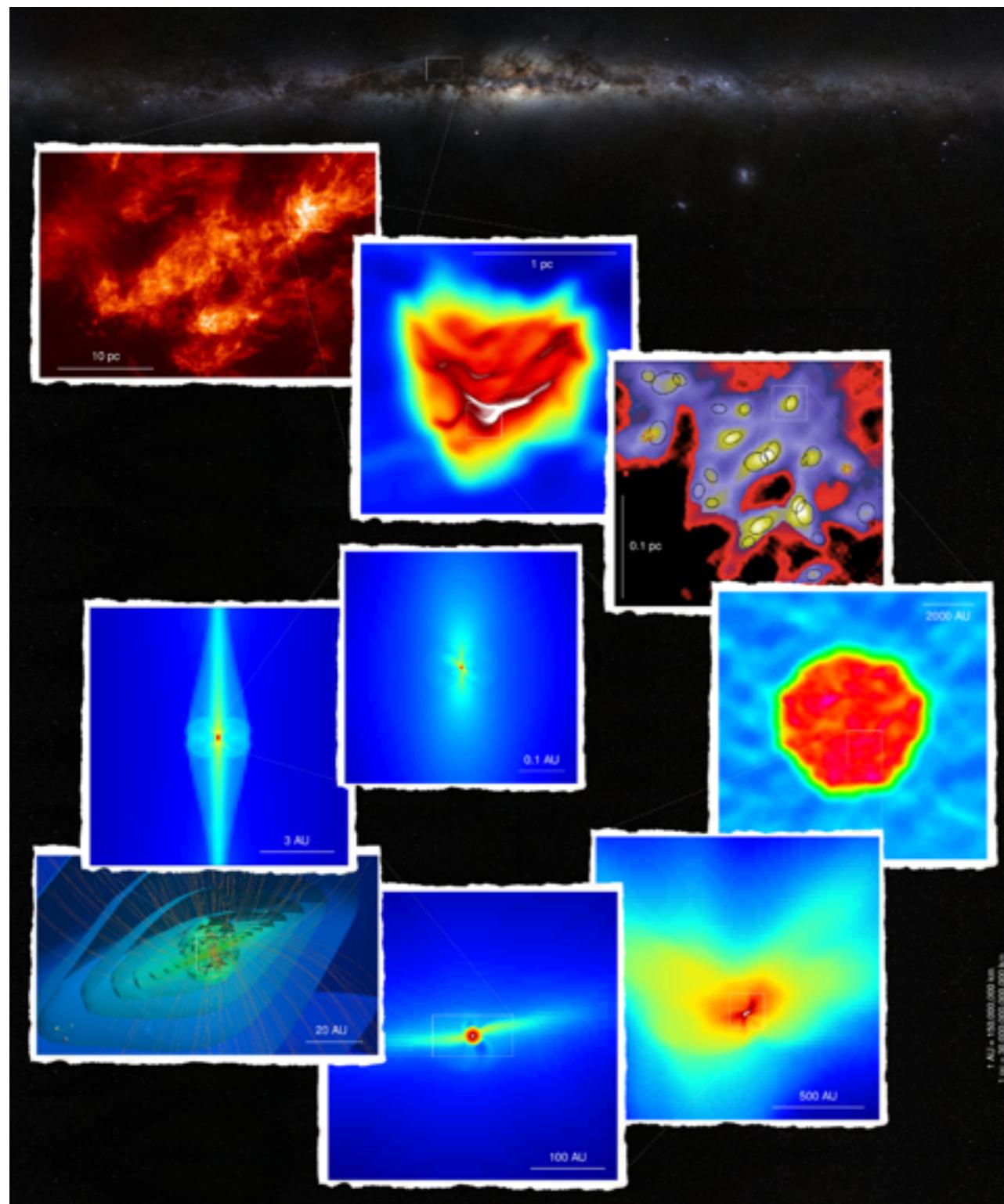
## 3. Dense core

- formation
- low mass star evolution sequence

## 4. Cluster formation

- binary
- IMF

# Star formation: building blocks & challenge



Vaytet et al. (2013)

- from parsec scale ( $10^{18}$  cm) to stellar radius ( $10^{10}$  cm)
- density: from  $1 \text{ cm}^{-3}$  to  $10^{24} \text{ cm}^{-3}$
- temperature:  $10 \text{ K}$  -  $10^6 \text{ K}$
- ionisation depends on density and temperature... (*ideal vs non-ideal MHD*)
- chemistry, dust grain evolution ( *$H_2$  formation, growth, evaporation*)
- initial conditions for stellar evolution (*entropy level, magnetic field flux/geometry, angular momentum*)

# What do we find in the interstellar medium?

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- photons at all wavelengths
  - gas (mainly H, 10% He and  $10^{-4}$  heavy elements), turbulent
  - magnetic fields (from galactic dynamo?)
  - dust (solid phase, 1% mass compared to the gas), but (thermo)dynamically important...
  - cosmic rays (high energy particles)
- 
- multifold research field, all processes couple together...
  - slow progress, but progress

# Energy equipartition

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$$E_{\text{th}} = E_{\text{grav}} = E_{\text{kin}} = E_{\text{mag}} = E_{\text{rad}} = E_{\text{cr}} \sim 1 \text{ ev/cm}^3$$

- **Thermal energy:**  $P/k \sim 4000 \text{ K/cm}^3$   
 $\Rightarrow E_{\text{th}} = P/(\gamma - 1) \sim 10^{-12} \text{ erg/cm}^3$
- **Kinetic energy:** Mach number  $\sim 4$   
 $\Rightarrow E_{\text{kin}} = 0.5(\gamma - 1)E_{\text{th}}\mathcal{M}^2 \sim 5 E_{\text{th}}$

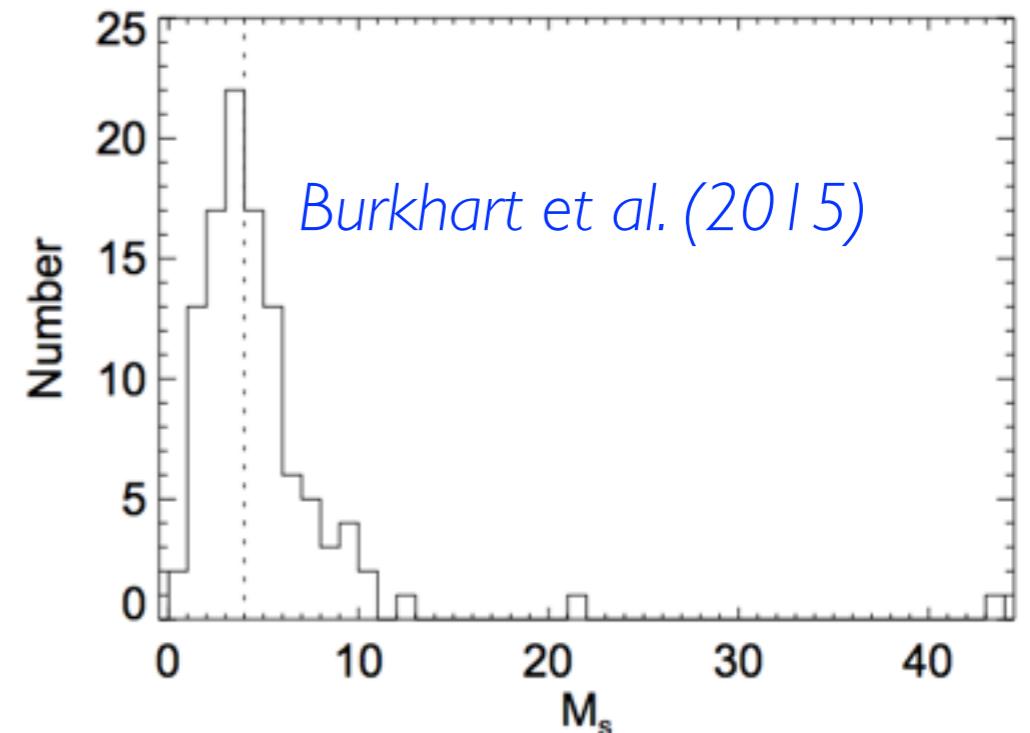


FIG. 3.— Histogram of the sonic Mach number as calculated from the absorption line data for Perseus. The median value is  $M_s = 4.0$  and is shown with a straight vertical line.

# Energy equipartition

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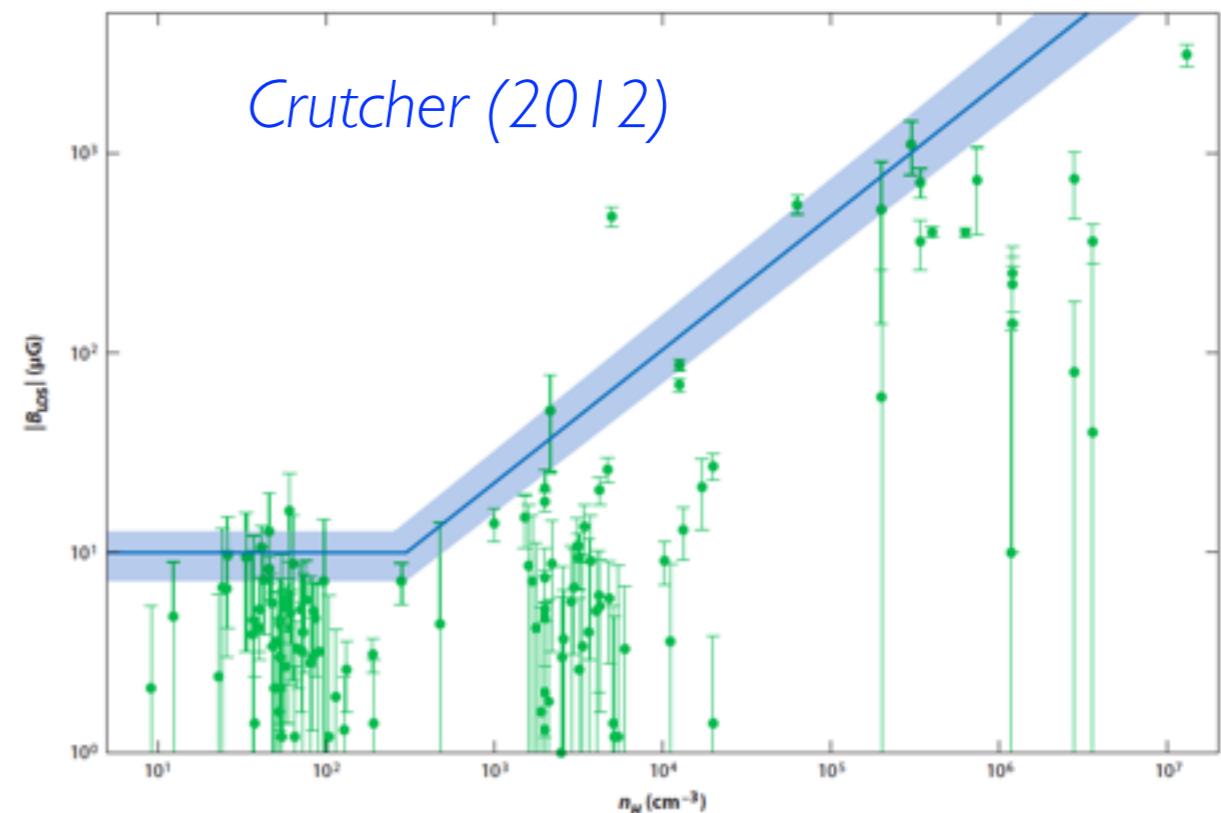
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- Kinetic energy: Mach number  $\sim 4$

$$\Rightarrow E_{\text{kin}} = 0.5(\gamma - 1)E_{\text{th}} \mathcal{M}^2 \sim 5 E_{\text{th}}$$

- Magnetic energy:  $B \sim 10 \mu\text{G}$

$$\Rightarrow E_{\text{mag}} = B^2/(8\pi) \sim 4 \times 10^{-12} \text{ erg/cm}^3$$



# Energy equipartition

$$E_{\text{th}} = E_{\text{grav}} = E_{\text{kin}} = E_{\text{mag}} = E_{\text{rad}} = E_{\text{cr}} \sim 1 \text{ ev/cm}^3$$

- Radiation energy

Component of ISRF	Energy density ( $\text{erg cm}^{-3}$ )
Synchrotron	$2.7 \times 10^{-18}$
CMB	$4.19 \times 10^{-13}$
Dust emission	$5.0 \times 10^{-13}$
Nebular emission (bf, ff)	$4.5 \times 10^{-15}$
Nebular emission ( $\text{H}\alpha$ )	$8 \times 10^{-16}$
Nebular emission (other bb)	$10^{-15}$
Starlight, $T_1 = 3000 \text{ K}$	$4.29 \times 10^{-13}$
Starlight, $T_2 = 4000 \text{ K}$	$3.19 \times 10^{-13}$
Starlight, $T_3 = 7000 \text{ K}$	$2.29 \times 10^{-13}$
Starlight, power-law	$7.11 \times 10^{-14}$
Starlight, total	$1.05 \times 10^{-12}$
Soft X-rays	$10^{-17}$

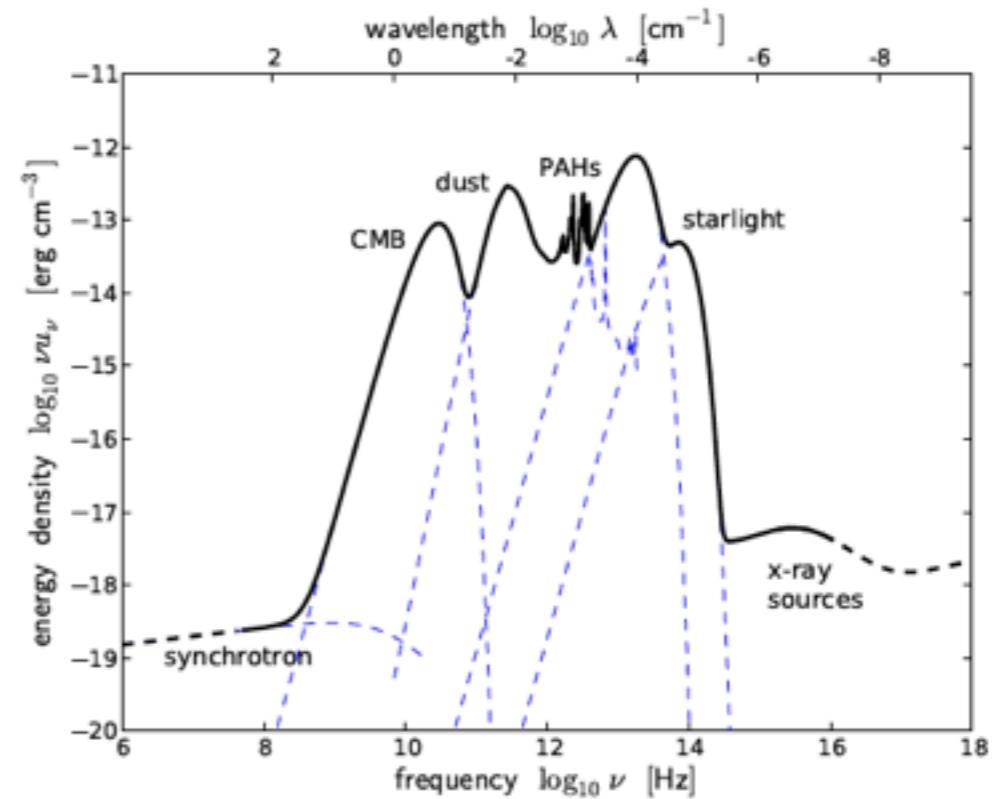


Fig. 1 Schematic sketch of the energy density of the interstellar radiation field at different frequencies. The contributions of the cosmic microwave background (CMB) as well as of old, low-mass and young, high-mass stars are taken to be perfect blackbodies with temperatures 2.73K, 3500K, and 18000K, respectively (see Chakraborty & Fields, 2013). The contributions from dust and PAHs are obtained from Draine & Li (2007). The estimate for the Galactic synchrotron emission is taken from Draine (2011) and the one for the X-ray flux from Snowden et al. (1997). Note that in the vicinity of massive star clusters, the contributions from massive stars can be orders of magnitude larger than the numbers provided here. For further discussions, see for example Draine (2011).

# Molecular cloud evolution

- Molecular clouds are turbulent
  - Power-laws over decades => turbulent cascade?

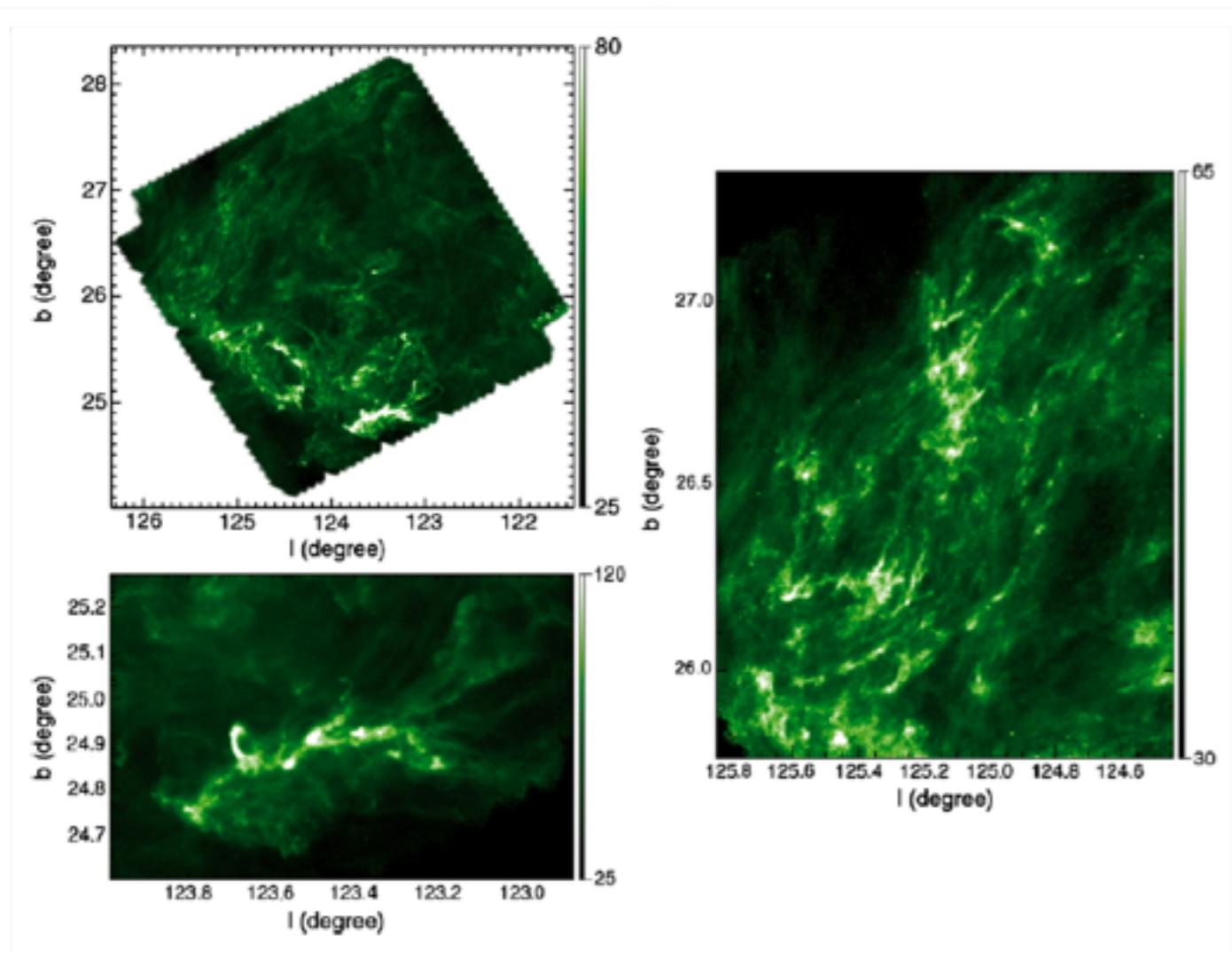
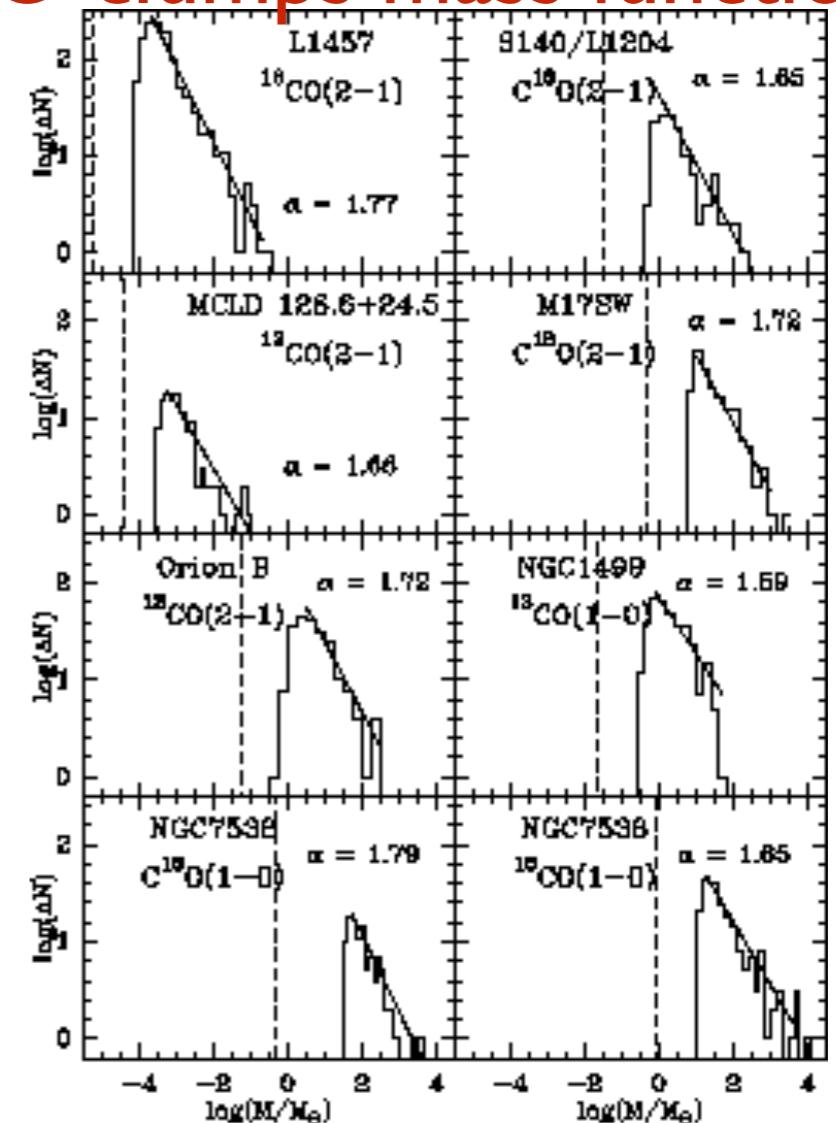


Fig. 11 Left: *Herschel*/SPIRE 250  $\mu\text{m}$  map of the Polaris Flare over  $\sim 7 \text{ pc} \times 7 \text{ pc}$ . Units are  $\text{MJy sr}^{-1}$  (top). Subfield of the region of largest column density discussed in Sect. 3.6 (bottom). Right: Another subset of regions of lowest column density. Note the brightness difference (from Miville-Deschénes et al. 2010)

CO clumps mass functions

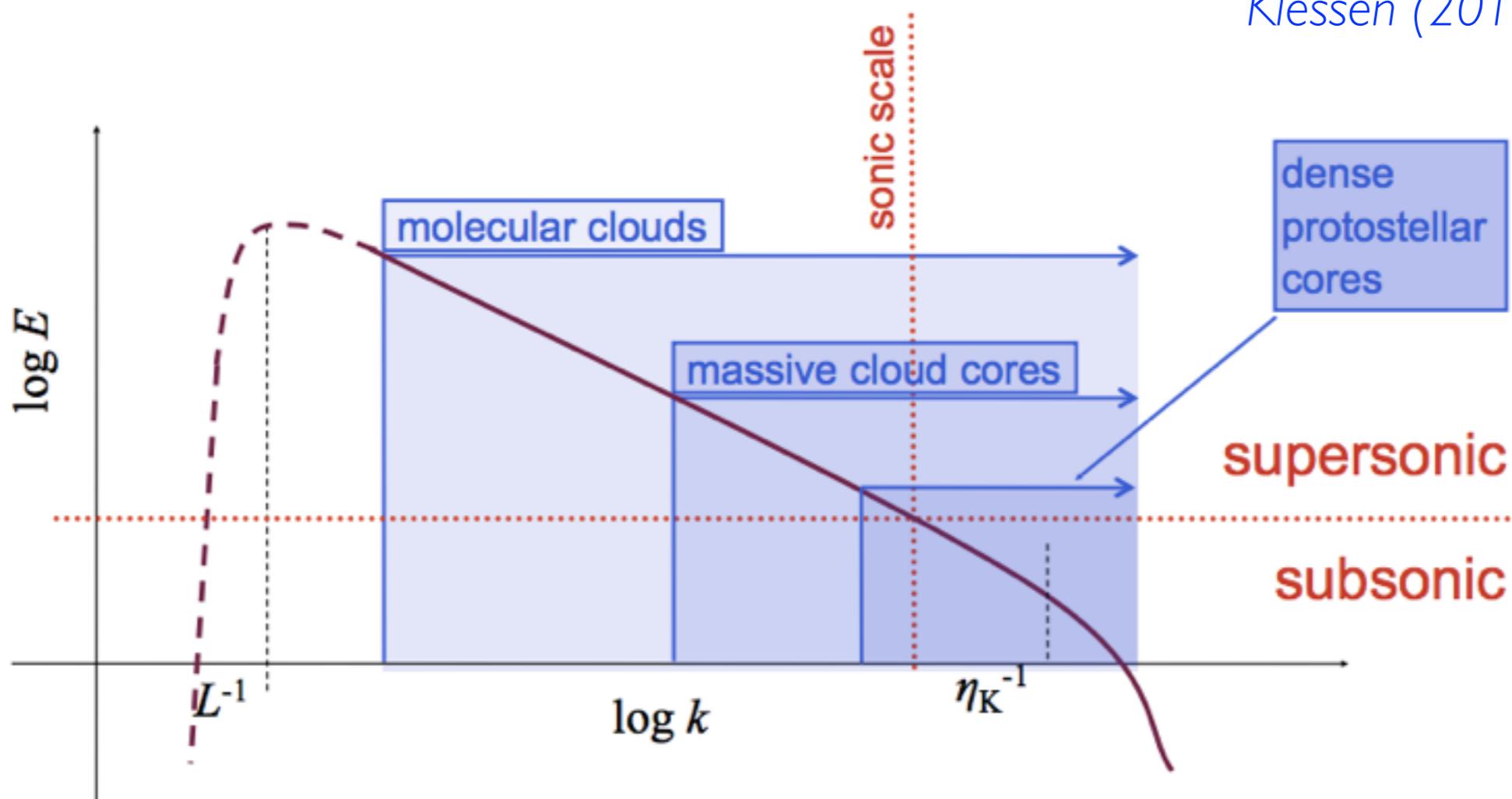


Kramer et al. (1998)

# Molecular cloud evolution

- Molecular clouds are turbulent

Klessen (2010)



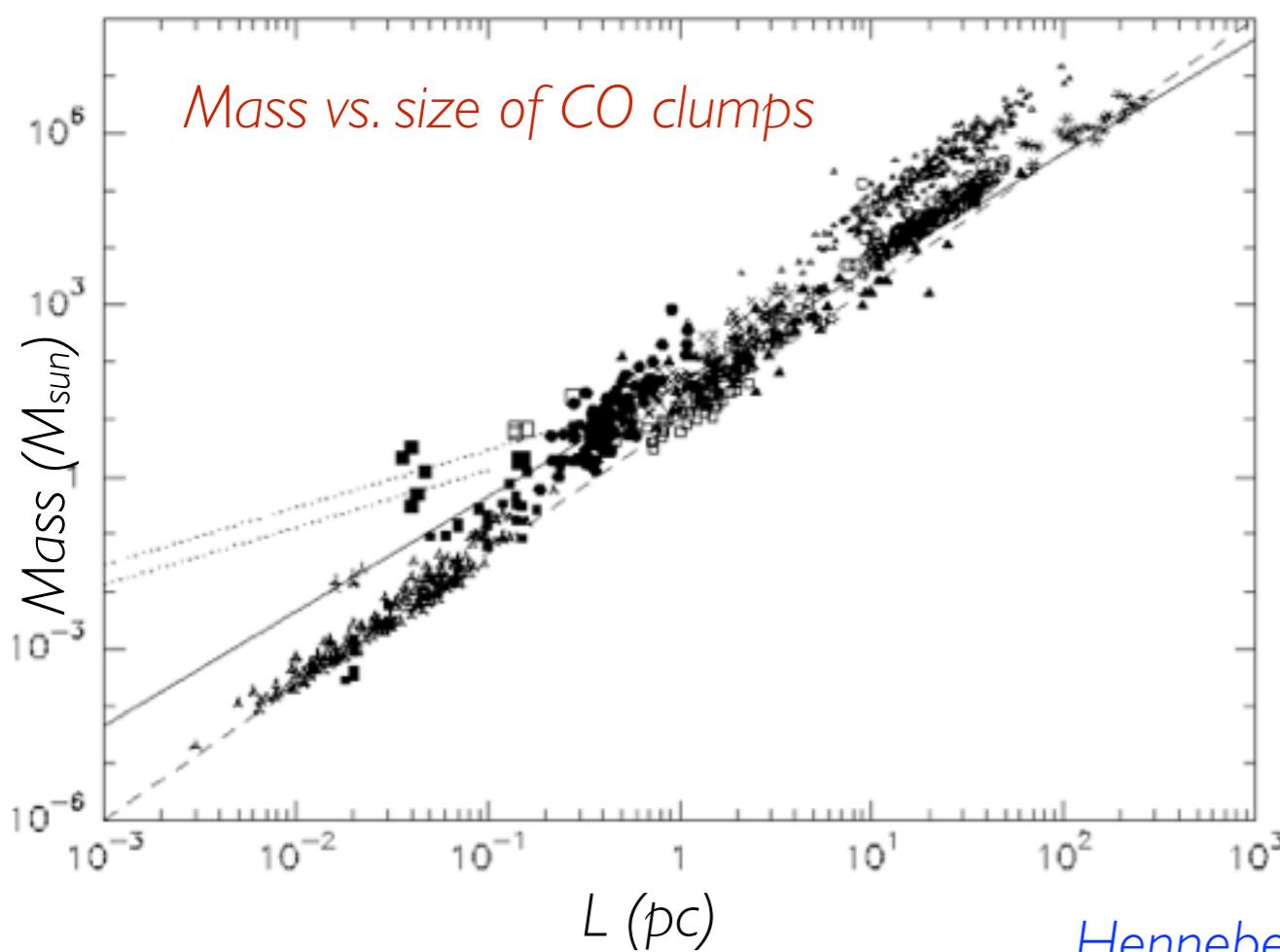
**Fig. 2.** Simple cartoon picture of the turbulent energy spectrum, i.e. of the kinetic energy carried by modes of different wave numbers  $k$ , and their relation to different cloud structures (see also Table 1). Turbulence is driven on large scales comparable to the size  $L$  of the cloud and is dissipated on very small scales  $\eta_K$ .

# Molecular cloud evolution

- Molecular clouds are turbulent

Larson (1981) relations

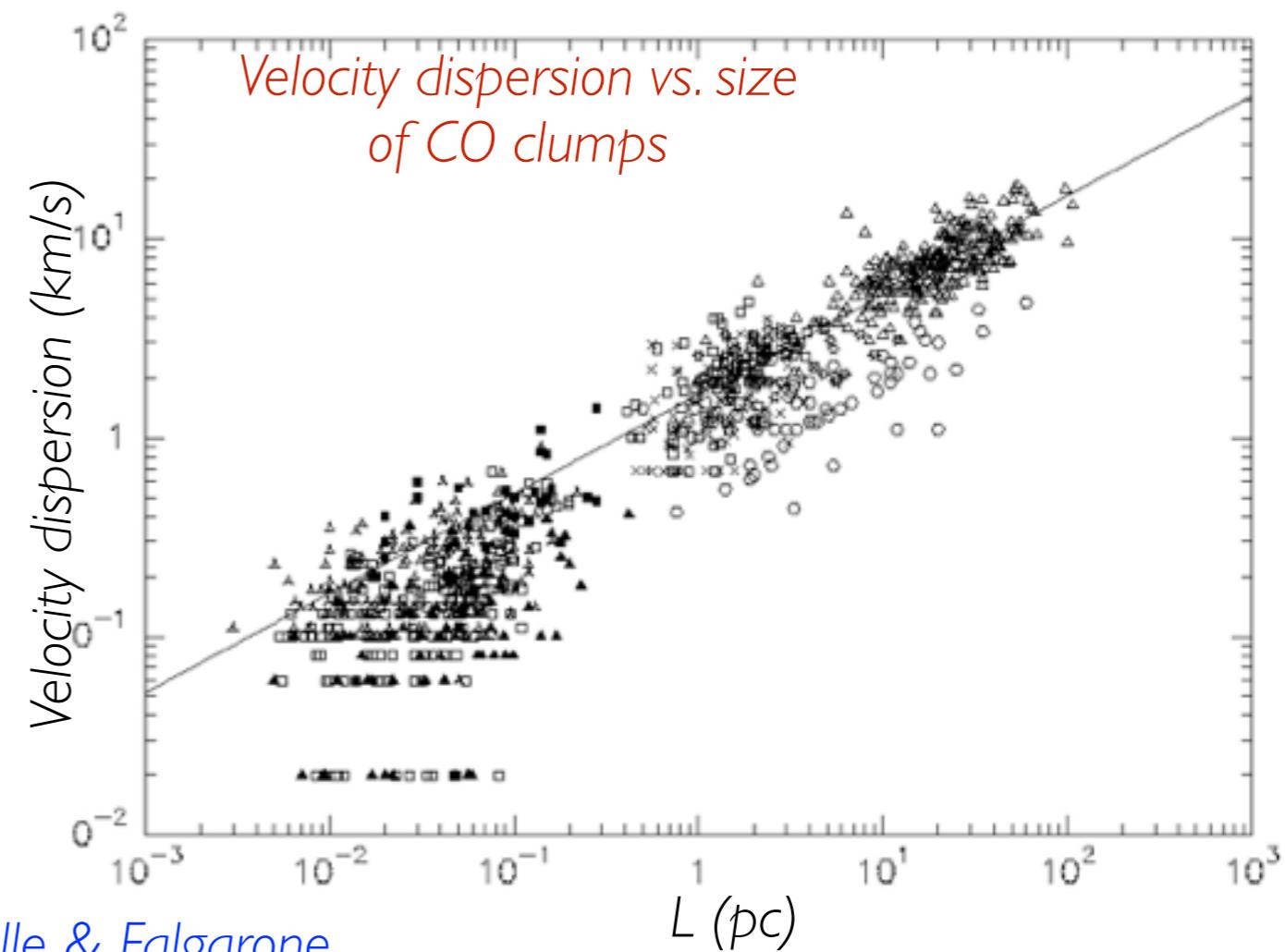
$$n = 3000 \text{ cm}^{-3} \left( \frac{L}{1 \text{ pc}} \right)^{-0.7}$$



Mass vs. size of CO clumps

$$\Delta v_{\text{NT}} \sim 1 \text{ km s}^{-1} \left( \frac{L}{1 \text{ pc}} \right)^{0.5}$$

$$\Delta v_{\text{NT}} \sim 1 \text{ km s}^{-1} \left( \frac{n}{3000 \text{ cm}^{-3}} \right)^{-5/7}$$



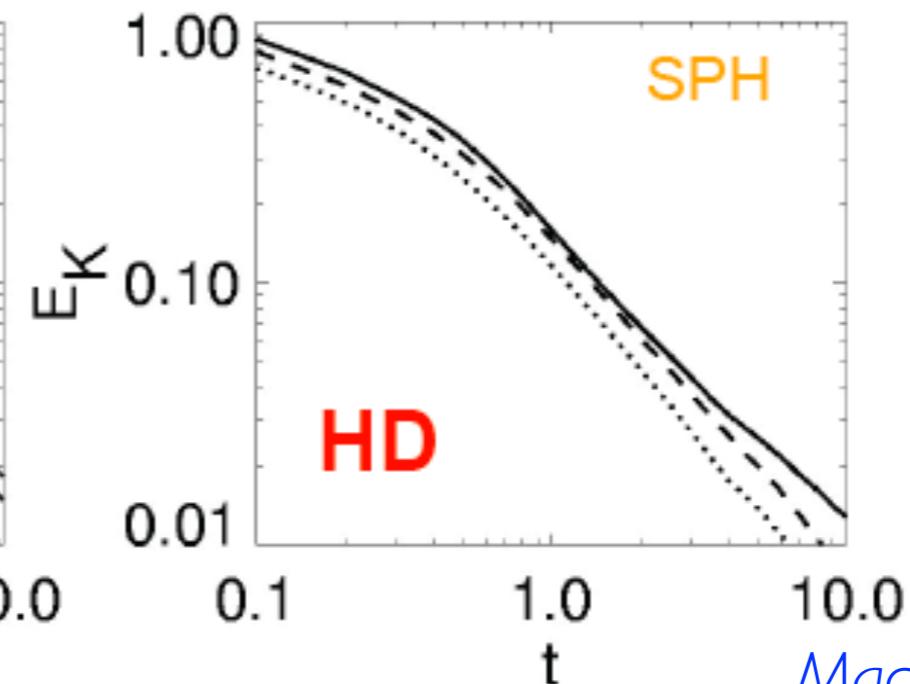
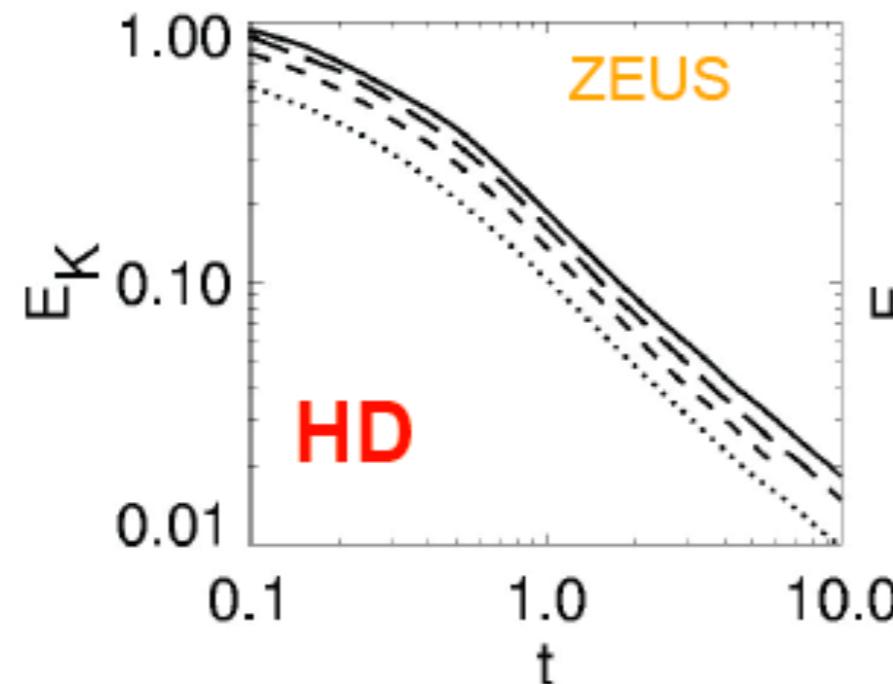
Velocity dispersion vs. size  
of CO clumps

Hennebelle & Falgarone  
(2012 A&ARA)

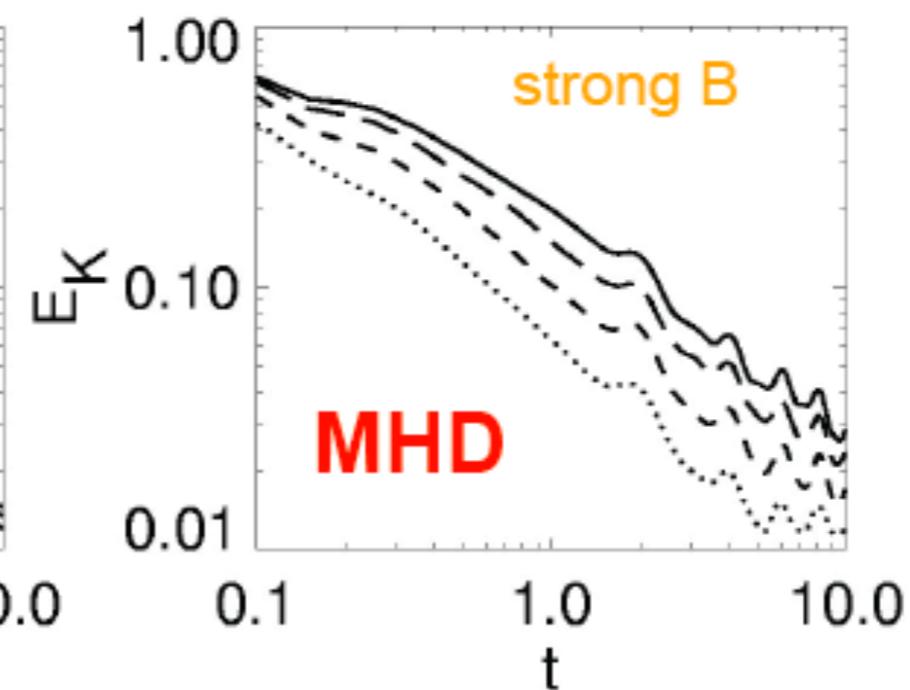
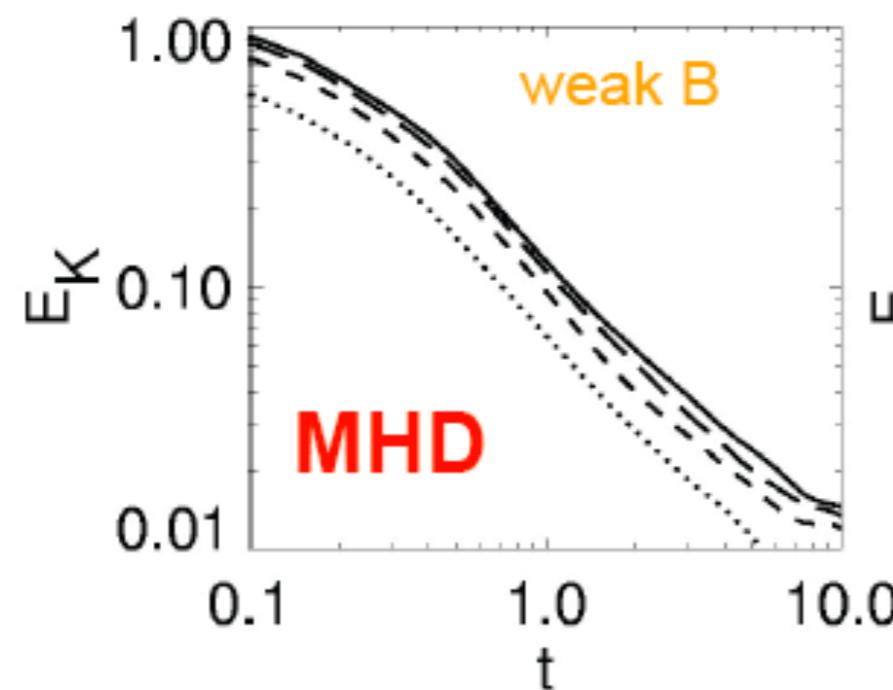
# Turbulence in molecular clouds

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- Energy dissipation



Mac Low et al. (1998)



# Energy dissipation

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See the discussion in [Klessen & Glover \(2014\)](#)

- **Energy dissipation**  $L_d/v_{\text{rms}}$

✓ energy is dissipated in a crossing time

✓ dissipation rate:

$$\dot{e} = \frac{1/2\rho v_{\text{rms}}^2}{(L_d/v_{\text{rms}})} = \frac{1/2\rho v_{\text{rms}}^3}{L_d}$$

✓ For typical numbers:

$$\dot{e} = 3 \times 10^{-27} \text{ erg cm}^{-3} \text{s}^{-1} \left( \frac{n}{1 \text{ cm}^{-3}} \right) \left( \frac{v_{\text{rms}}}{10 \text{ km s}^{-1}} \right)^3 \left( \frac{L_d}{100 \text{ pc}} \right)^{-1}$$

✓ energy injection must compensate this dissipation

# Source of energy injection

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See the discussion in [\*Klessen & Glover \(2014\)\*](#)

- Different mechanisms, but no definitive answer:
  - ✓ accretion at galactic scales
  - ✓ supernova explosion
  - ✓ spiral arms
  - ✓ gravitational instability
  - ✓ HII region
  - ✓ protostellar jets
- Connect large scale (galaxy) and small scales (protostars) - yet this is another story!

# Energy injection

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- **Accretion onto the galaxy** ([Klessen & Hennebelle 2010](#))
  - ✓ galaxies are fed by gas entering the dark matter halo
  - ✓ needs to replenish the gas content at a rate similar to the SFR ( $2\text{-}4 \text{ M}_\odot/\text{yr}$ )
  - ✓ energy injection rate:
$$\dot{e} = \rho \dot{\epsilon} = \frac{1}{2} \rho \frac{\dot{M}_{\text{in}}}{M_{\text{gas}}} v_{\text{in}}^2$$
$$= 6.2 \times 10^{-27} \text{ erg cm}^{-3} \text{ s}^{-1} \left( \frac{n}{1 \text{ cm}^{-3}} \right) \left( \frac{\dot{M}_{\text{in}}}{3 \text{ M}_\odot \text{ yr}^{-1}} \right) \left( \frac{v_{\text{in}}}{220 \text{ km s}^{-1}} \right)^2$$
  - ✓ Only a few percent of this energy input is needed to explain the energy dissipation rate
  - ✓ but... accretion is not steady and the conversion of kinetic to turbulent energy depends linearly on the density contrast

# Energy injection

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- Rotation of the galaxy (*Klessen & Glover 2014*)
  - ✓ rotation energy can be converted into turbulent energy

- spiral arms
- energy injection rate:

$$\begin{aligned}\dot{e} &\approx G(\Sigma_g/H)^2 L^2 \Omega \\ &\approx 4 \times 10^{-29} \text{ erg cm}^{-3} \text{ s}^{-1} \times \\ &\quad \times \left( \frac{\Sigma_g}{10 M_\odot \text{ pc}^{-2}} \right)^2 \left( \frac{H}{100 \text{ pc}} \right)^{-2} \left( \frac{L}{100 \text{ pc}} \right)^2 \left( \frac{\Omega}{(220 \text{ Myr})^{-1}} \right)\end{aligned}$$

- magneto-rotational instability (*Balbus & Hawley 1998*)
- energy injection rate (*Sellwood & Balbus 1999*)

$$\dot{e} = 3 \times 10^{-29} \text{ erg cm}^{-3} \text{ s}^{-1} \left( \frac{B}{3 \mu \text{G}} \right)^2 \left( \frac{\Omega}{(220 \text{ Myr})^{-1}} \right)$$

# Energy injection

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- Stellar feedback

✓ supernovae

$$\dot{e} = \frac{\sigma_{\text{SN}} \xi_{\text{SN}} E_{\text{SN}}}{\pi R_{\text{sf}}^2 H}$$
$$= 3 \times 10^{-26} \text{ erg s}^{-1} \text{ cm}^{-3} \times$$
$$\times \left( \frac{\xi_{\text{SN}}}{0.1} \right) \left( \frac{\sigma_{\text{SN}}}{(100 \text{ yr})^{-1}} \right) \left( \frac{H}{100 \text{ pc}} \right)^{-1} \left( \frac{R}{15 \text{ kpc}} \right)^{-2} \left( \frac{E_{\text{SN}}}{10^{51} \text{ erg}} \right)$$

✓ protostellar jets and outflow

$$L_{\text{jet}} = \frac{1}{2} \dot{M}_{\text{jet}} v_{\text{jet}}^2 = 1.3 \times 10^{32} \text{ erg s}^{-1} \left( \frac{\dot{M}_{\text{jet}}}{10^{-8} M_{\odot} \text{ yr}^{-1}} \right) \left( \frac{v_{\text{jet}}}{200 \text{ km s}^{-1}} \right)$$

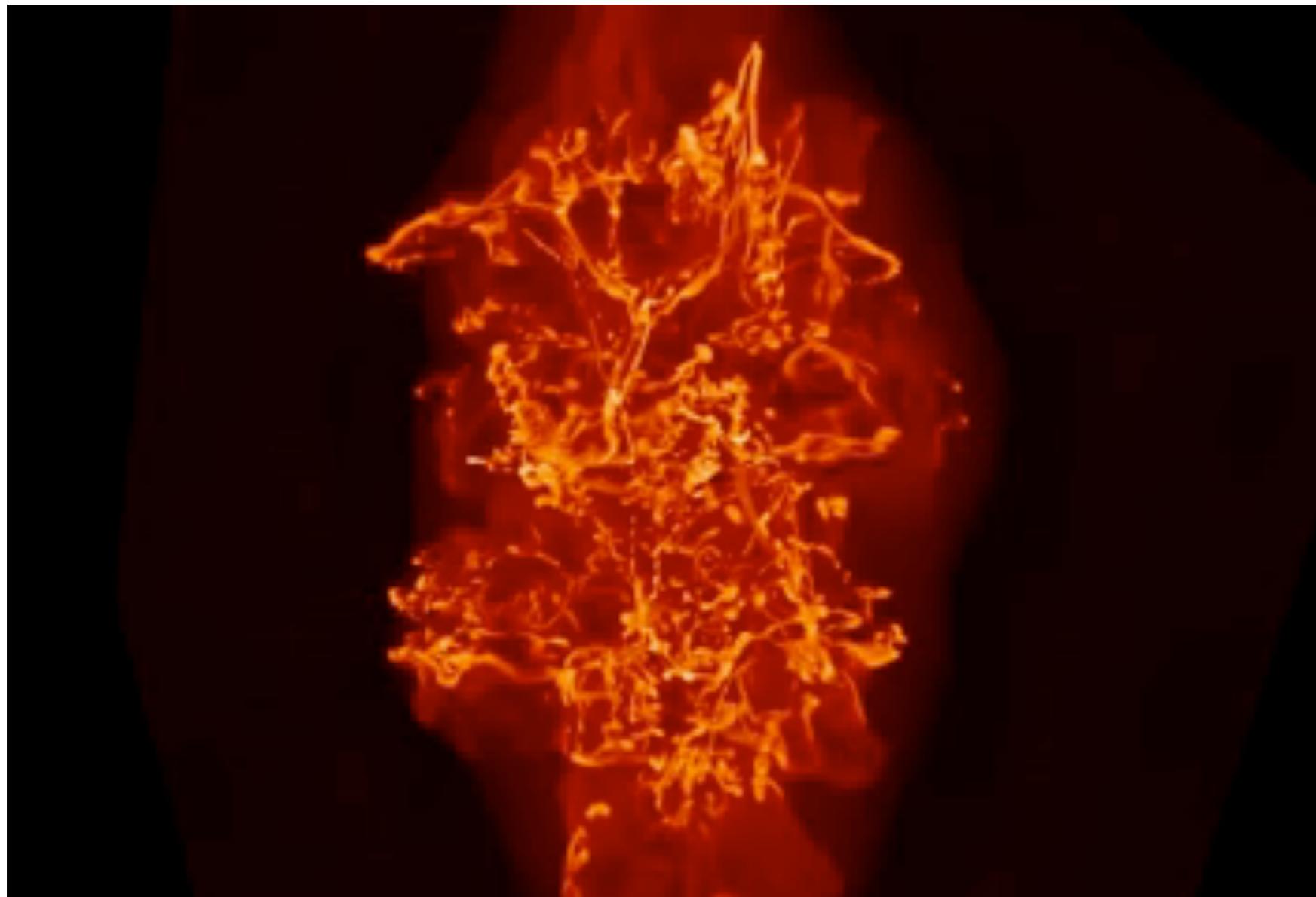
$$\dot{e} = \frac{1}{2} \xi_{\text{jet}} f_{\text{jet}} \frac{\dot{M}_{\text{SF}} v_{\text{jet}}^2}{\pi R^2 H} = \frac{1}{2} f_{\text{jet}} \frac{\dot{M}_{\text{SF}} v_{\text{jet}} \sigma}{\pi R^2 H}$$
$$= 1.4 \times 10^{-28} \text{ erg cm}^{-3} \text{ s}^{-1} \times$$
$$\times \left( \frac{f_{\text{jet}}}{0.2} \right) \left( \frac{\dot{M}_{\text{SF}}}{3 M_{\odot} \text{ yr}^{-1}} \right) \left( \frac{v_{\text{jet}}}{200 \text{ km s}^{-1}} \right) \left( \frac{\sigma}{10 \text{ km s}^{-1}} \right) \left( \frac{H}{100 \text{ pc}} \right)^{-1} \left( \frac{R}{15 \text{ kpc}} \right)^{-2}$$

✓ stellar winds? Radiation? Continuous processes, integrated effect would more likely affect the collapsing cloud dynamics

# Molecular cloud formation

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- Colliding flows

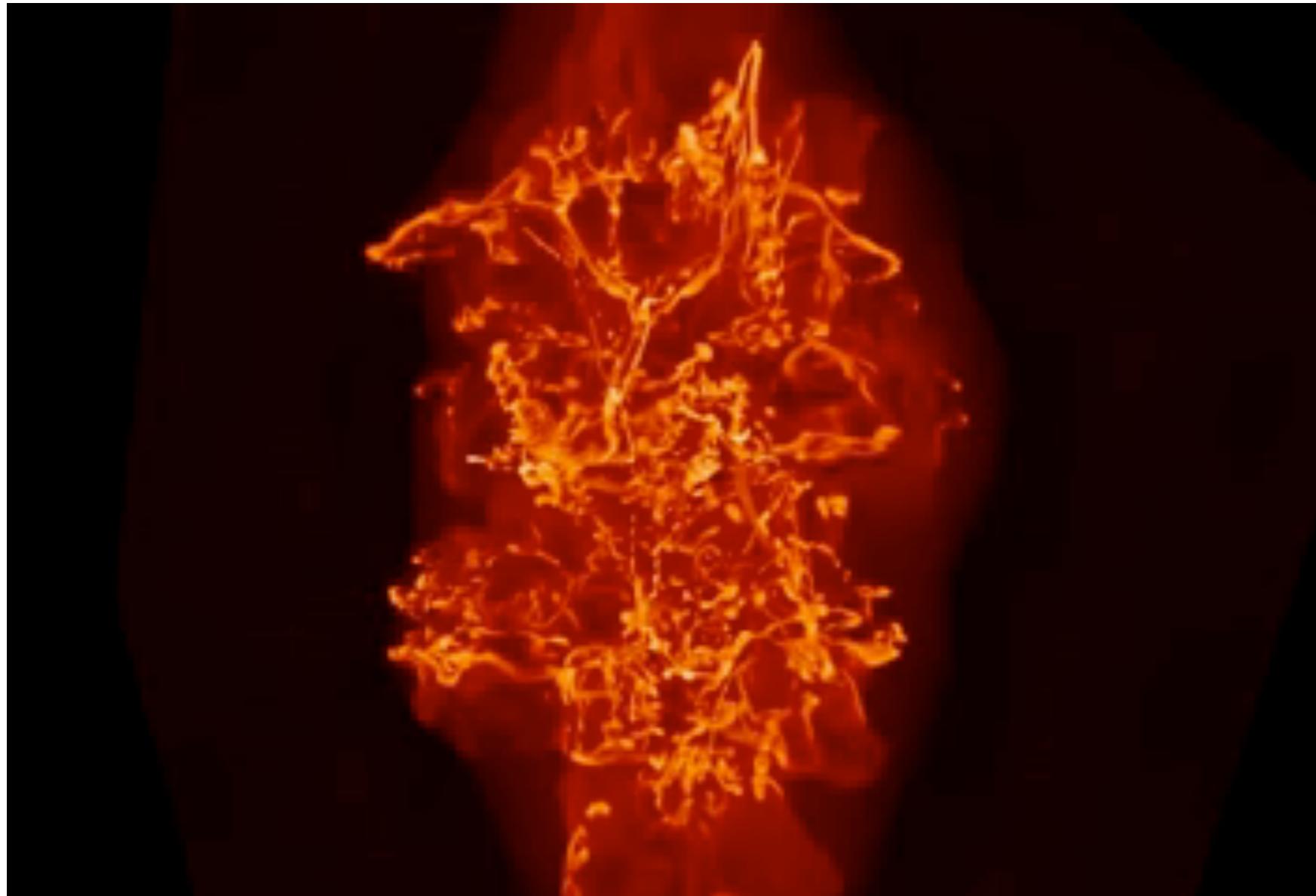


Simulation by  
Audit & Hennebelle

# Molecular cloud formation

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- Colliding flows

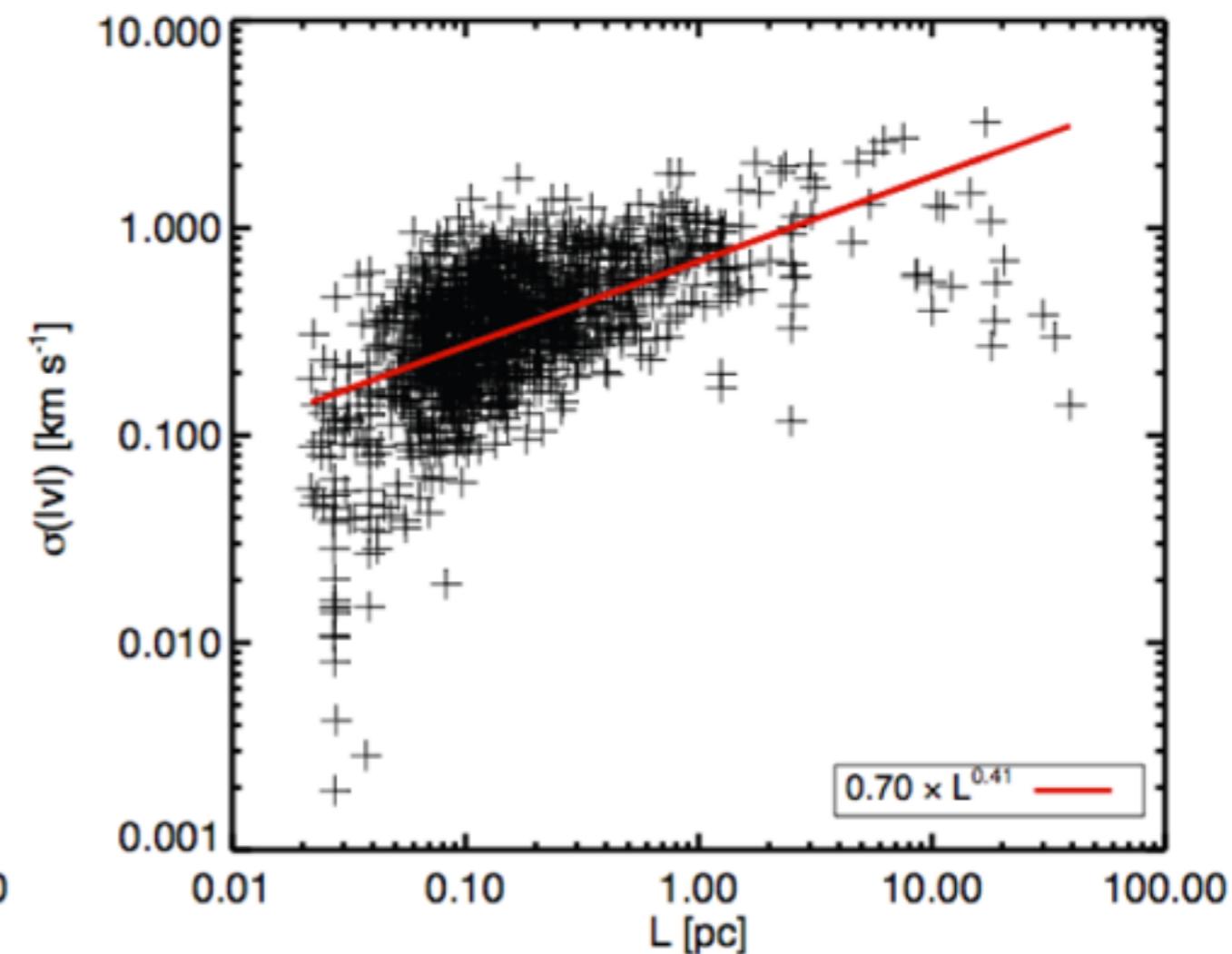
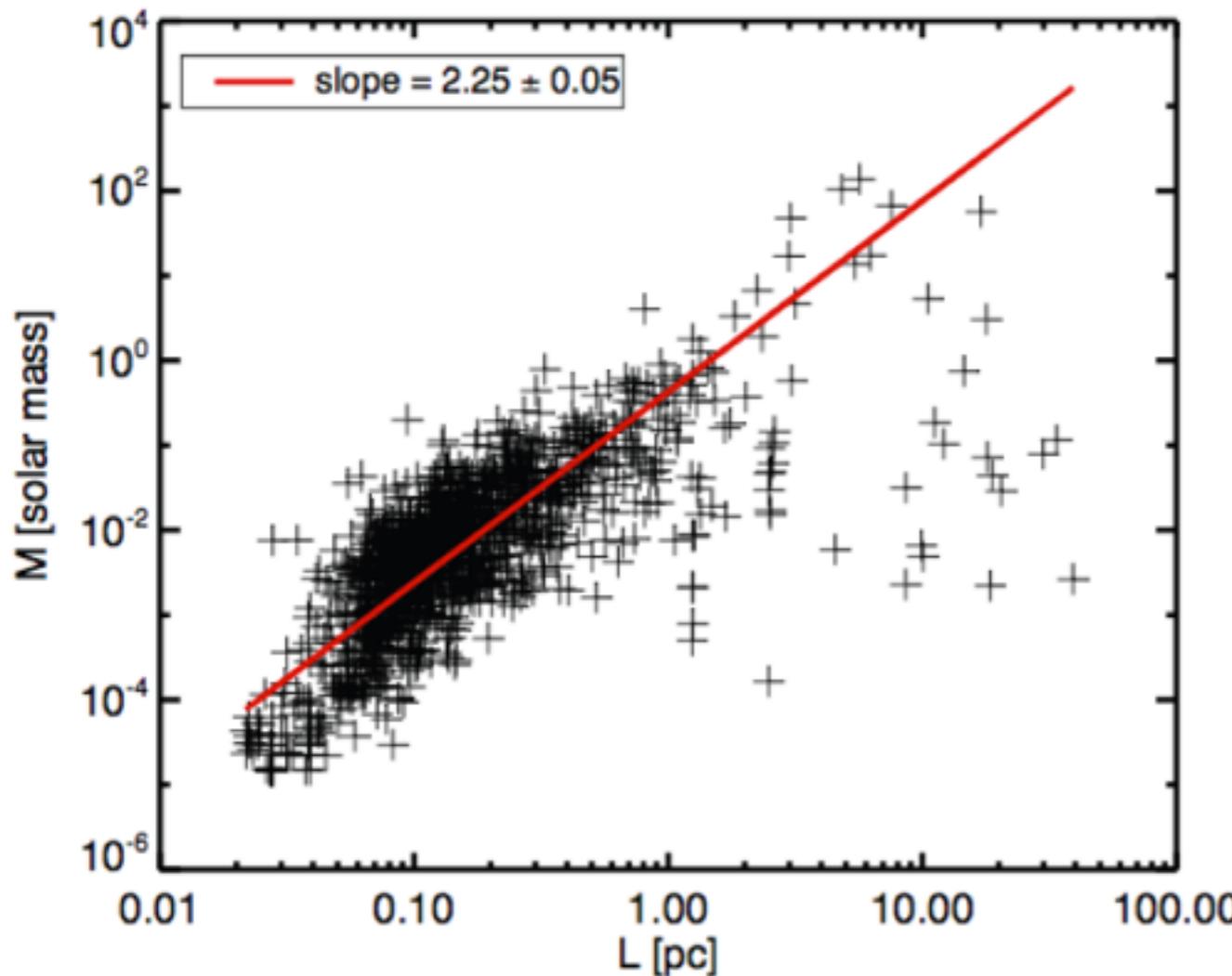


Simulation by  
Audit & Hennebelle

# Molecular cloud evolution

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- Colliding flows



+ mass spectrum similar to the one observed for CO clumps

Saury et al. (2014)

# Formation of self-gravitating cores

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- We now consider individual molecular clouds with:
  - gravity
  - turbulence
  - magnetic field
- Formation of gravitationally bound structures:
  - Virial analysis, with only thermal support to balance gravity

$$2\mathcal{T} + \Omega = 0$$

$$M_{\text{crit}} \propto \frac{C_s^3}{\sqrt{n}}$$

# Formation of self-gravitating cores

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- We now consider individual molecular clouds with:
  - gravity
  - turbulence
  - magnetic field
- Formation of gravitationally bound structures:
  - Virial analysis, with only thermal support

$$M_{\text{crit}} \sim 1.9 \left( \frac{T}{10 \text{ K}} \right)^{3/2} \left( \frac{n}{10^4 \text{ cm}^{-3}} \right)^{-1/2} M_{\odot}$$

# Formation of self-gravitating cores

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- **Turbulence**

- fluctuations at small scales compared to the Jeans scale

$$C_{\text{s,eff}}^2 \simeq C_{\text{s}}^2 + V_{\text{rms}}^2 / 3$$

- **Formation of gravitationally bound structures**

$$M_{\text{crit}} \propto \frac{C_{\text{s,eff}}^3}{\sqrt{n}}$$

- **Gravo-turbulent model** (*Hennebelle & Chabrier, Padoan & Nordlund*)

# Formation of self-gravitating cores

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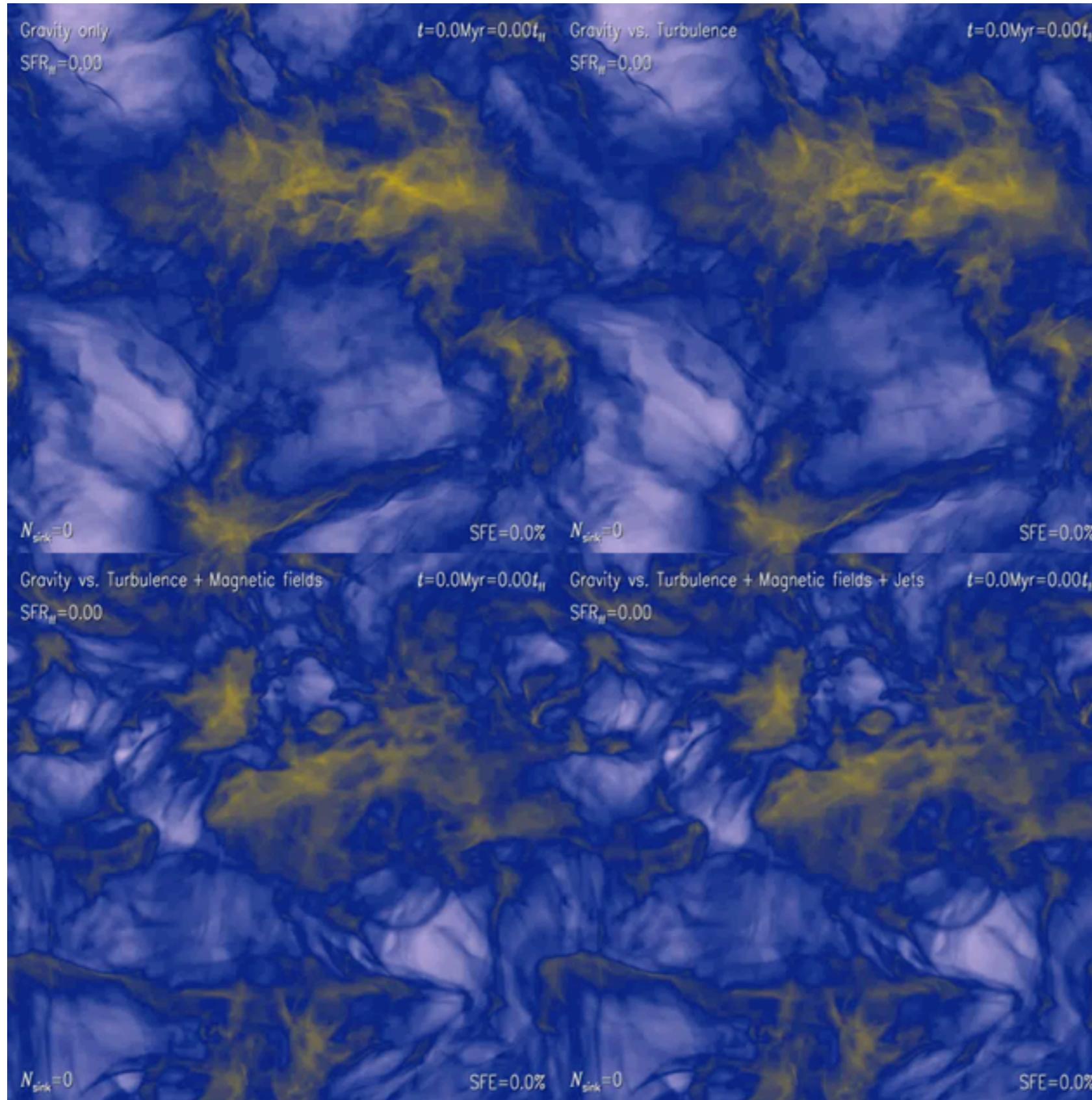
- Stability in presence of a magnetic field

$$2\mathcal{T} - 4\pi R^3 P_{\text{ext}} - \frac{1}{R} \left( \frac{3}{5} GM^2 - \frac{1}{3} R^4 B^2 \right) = 0$$

- Critical mass  $M_c \sim \left( \frac{5}{9G} \right)^{1/2} \phi_B$
- $M > M_c$ : “magnetically supercritical” cloud
- Magnetic fields “dilute” gravity:

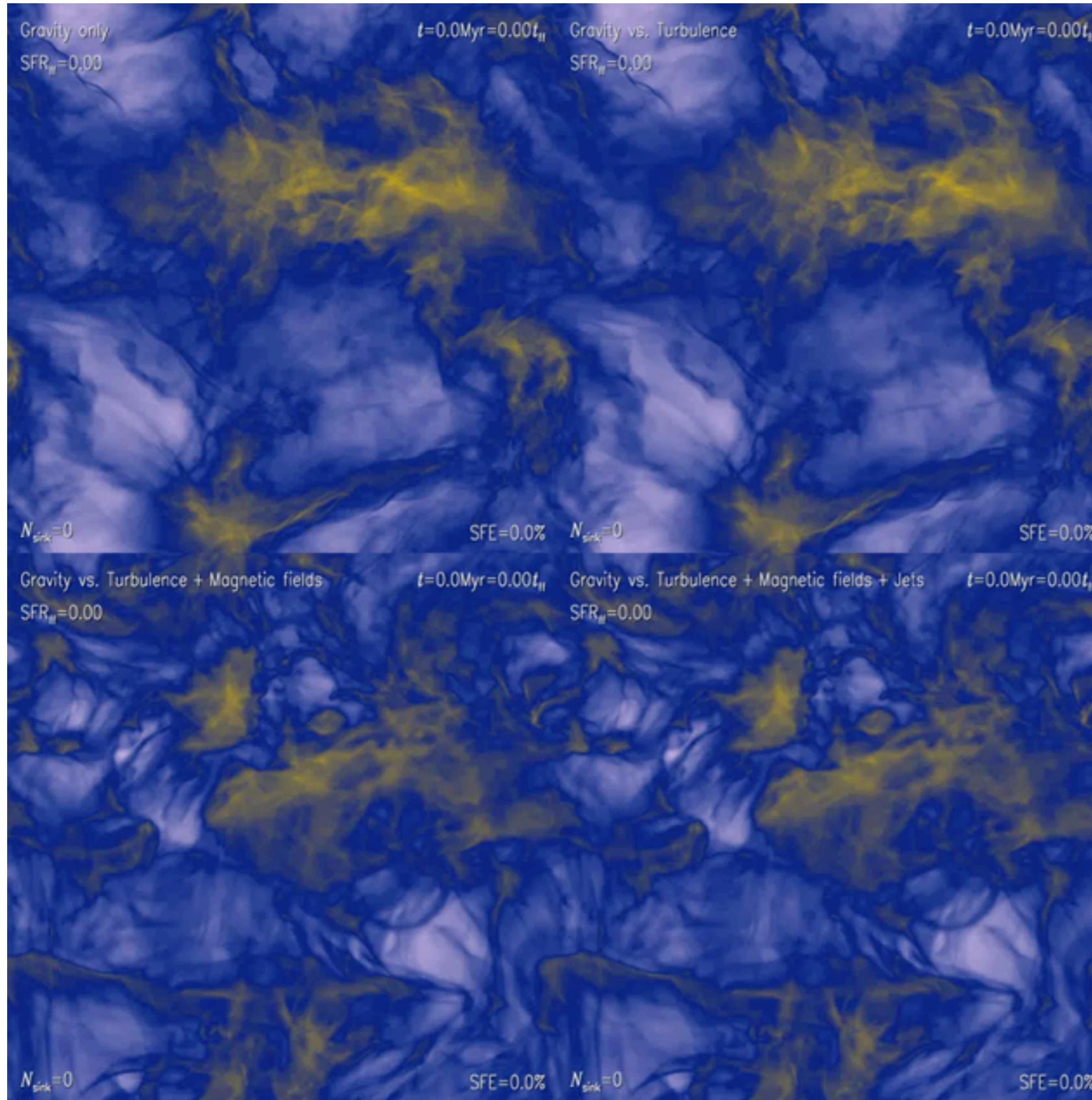
$$2(E_{\text{th}} + E_{\text{kin}}) + E_{\text{grav}}(1 - \mu^{-2})$$

# Molecular cloud evolution & dense core formation



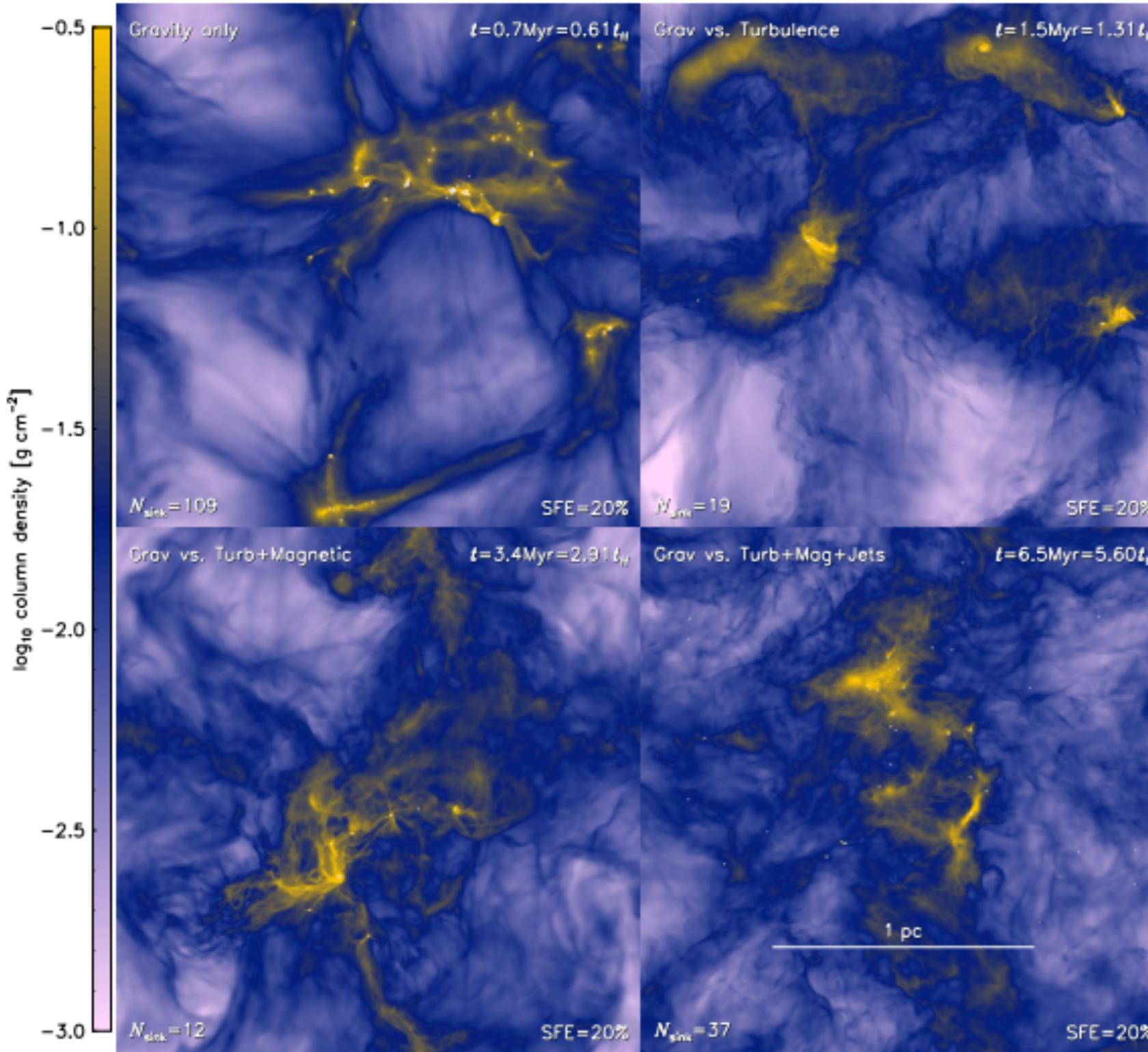
Federrath (2015)

# Molecular cloud evolution & dense core formation



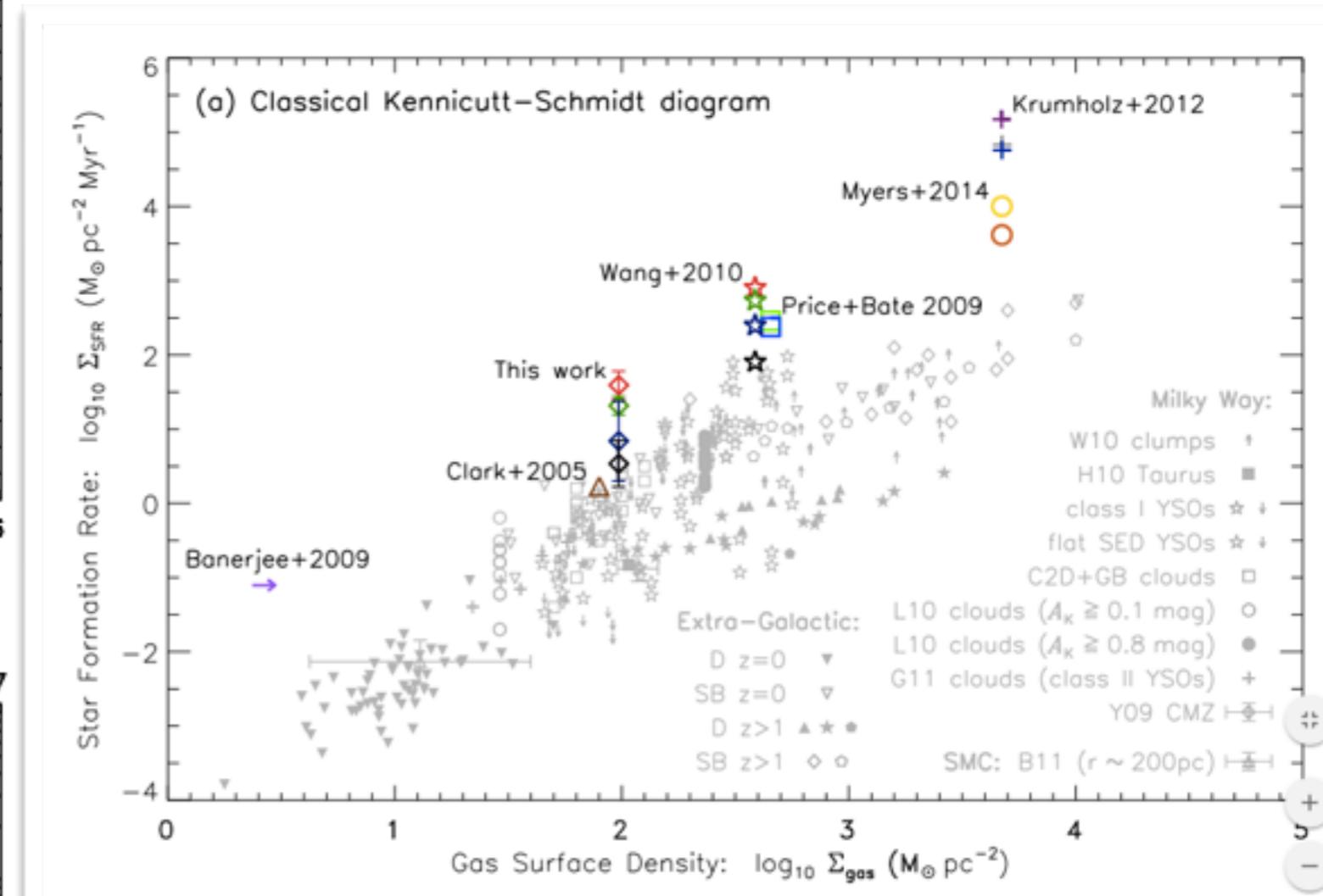
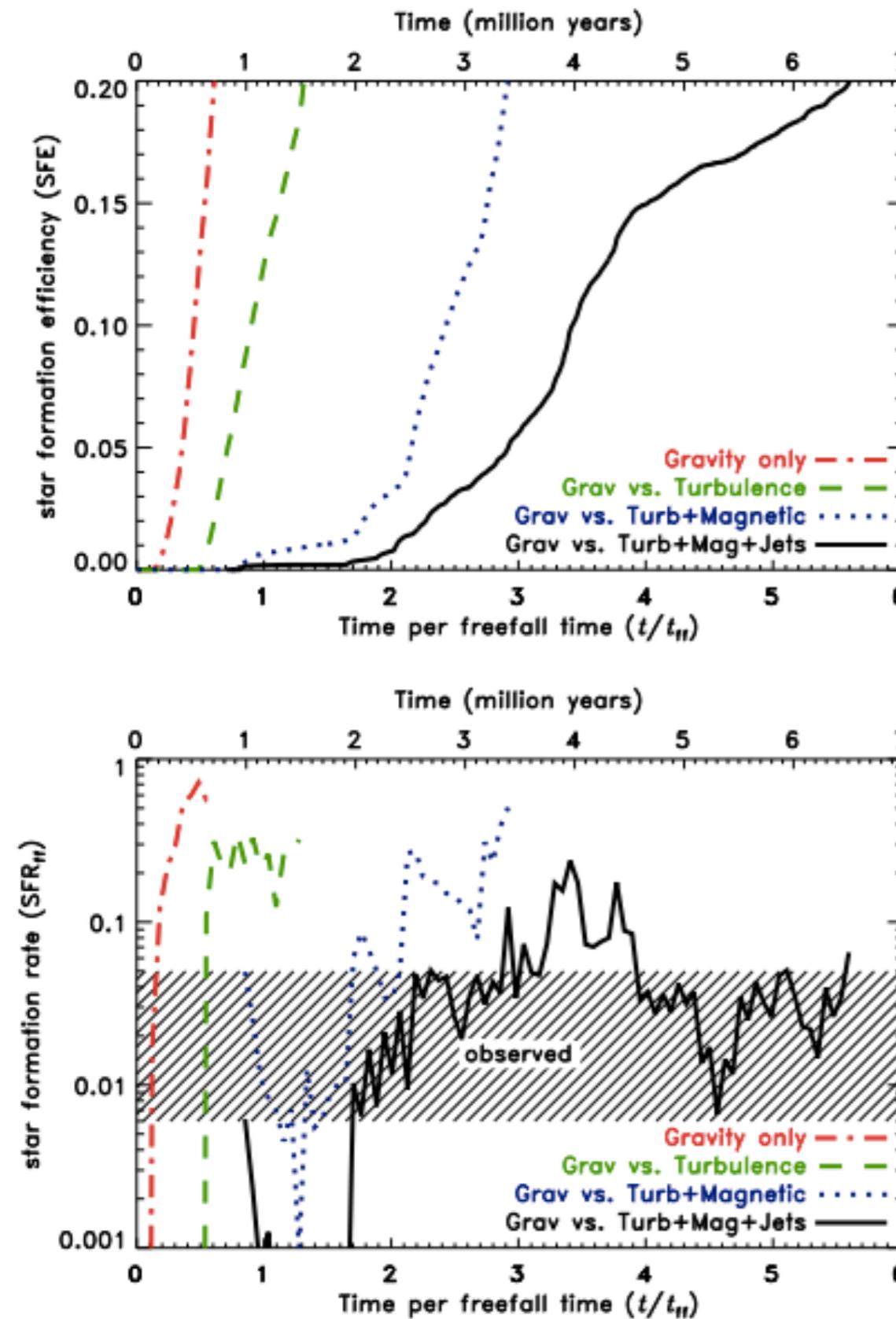
Federrath (2015)

# Molecular cloud evolution & dense core formation



Federrath (2015)

# Molecular cloud evolution & dense core formation



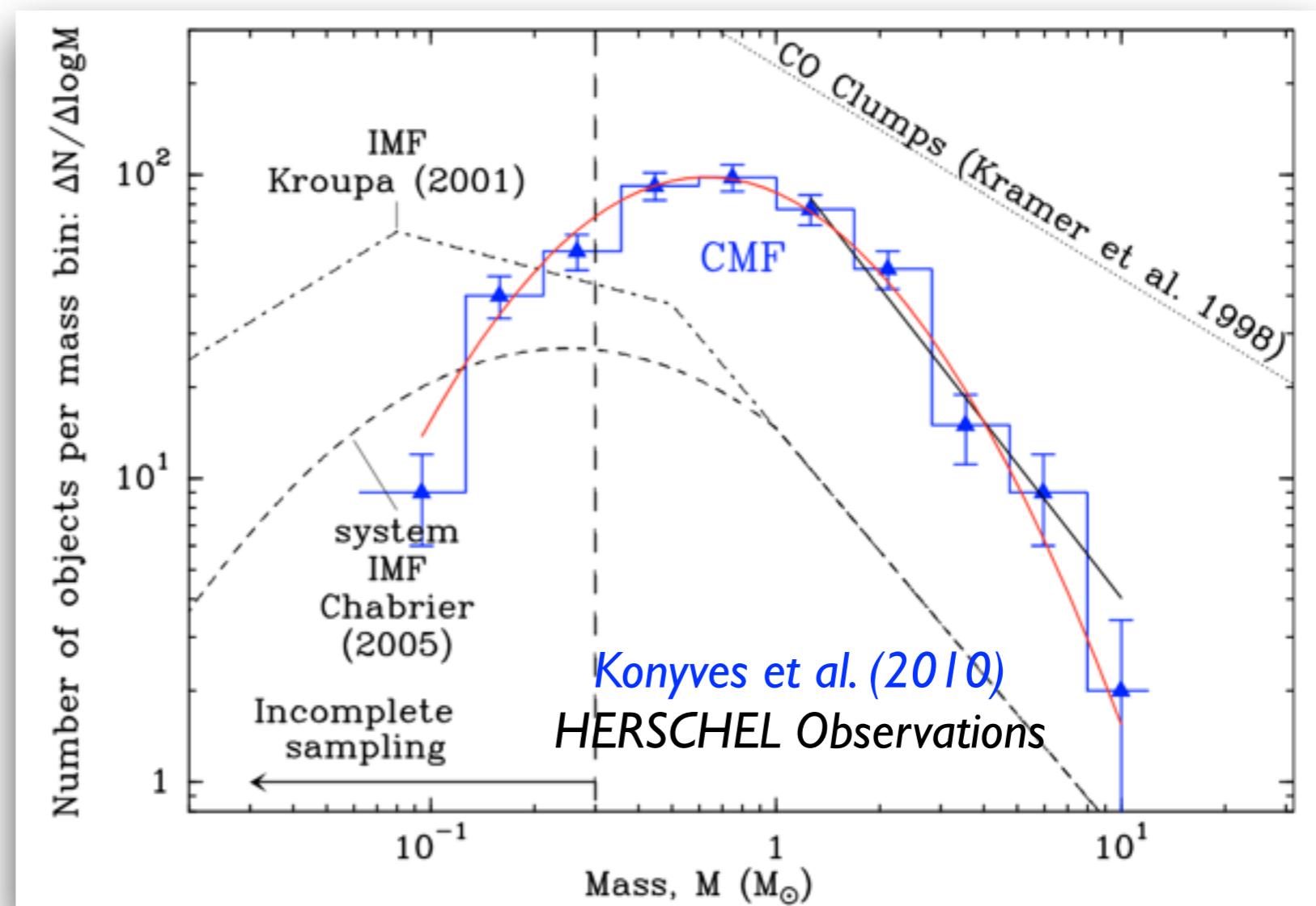
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# Dense core formation

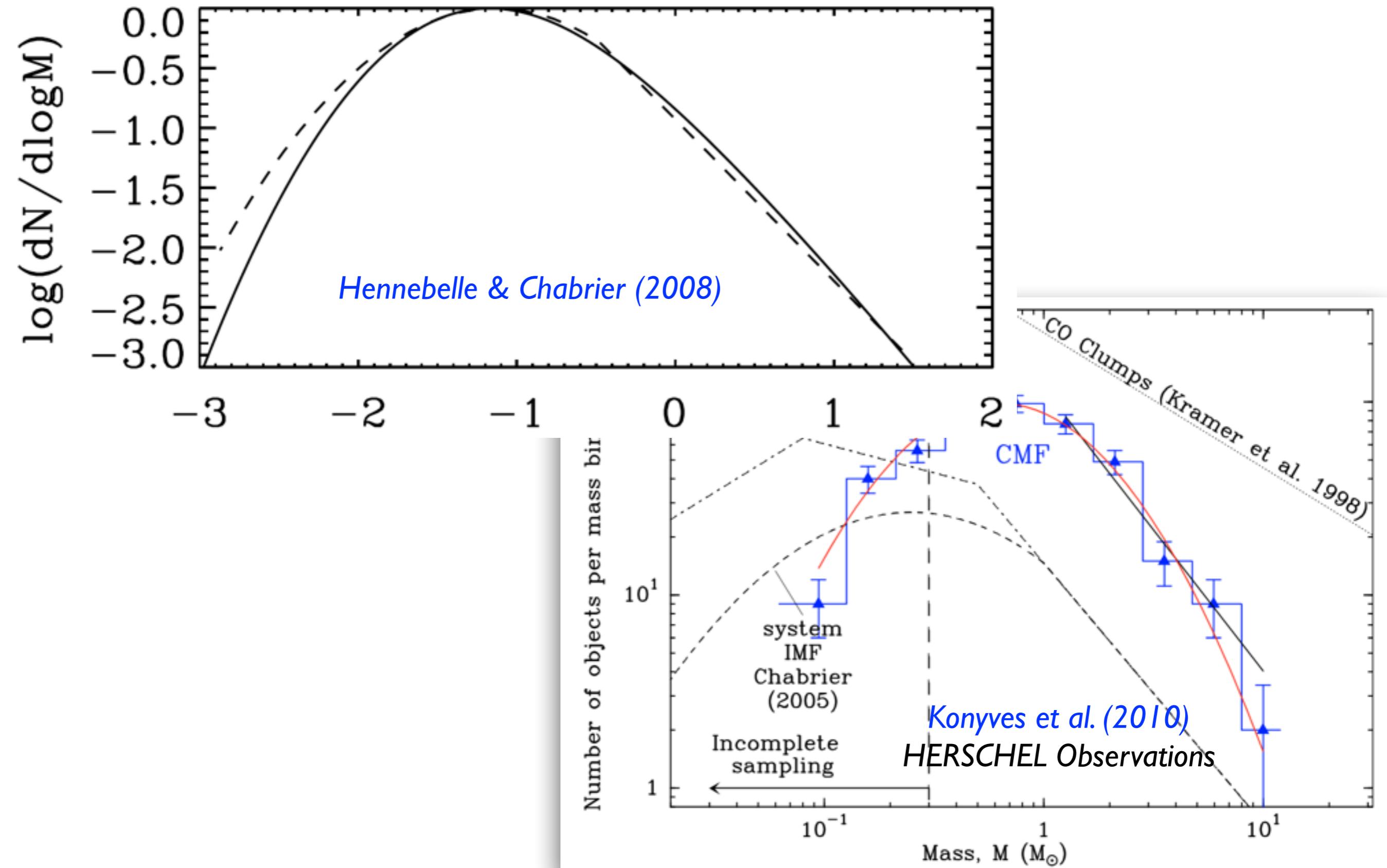
- At the sonic scale for the majority
- Dense core are the progenitors of stars
- I-I relation between core mass function and initial stellar mass function?
- Analytical description (e.g., [Hennebelle & Chabrier](#))



Barnard 68



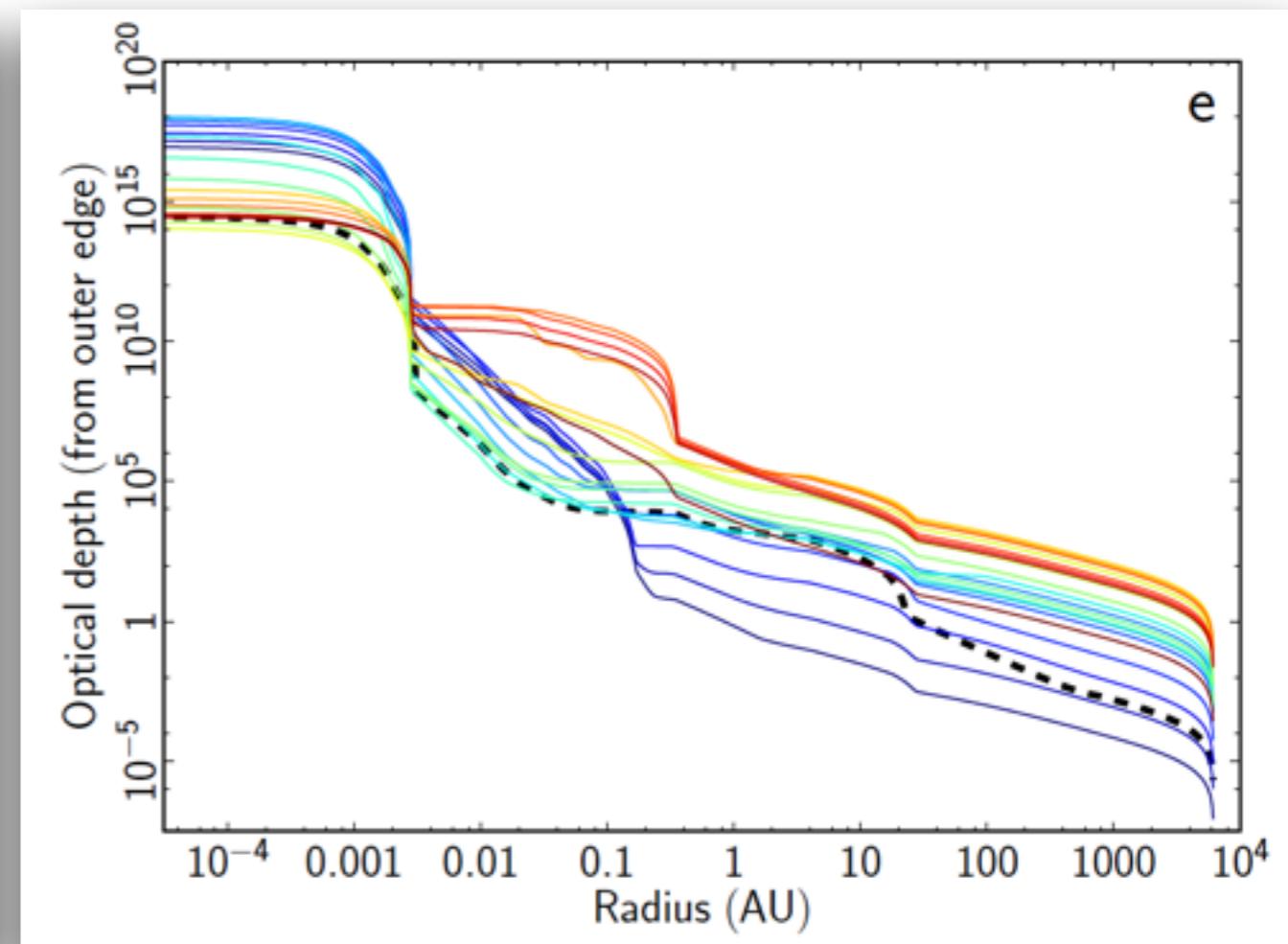
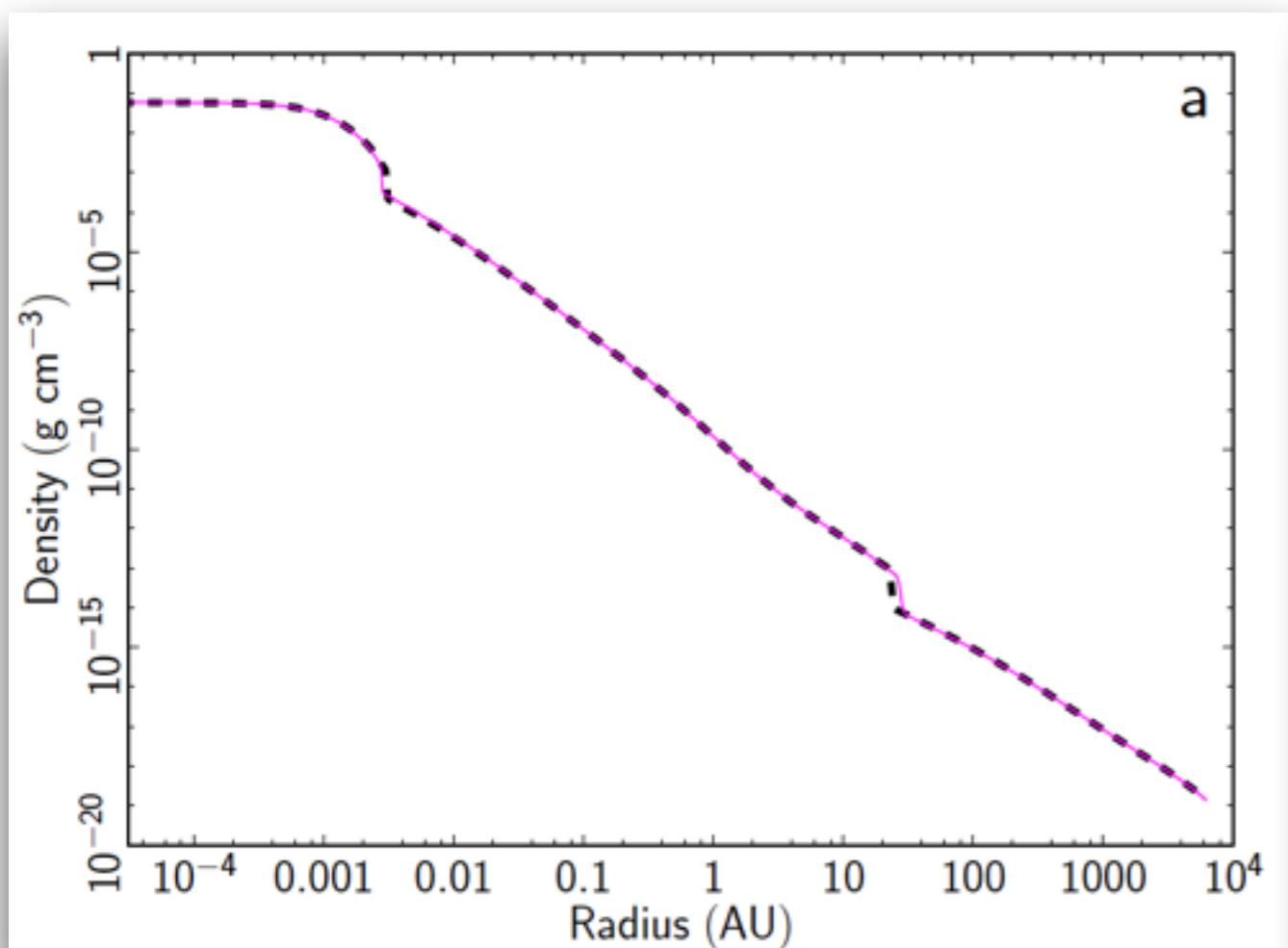
# Dense core formation



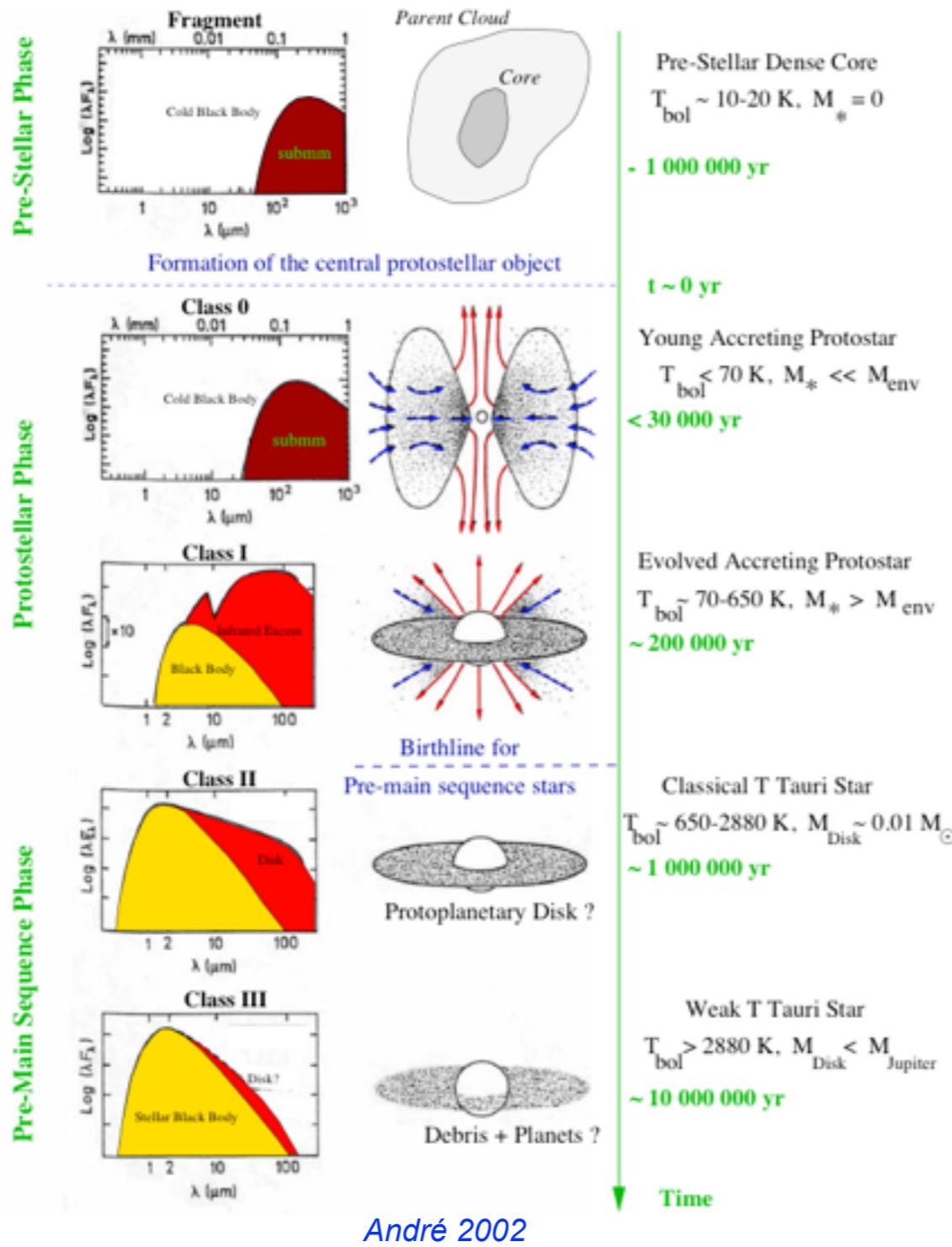
# Dense core collapse: the challenge

✓ Follow the dynamics over a wide range of physical scales:

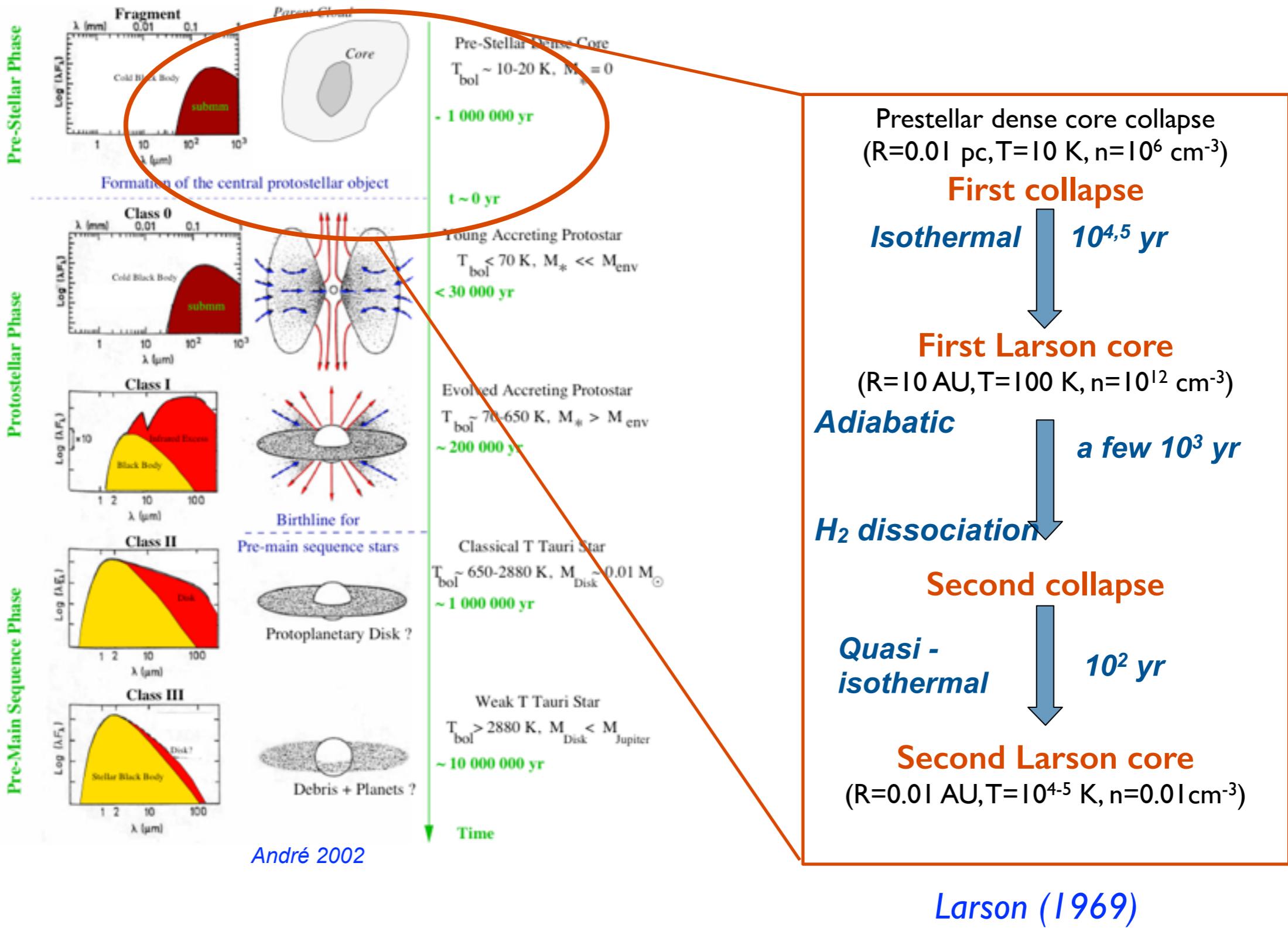
- **time** scales: free-fall time ( $\sim 10^{4,5}$  yr) to second
- **spatial** scales: parsec to stellar radius
- **physical** scales: density ranges from  $1 \text{ cm}^{-3}$  to  $10^{24} \text{ cm}^{-3}$



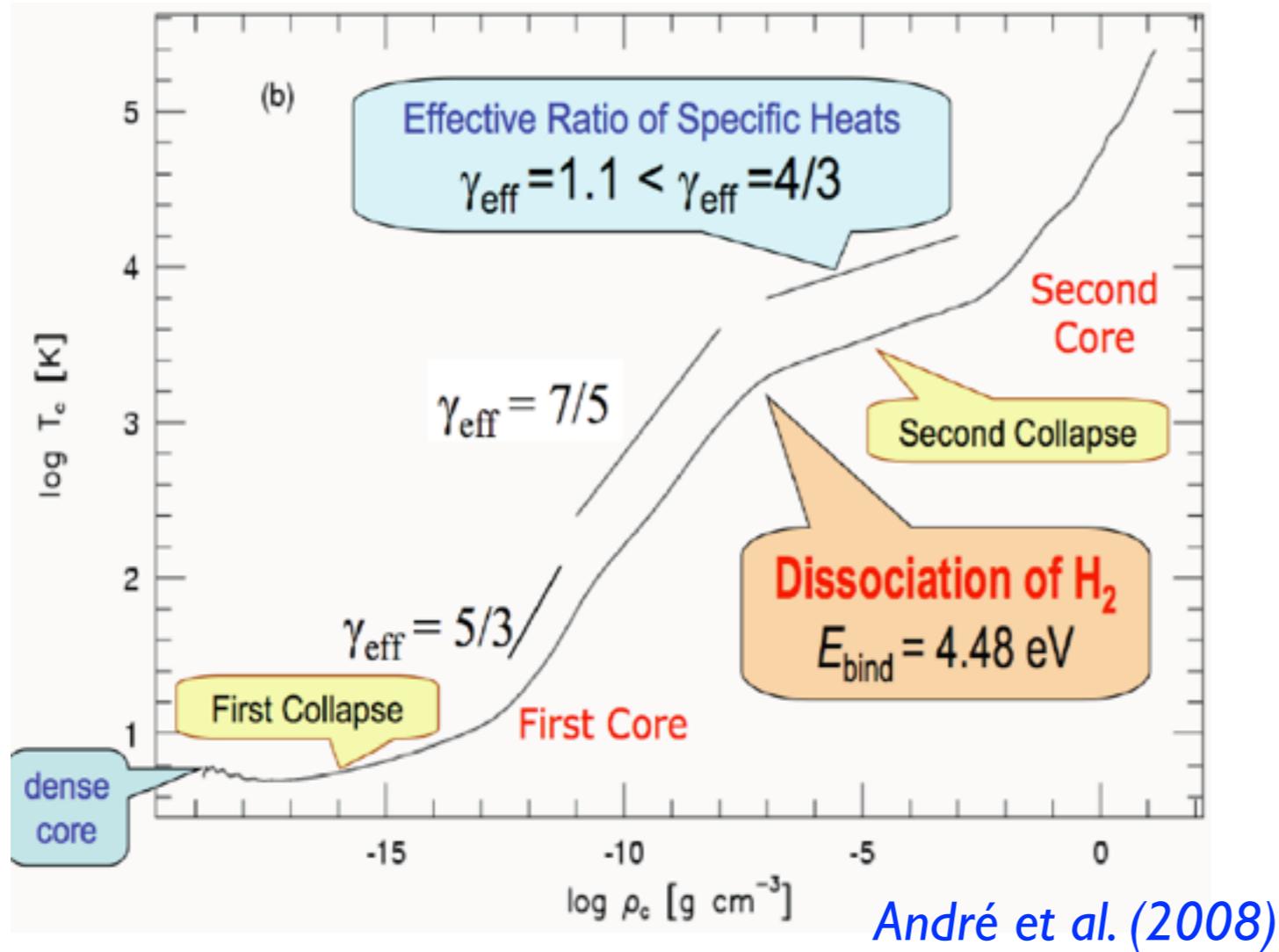
# Star formation evolutionary sequence



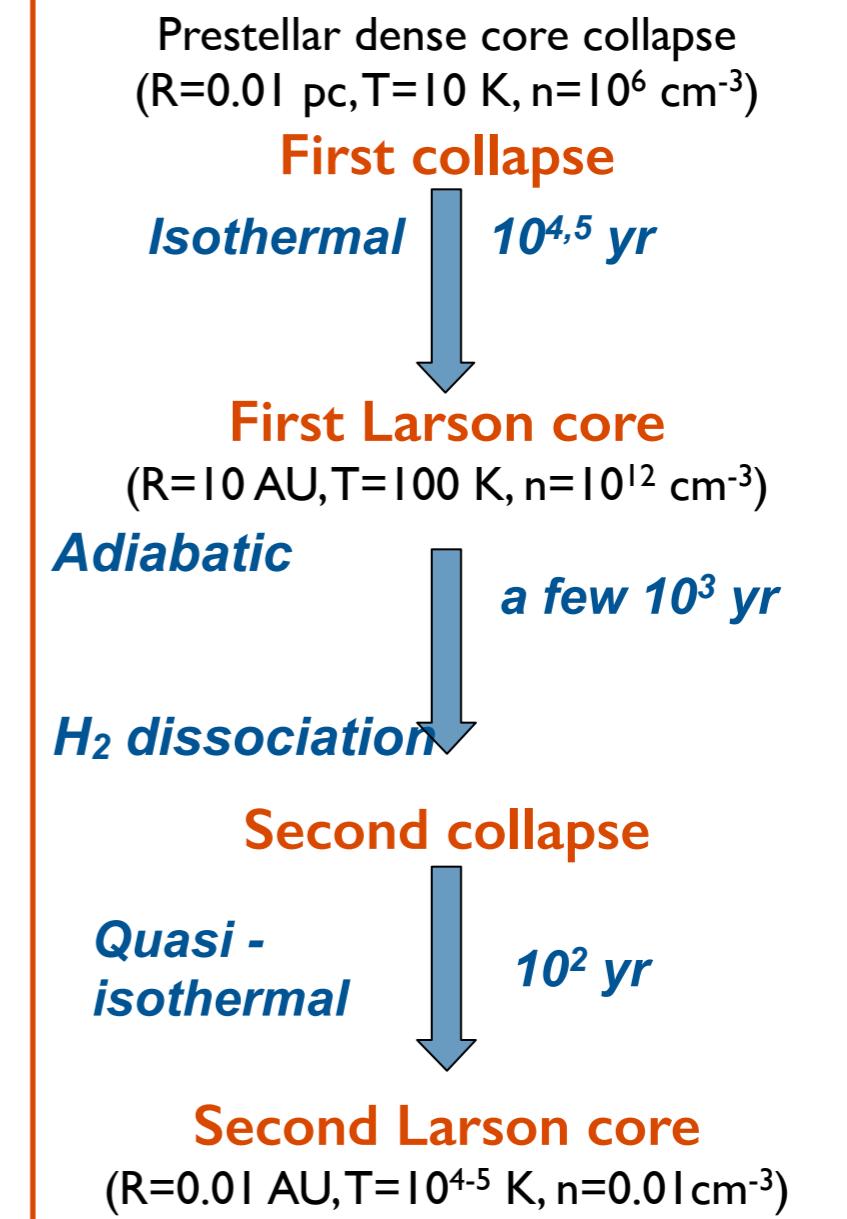
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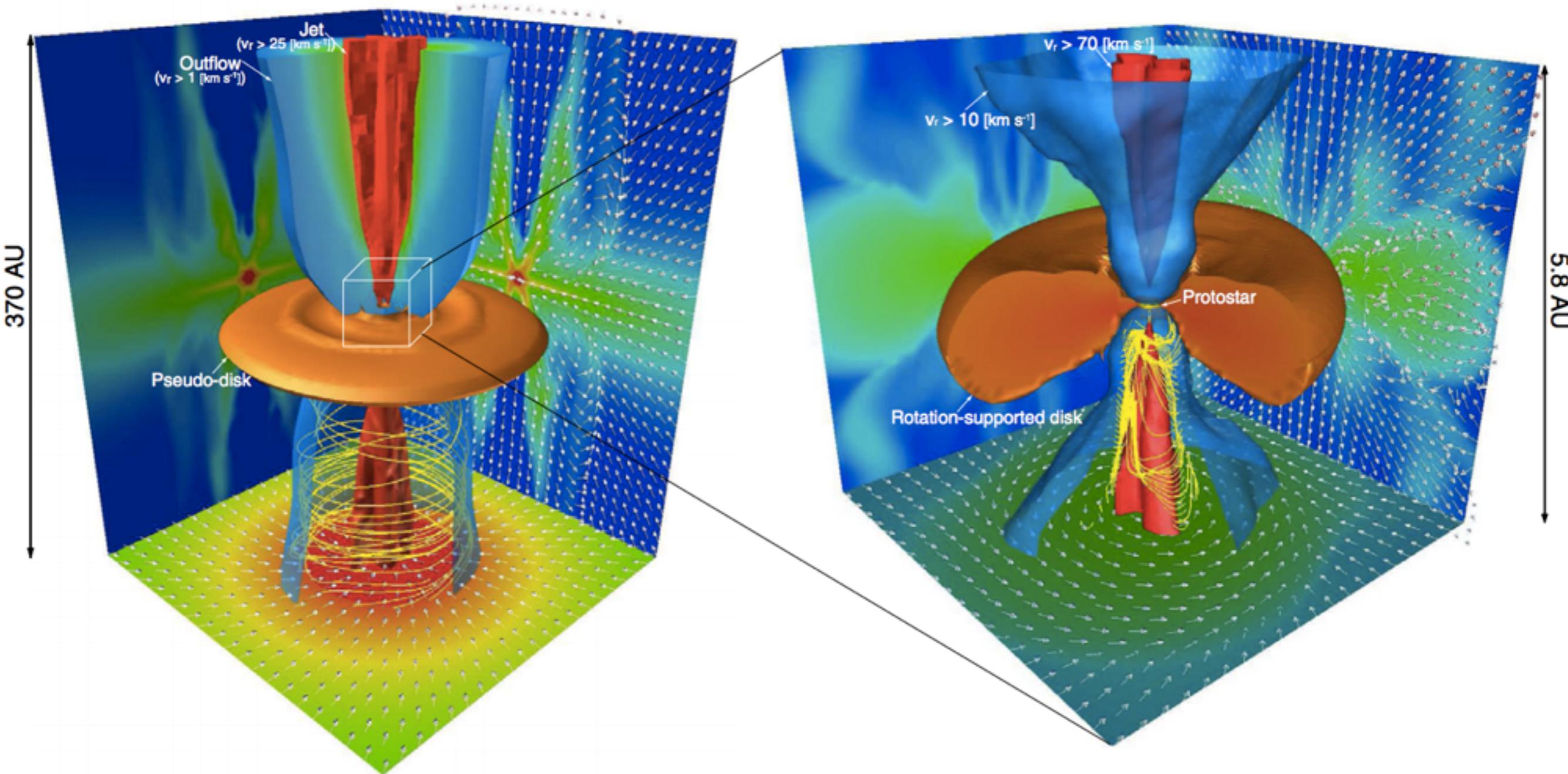
# Star formation evolutionary sequence



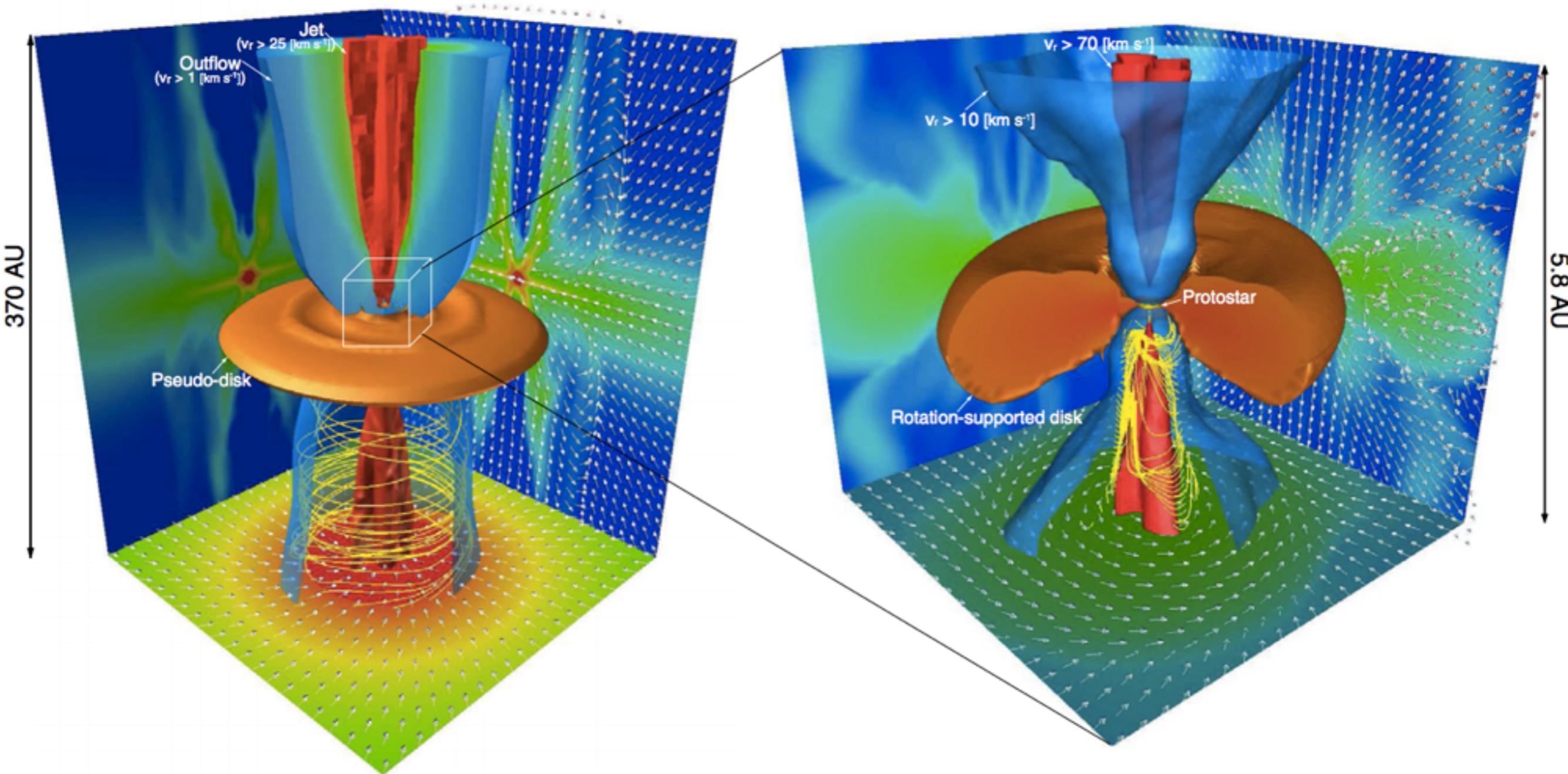
$$M_{\text{Jeans}} \propto \rho^{\frac{3}{2}} n^{-2}$$



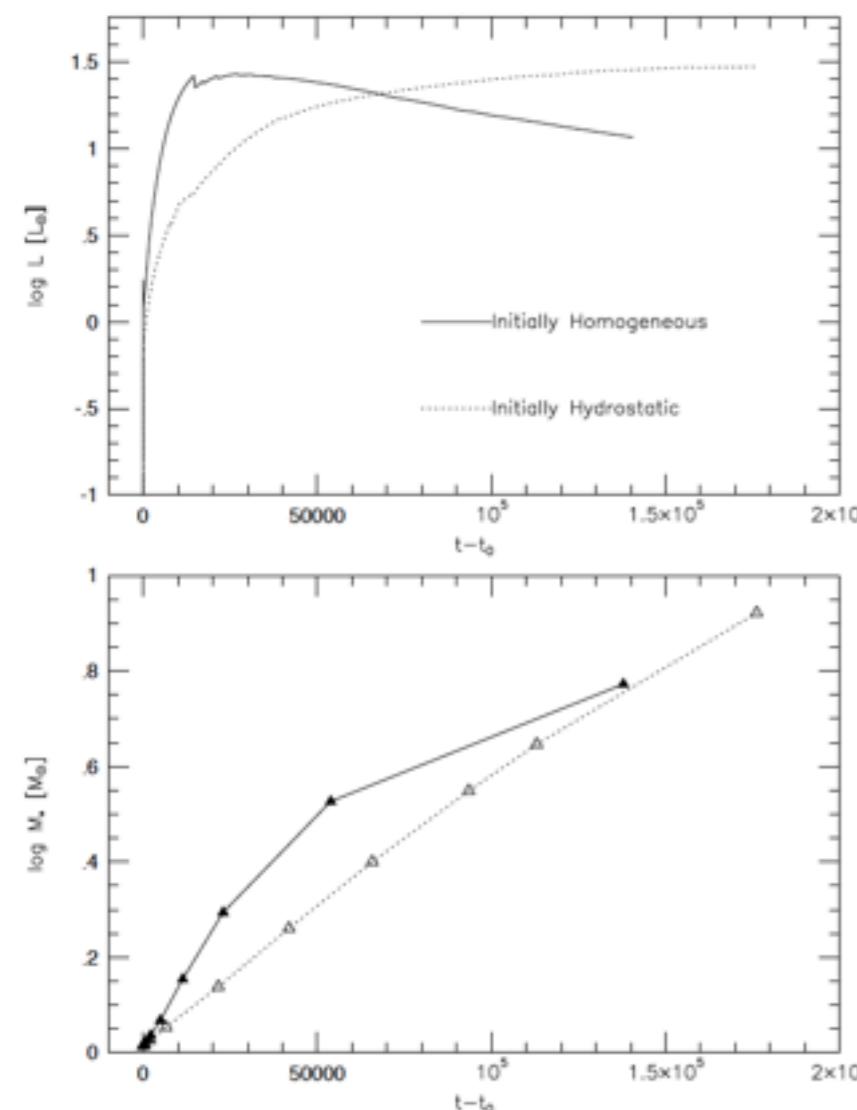
# Protostellar core



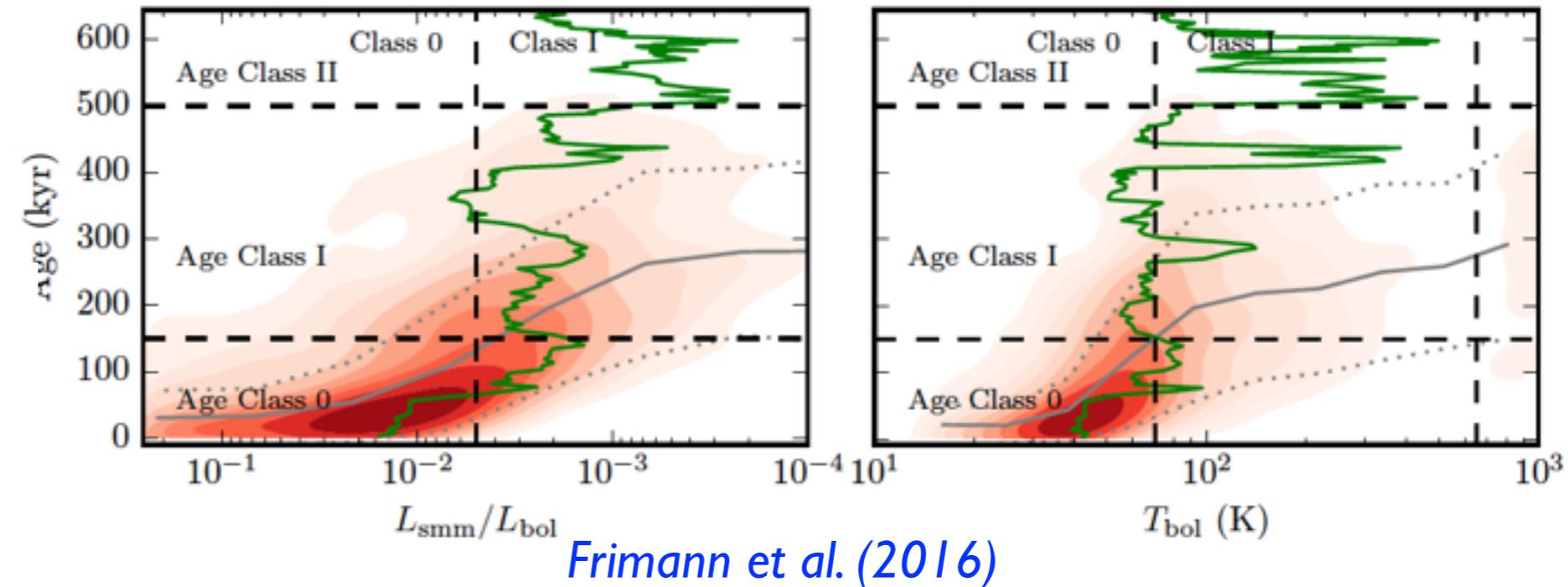
# Protostellar core



# Luminosity and other evolution tracers



Masunaga et al. (2000)



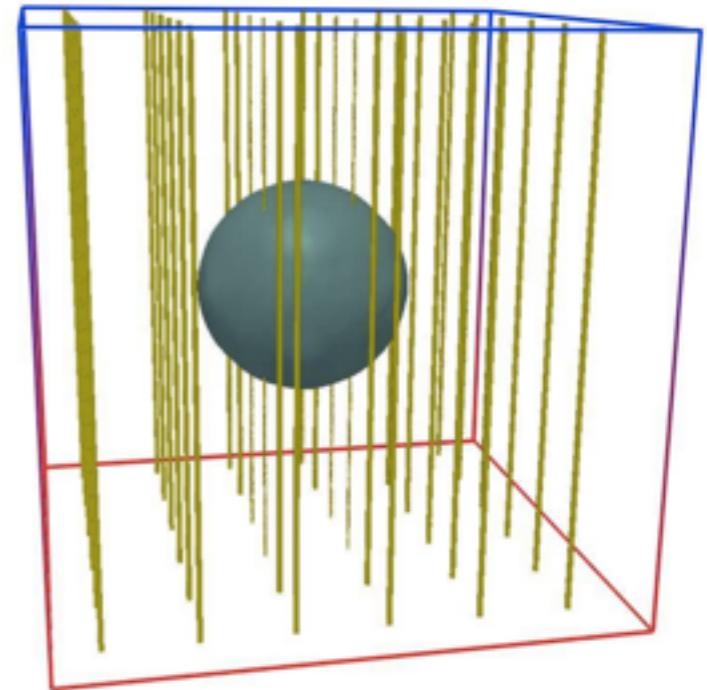
Frimann et al. (2016)

- models match well the distributions of observed tracers
- but... observed quantities do not trace well protostellar ages
- needs more quantitative analysis and models integrating more physics.

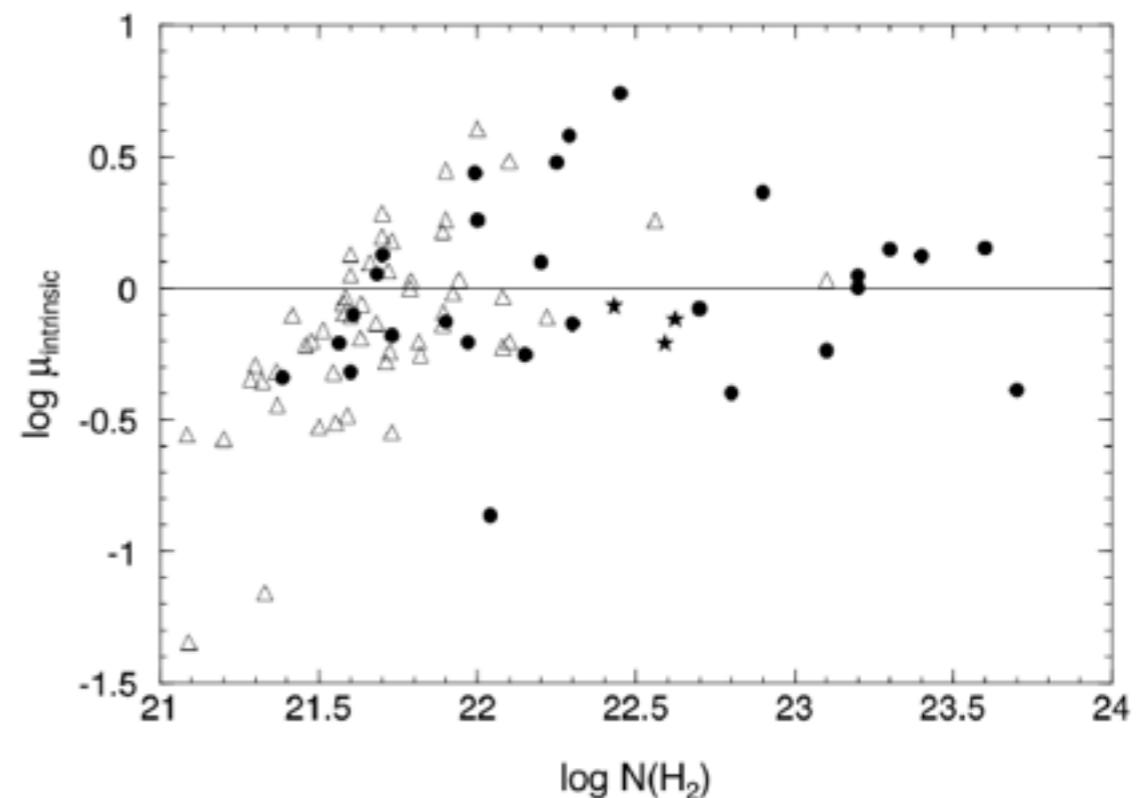
# Numerical experiments

## Typical initial conditions:

- $1 M_{\odot}$  isolated dense core
  - uniform / BE-like density profile
  - uniform temperature (10 K,  $\alpha = E_{\text{th}}/E_{\text{grav}}$ )
  - solid body / differential rotation ( $\beta = E_{\text{rot}}/E_{\text{grav}}$ )
  - $m=2$  density perturbation / turbulent velocity field
  - organised magnetic field
- $\mu = (\varphi/M)_{\text{crit}} / (\varphi/M)$  (observations  $\mu \sim 2-5$ )



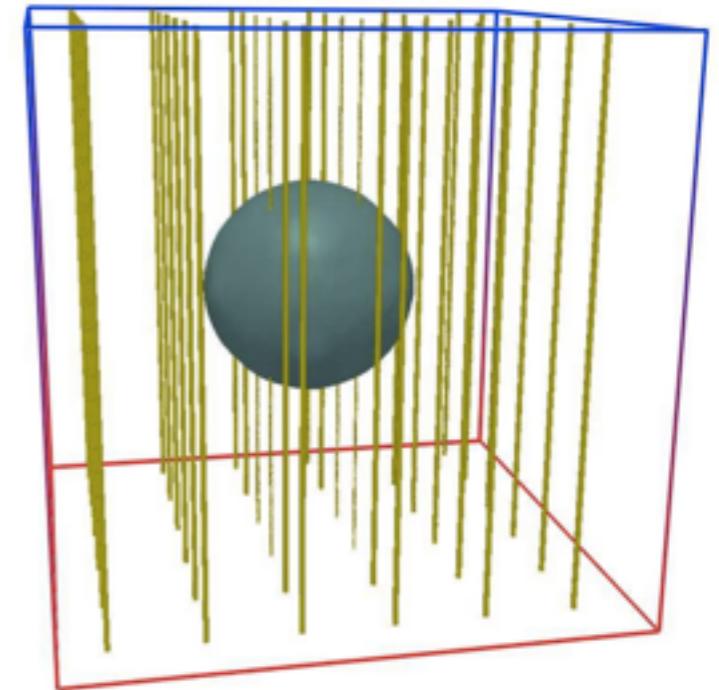
Refinement criterion solely based on  
the Jeans length



# Numerical experiments

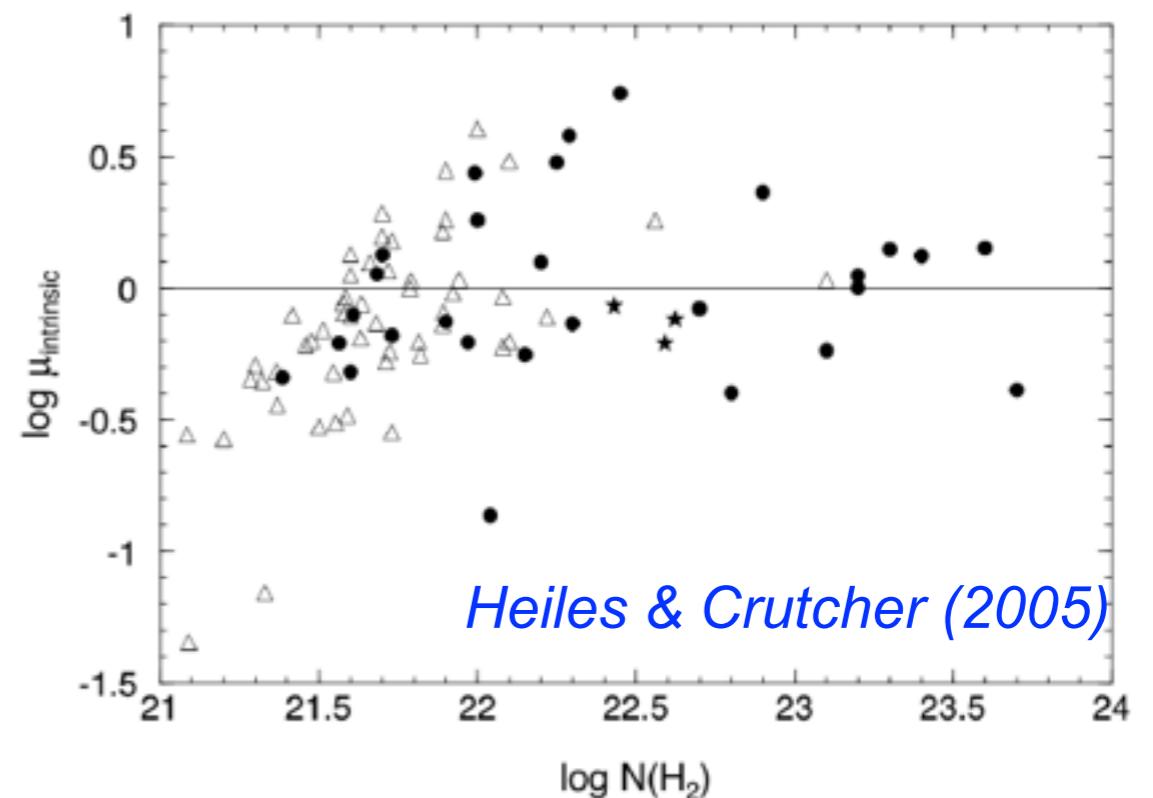
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Banerjee & Pudritz (2006)

Refinement criterion solely based on  
the Jeans length



# Numerics for star formation

## ★ 2 numerical methods :

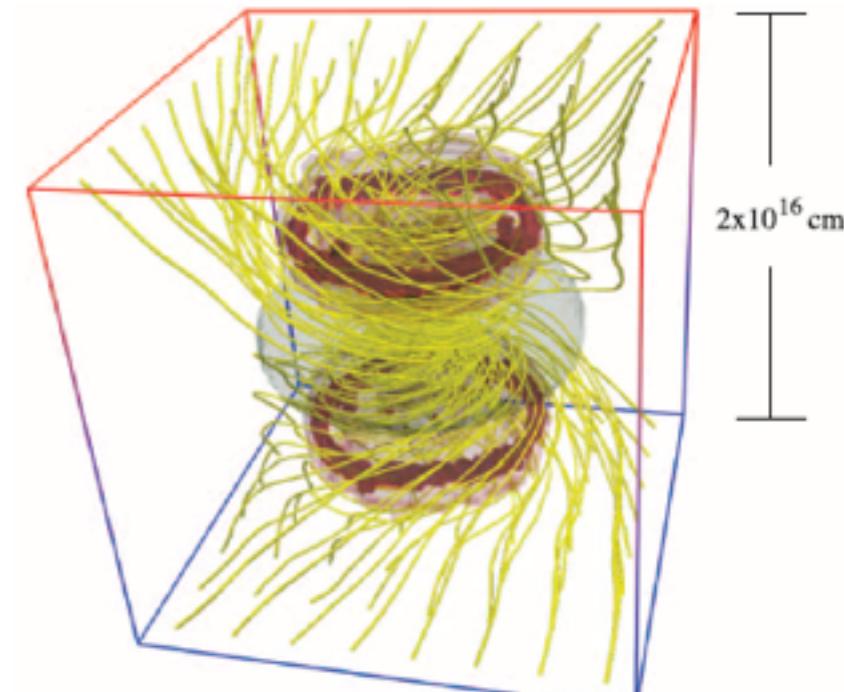
- **Grid based code (AMR)** : RAMSES code ([Teyssier 2002, Fromang et al. 2006, Commerçon et al. 2011a](#)), ORION code ([Krumholz et al.](#)) FLASH code ([Banerjee, Seifried et al.](#)), etc...

→ **Advantages :**

- ✓ accuracy
- ✓ shocks
- ✓ refinement criteria

→ **Disadvantages :**

- ✓ (headach)
- ✓ Eulerian



[Banerjee & Pudritz 06](#)

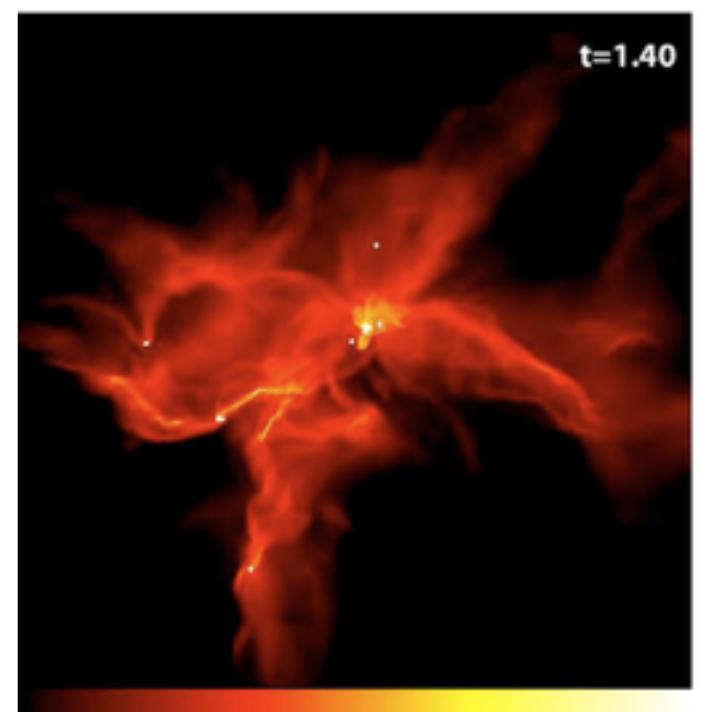
- **Lagrangian - SPH** : e.g. Bate & Price (RHD & MHD), Stamatellos et al. 2008 (RHD), etc...

→ **Advantages :**

- ✓ Lagrangian
- ✓ naturally adaptive
- ✓ (simpler)

→ **Disadvantages :**

- ✓ low density = low resolution
- ✓ noise, dissipative
- ✓ young



[Bate et al. 08](#)

# Numerical resolution criteria for SF

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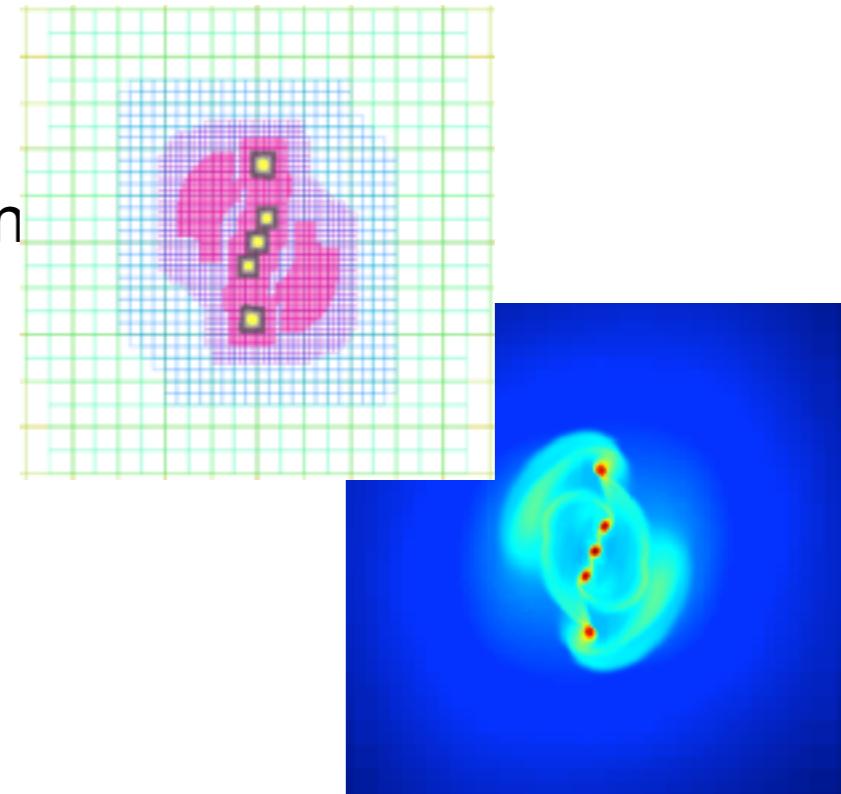
★ Gravitational instability → **Jeans** length

**AMR** : Refinement criteria  $N_J$  as a function of the local Jean

$$N_J \cdot \Delta x < \lambda_{\text{Jeans}}$$

↳ Truelove et al. 1997:  $N_J \geq 4$

↳ **Dynamical** criterion



# Numerical resolution criteria for SF

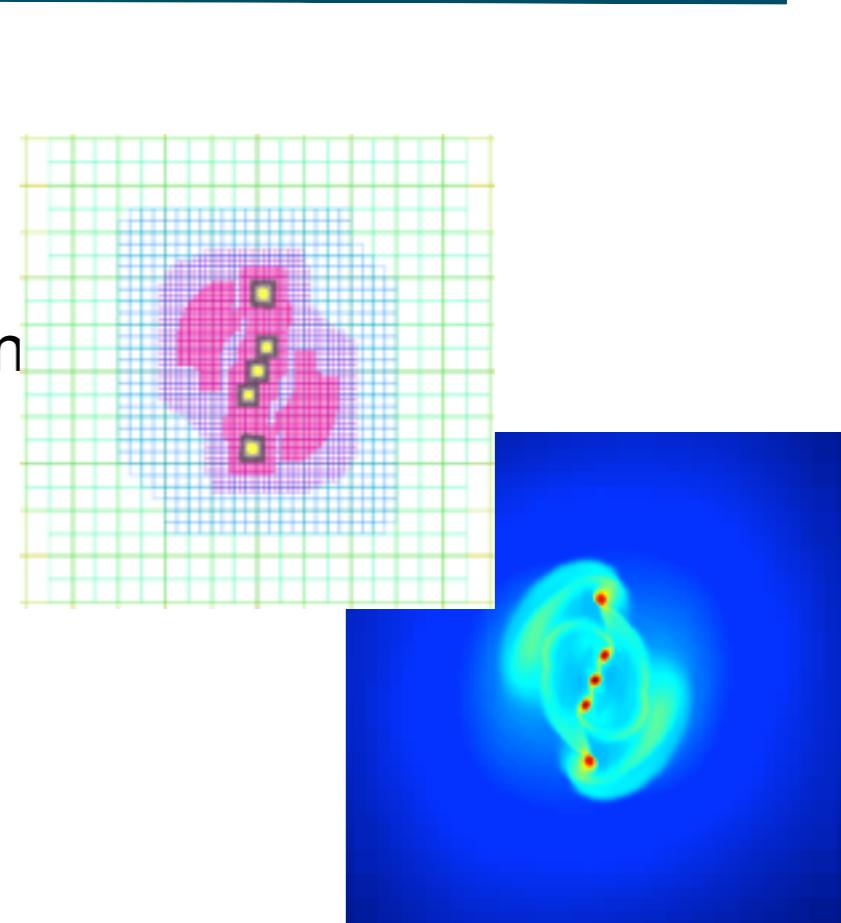
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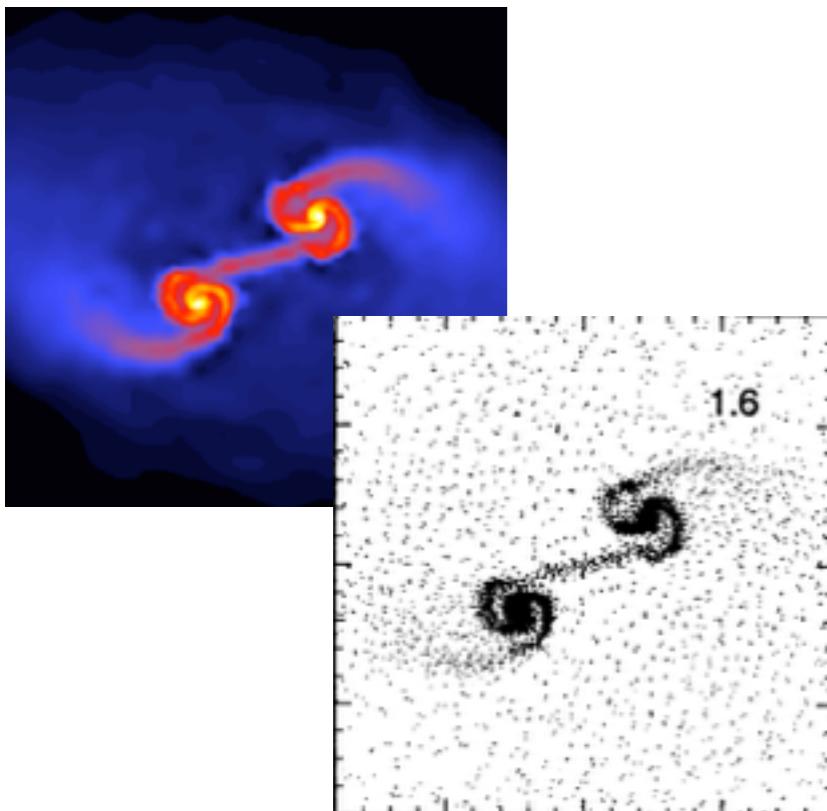
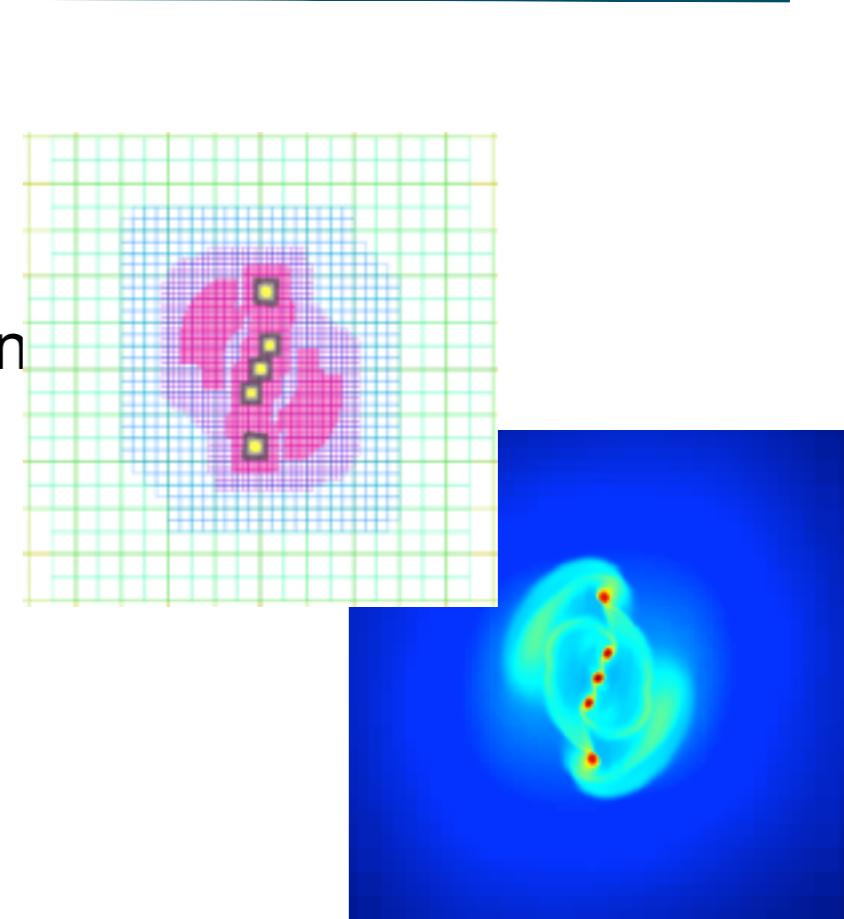
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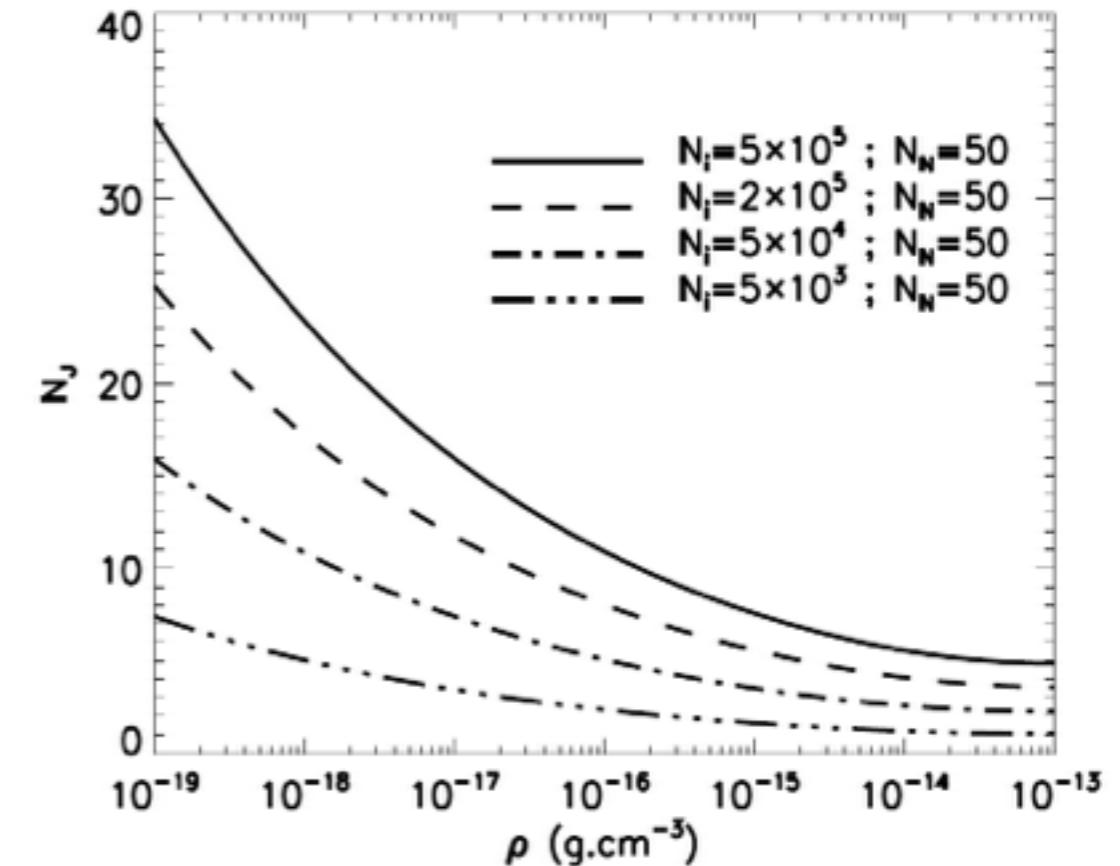
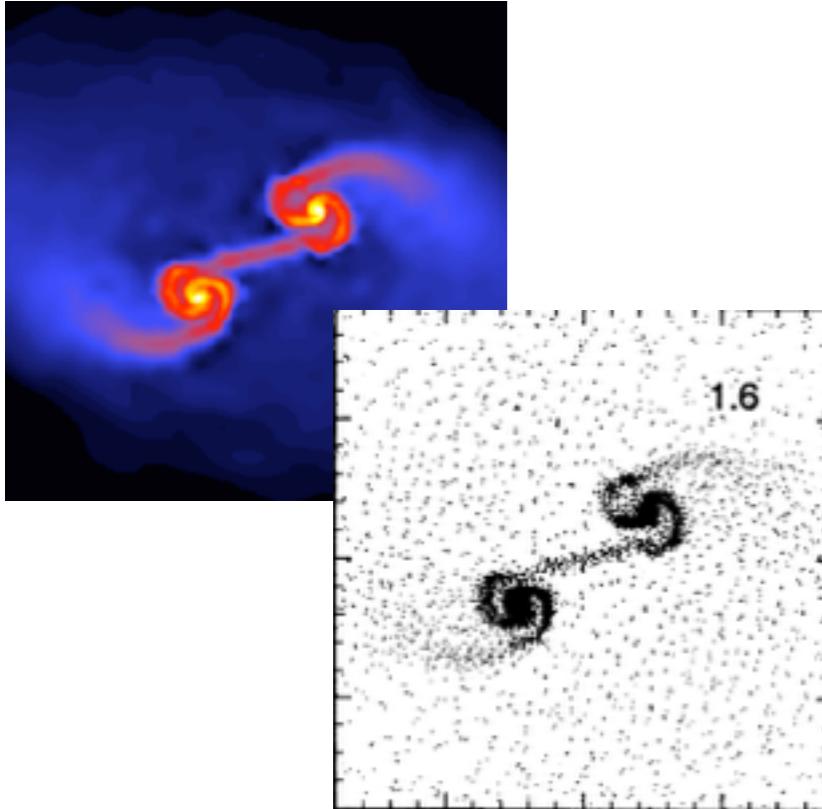


**SPH** : Total mass of the system particle + 2  $N_N$  ( $M_{\text{res}}$ ) should always be < than the local Jeans mass  $M_{\text{Jeans}}$  (Bate & Burkert 1997) → **static** criterion

↳ 2 parameters :  $N_p$  number of particles  
 $N_N$  number of neighbors

# Numerical resolution criteria for SF

AMR vs. SPH resolution:  $N_J^3 = M_{\text{Jeans}}/M_{\text{res}}$

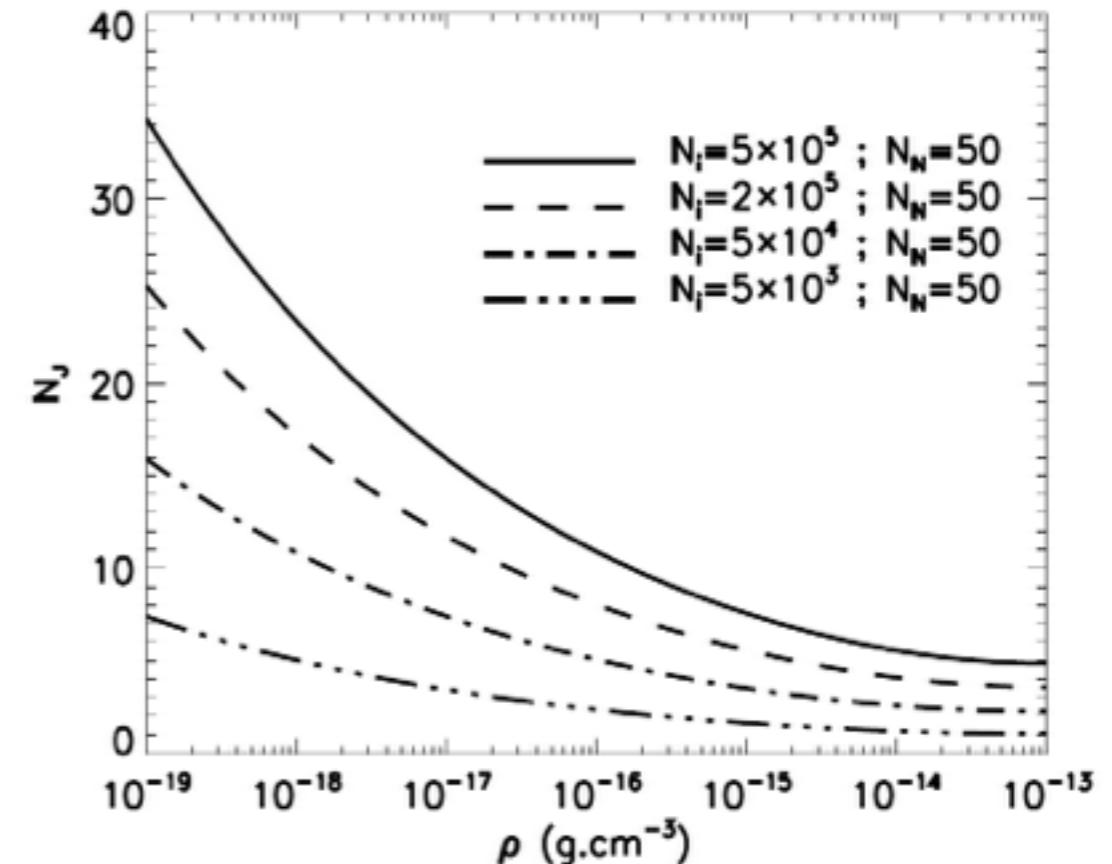


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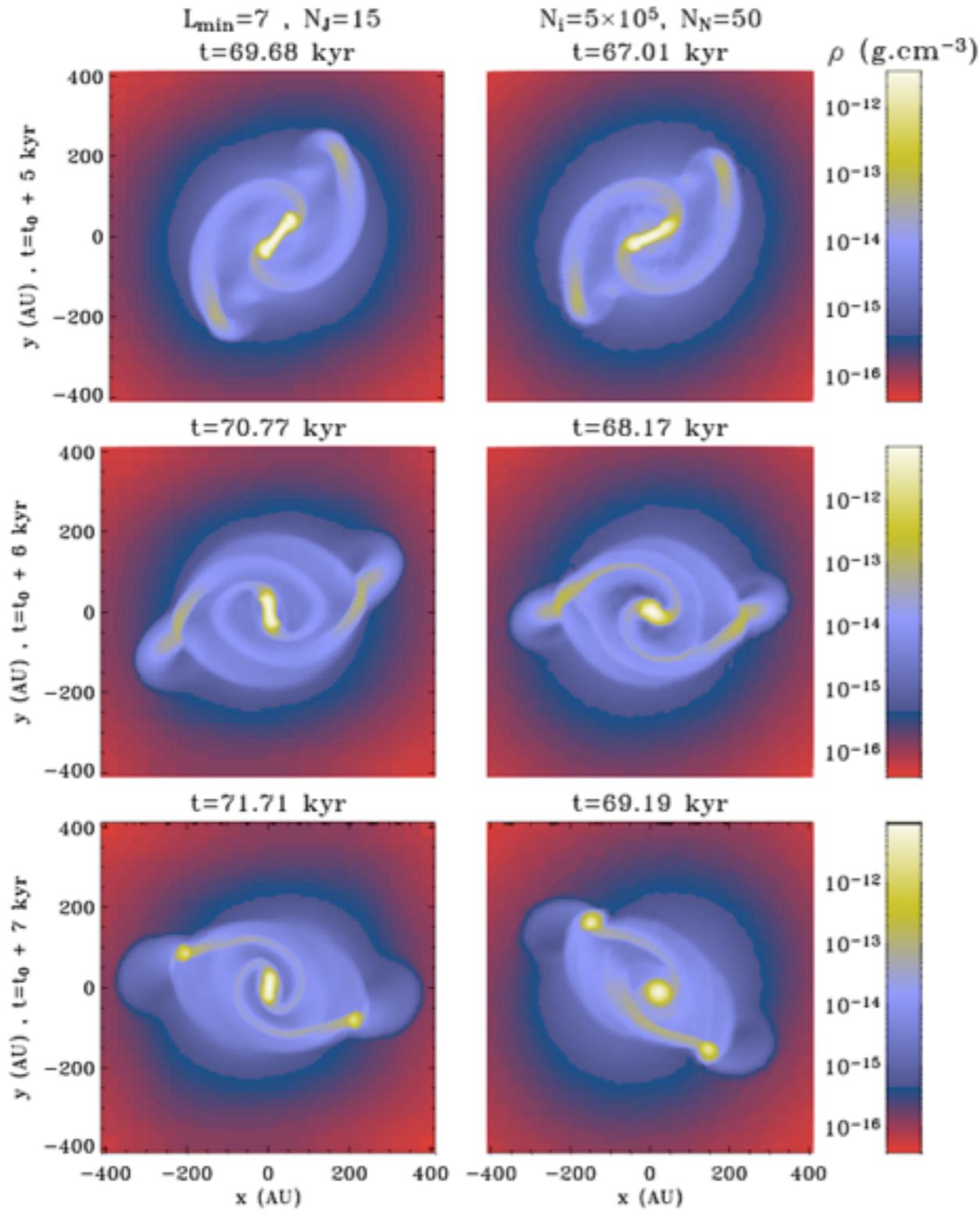
# Numerical resolution criteria for SF

AMR vs. SPH resolution:  $N_J^3 = M_{\text{Jeans}}/M_{\text{res}}$



- ★ Debate on the accuracy of both methods:
  - => Are these methods appropriate for star formation?
  - => Are they converging?
- ☞ Identical initial conditions (uniform density & temperature sphere in solid body rotation, Boss & Bodenheimer test)
- ☞ Same equations (Euler equation: mass, momentum and total energy + barotropic closure relation)

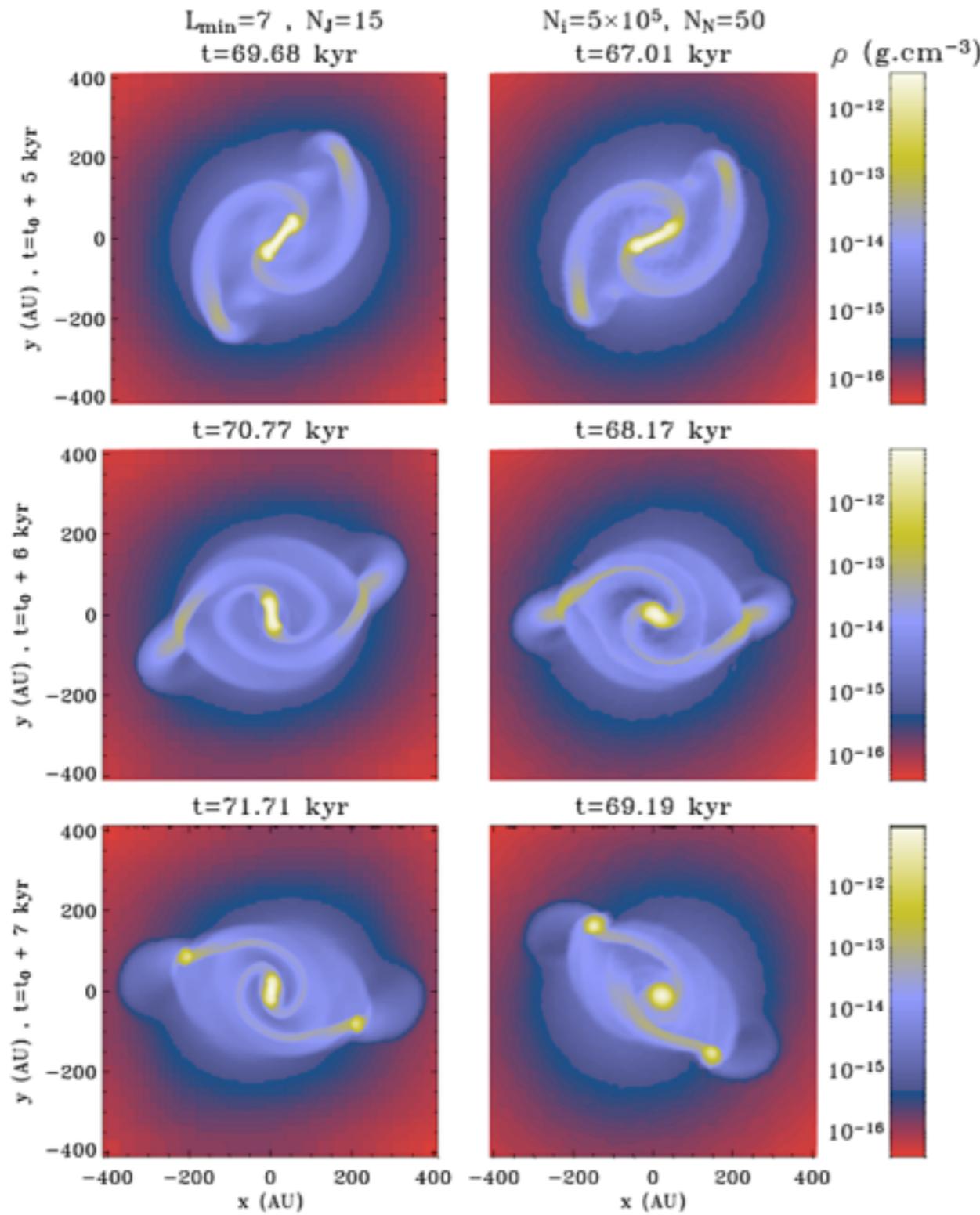
# AMR vs. SPH: Convergence



Hydro models

Commerçon et al. 2008

# AMR vs. SPH: Convergence



Hydro models

AMR:  $64^3$  ( $L_{\min}=6$ ) ;  **$N_J=15$  !**

SPH:  $N_p=5\times 10^5$  ;  $N_N=50$

i.e.  $\sim 5300$  particles/Jeans mass !

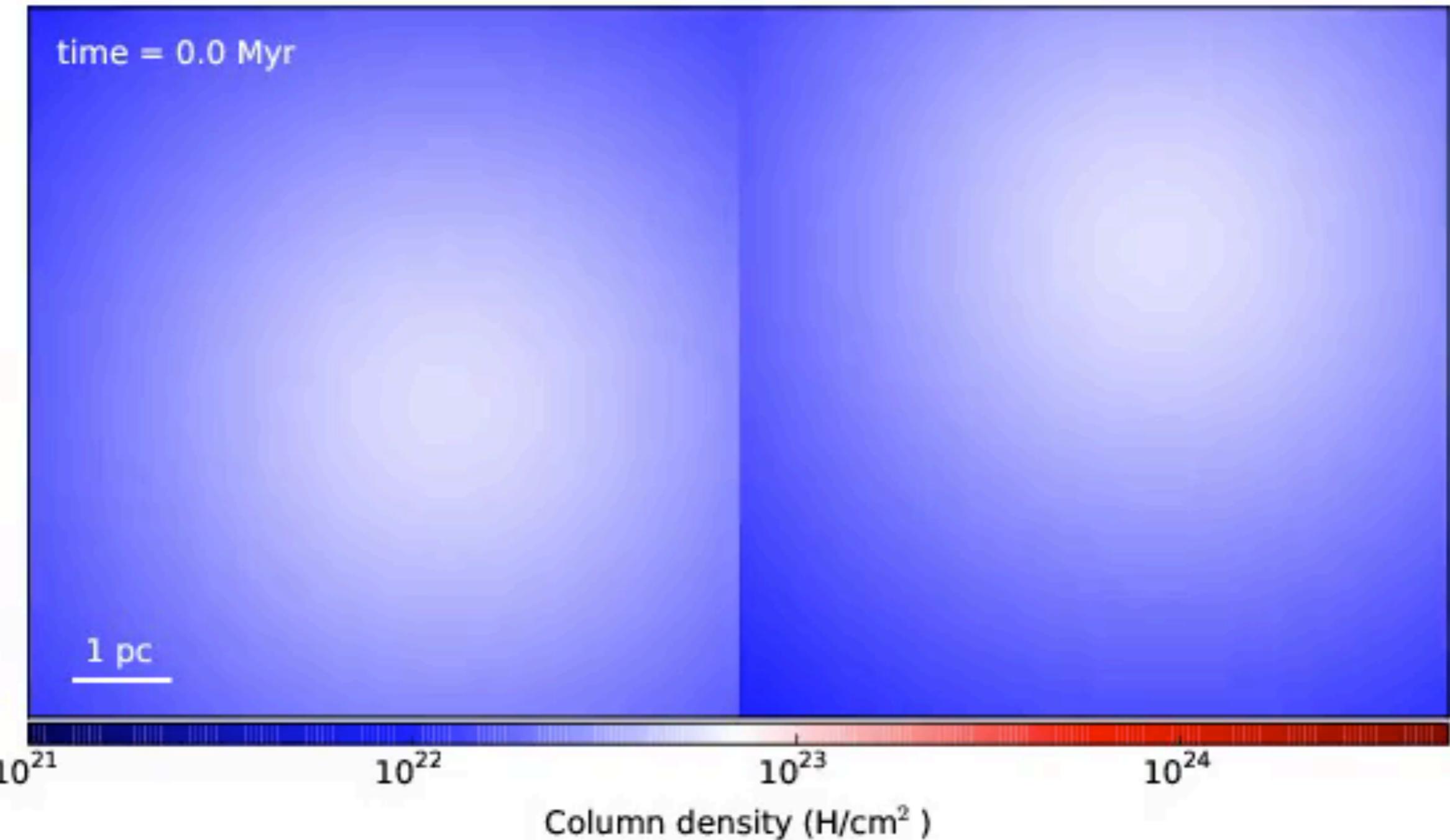
- CONVERGENCE!

Commerçon et al. 2008

# Star cluster formation

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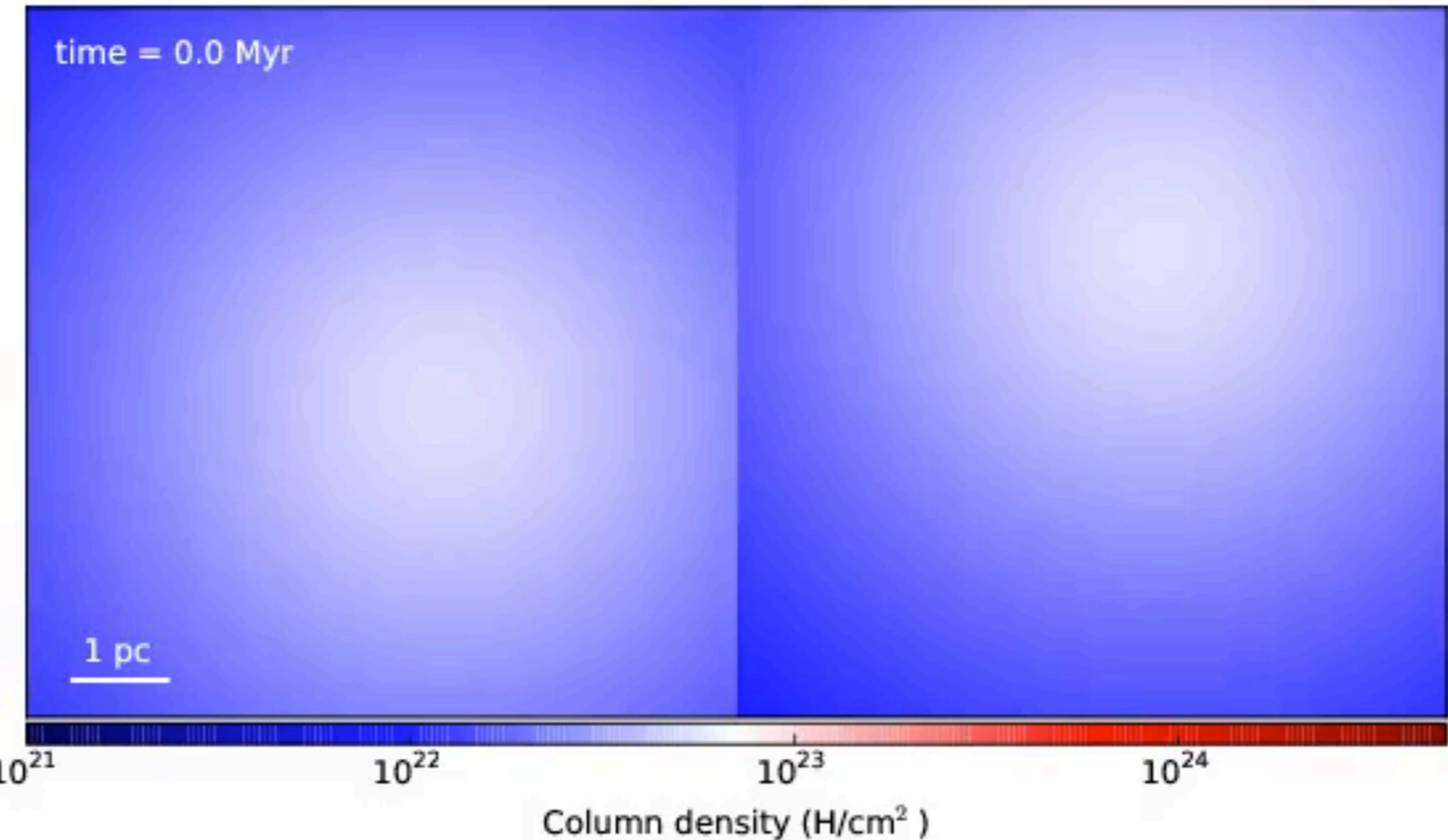
Lee, Hennebelle, Geen et al.



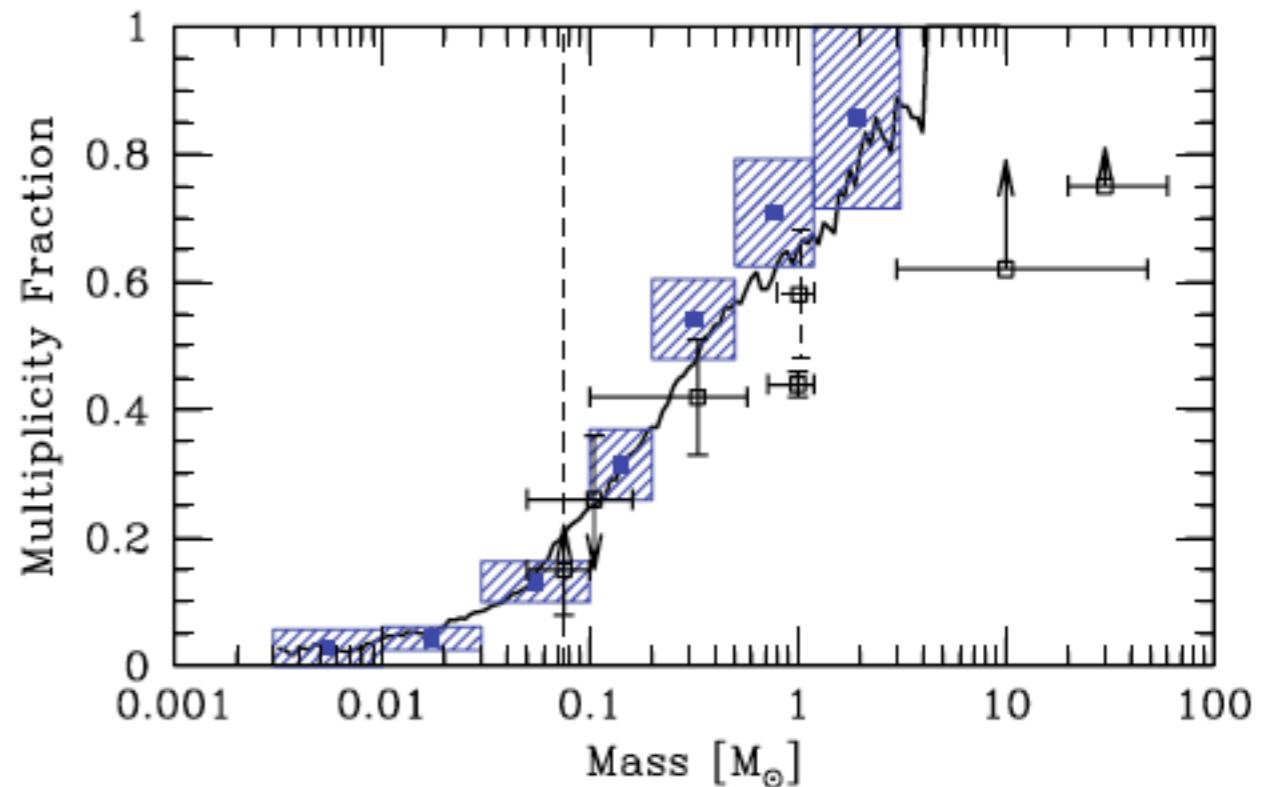
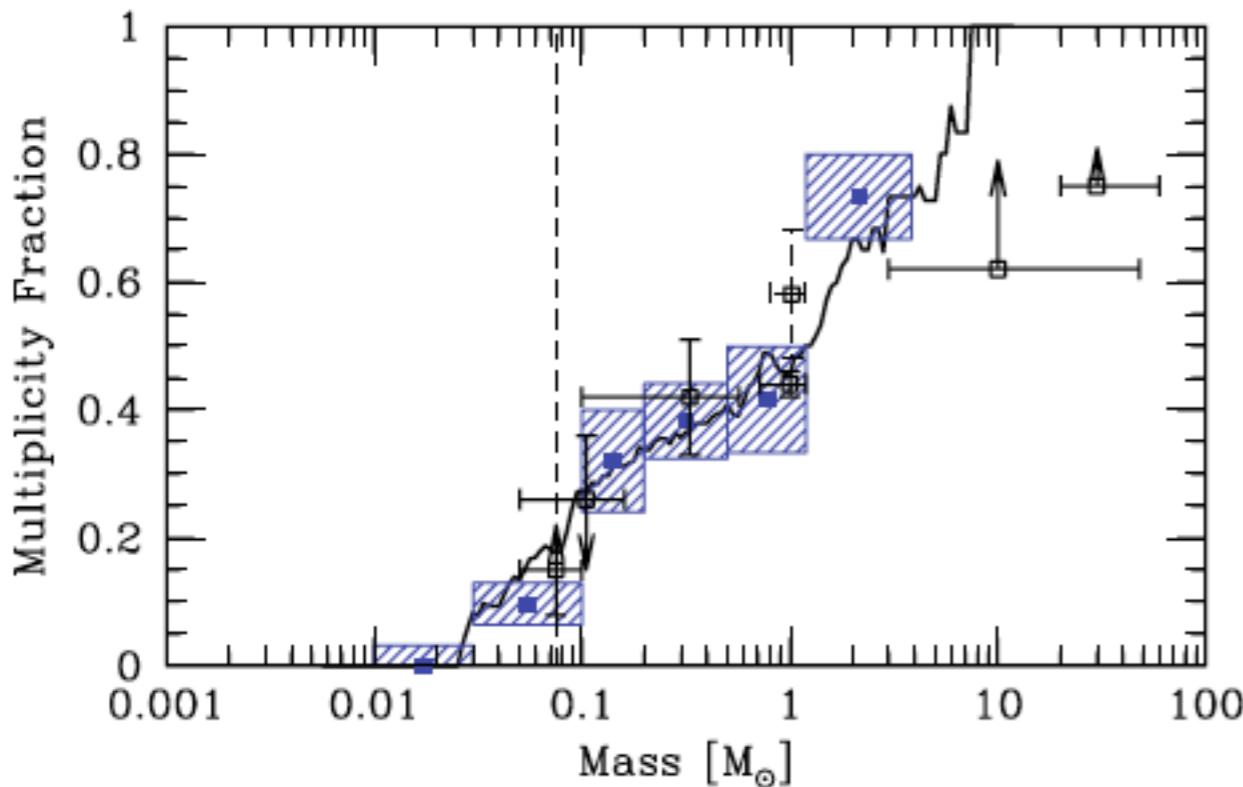
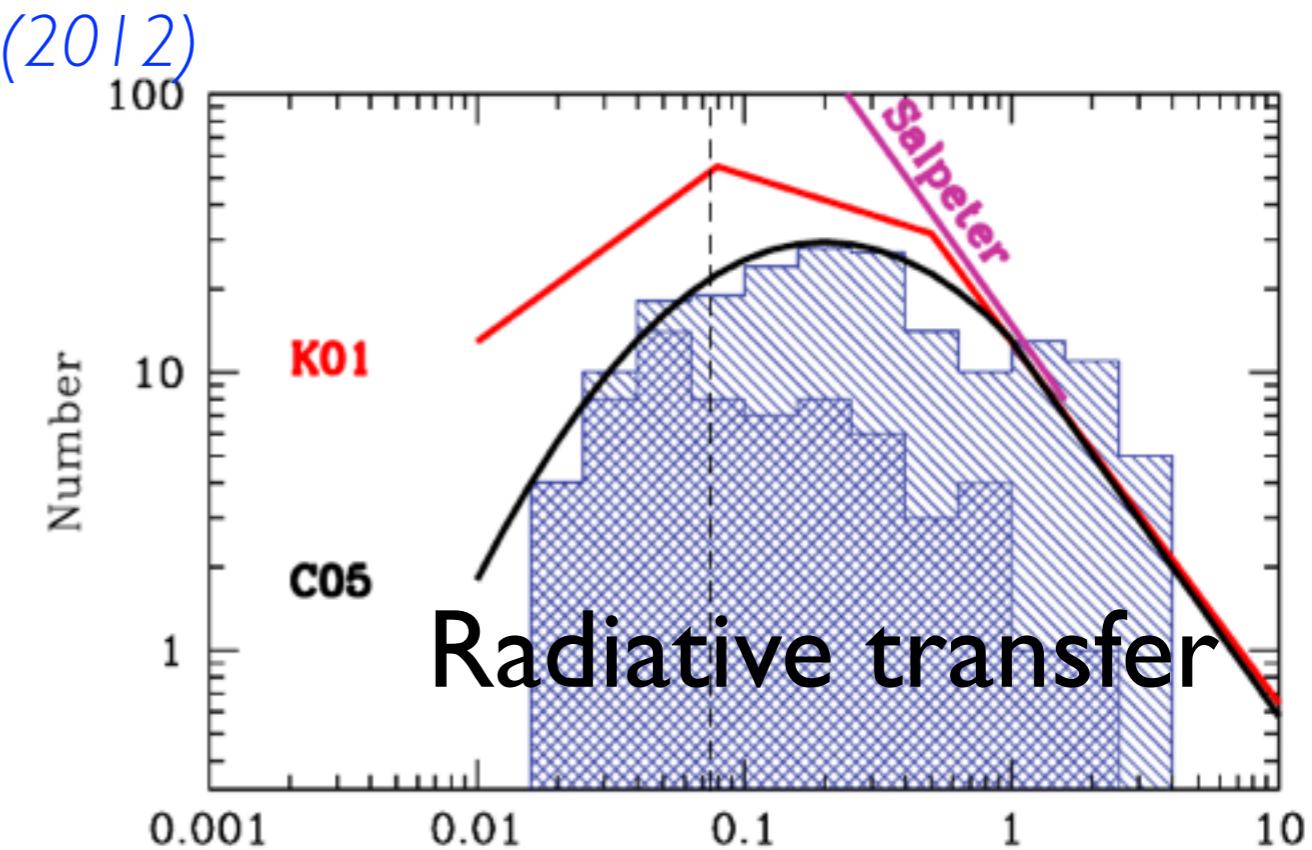
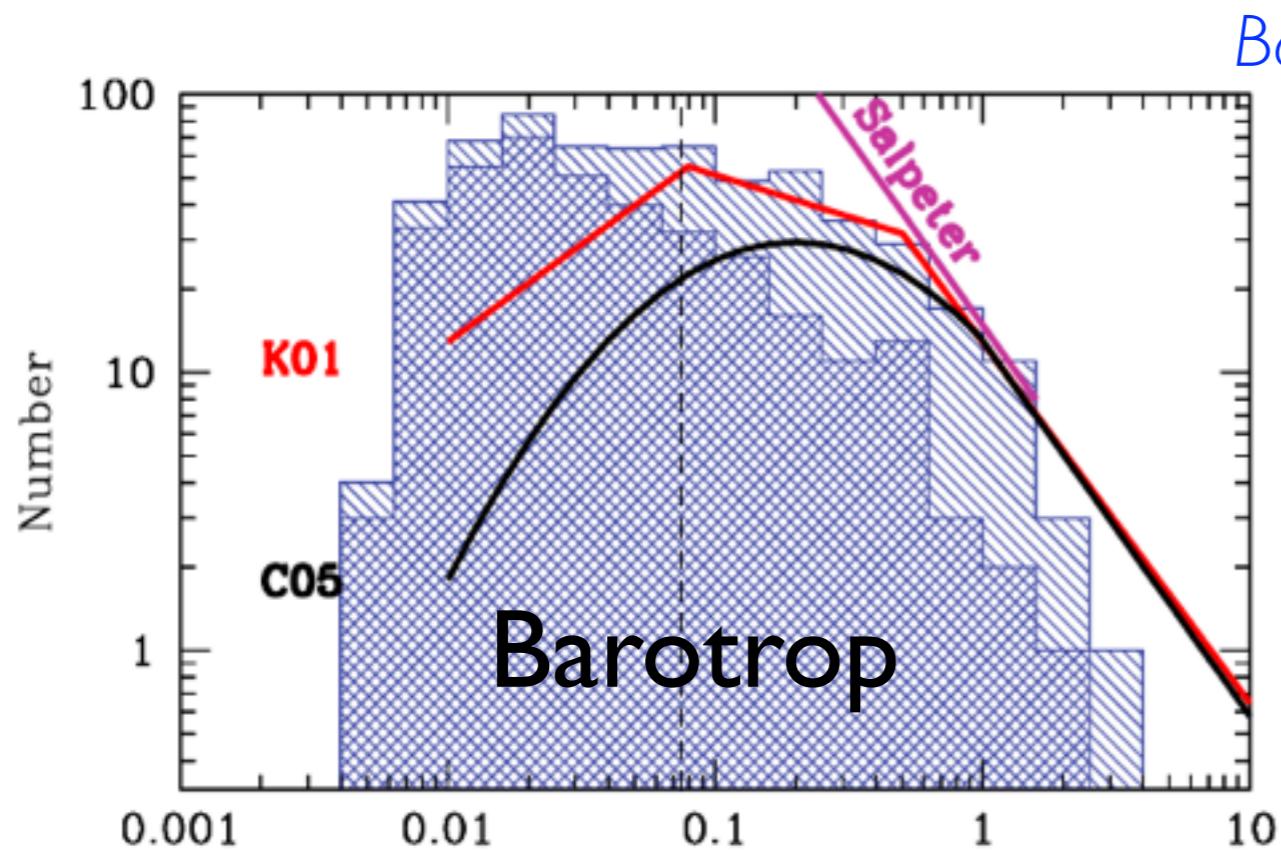
# Star cluster formation

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Lee, Hennebelle, Geen et al.



# Star cluster formation



# Formation of the protoplanetary disc

Benoît Commerçon - Anaëlle Maury

*Centre de Recherche Astrophysique de Lyon*

# Outline

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## 1. Introduction

## 2. Non ideal MHD

- chemistry
- ideal vs. non-ideal MHD

## 3. Disc formation

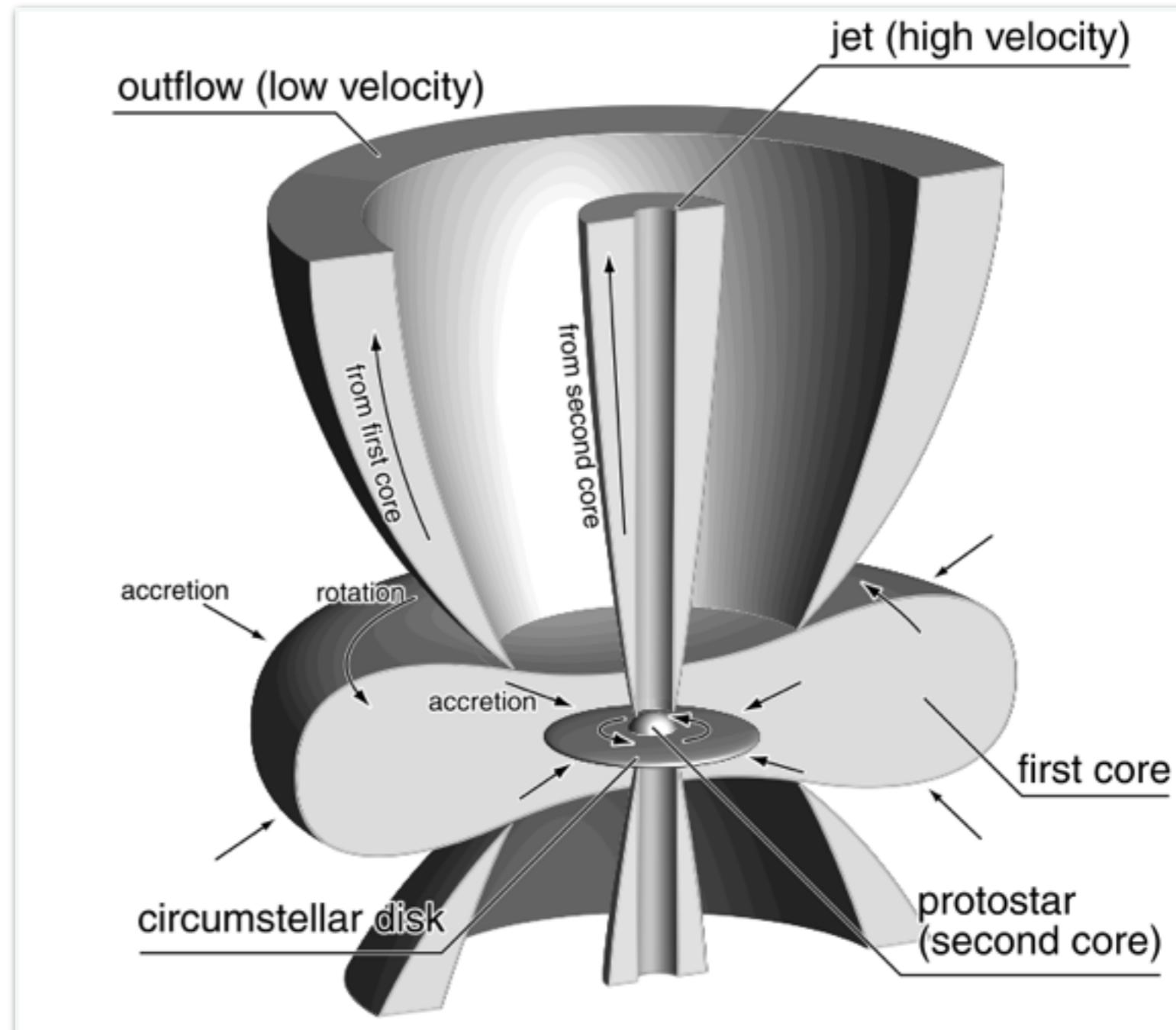
- properties
- evolution

## 4. Chemistry and dynamics

## 5. Comparison with observations

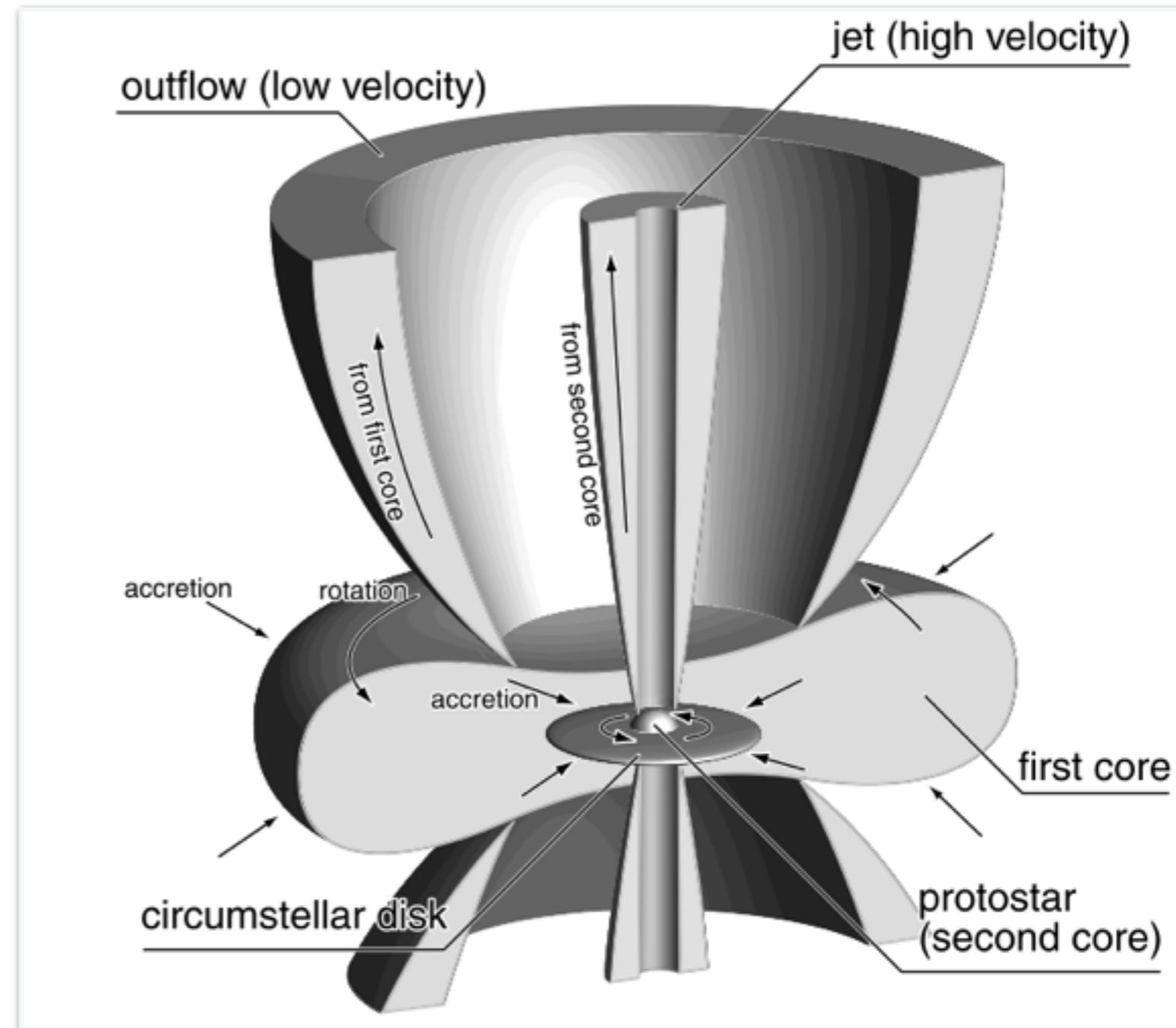
# Protostar formation

- Formation of a very complex structure, with jets, outflows, discs, etc..
- Disc formation depends highly on MHD effects...
- Chemistry, cosmic rays have to be taken into account to estimate ionization
- When does the disc form? Does it fragment?



# Protostar formation

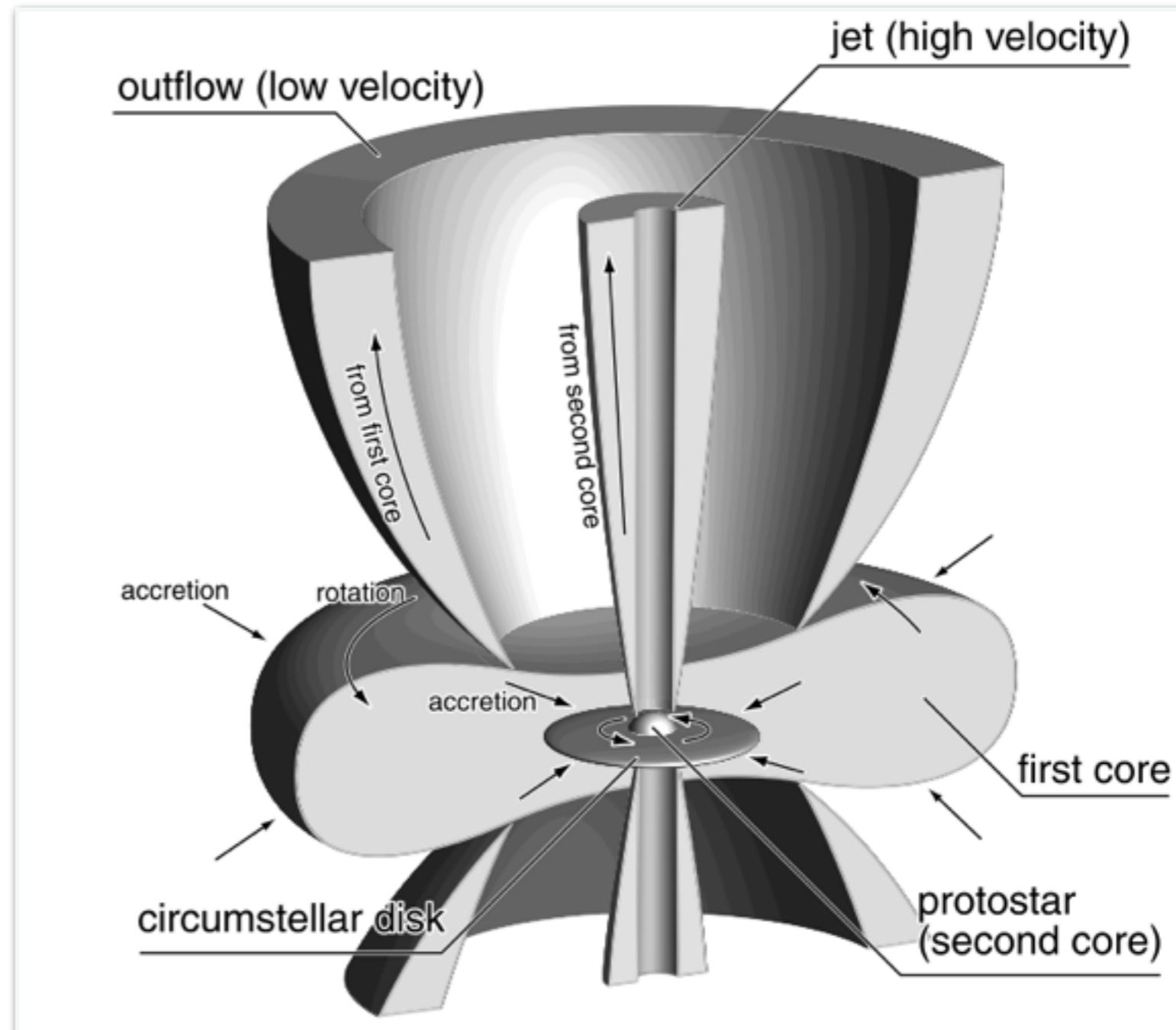
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Machida et al. (2010)

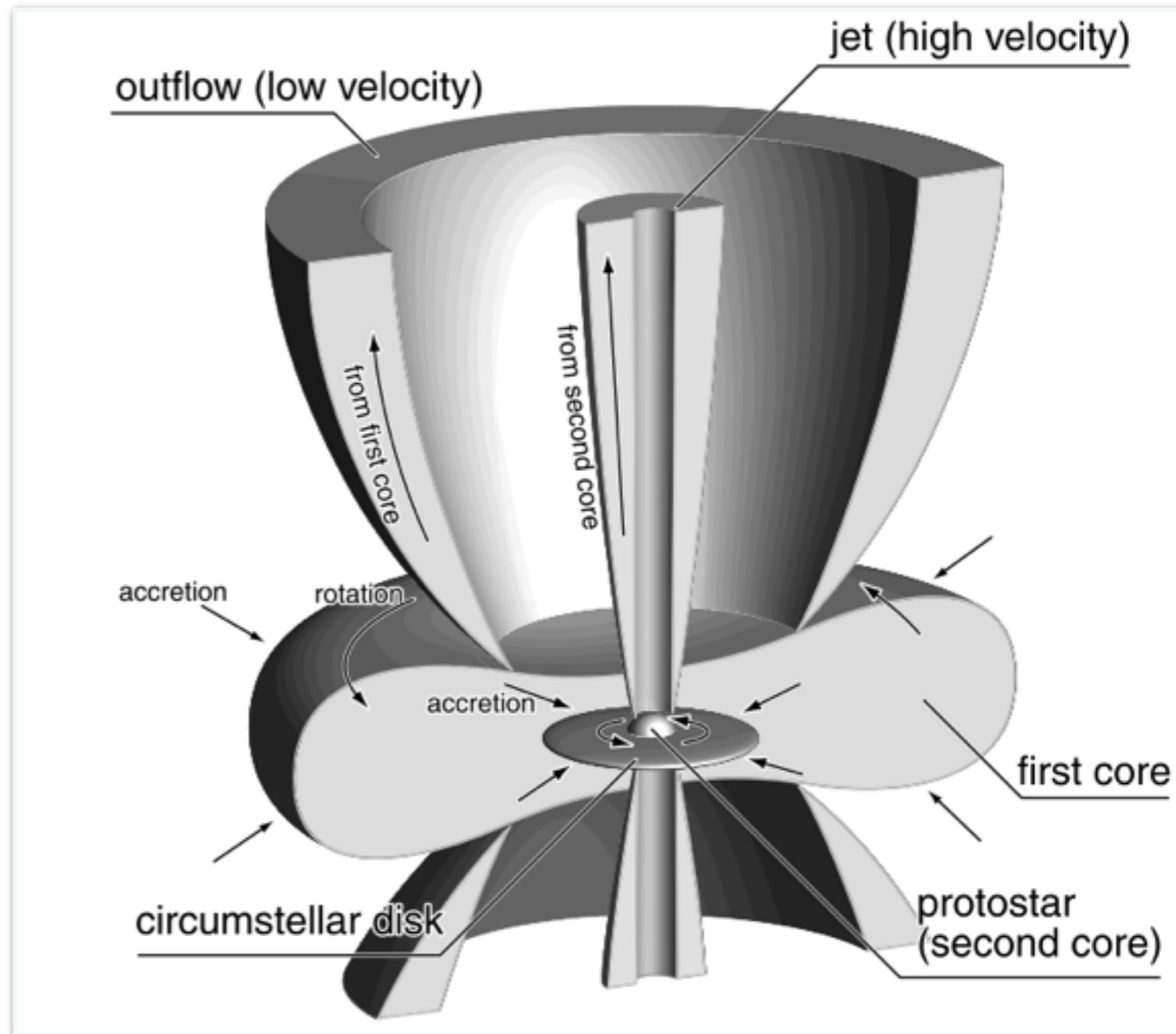
# Protostar formation

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- Implications for planet formation



# Protostar formation

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- Chemistry, cosmic rays have to be taken into account to estimate ionization
- When does the disc form? Does it fragment?
- Implications for planet formation



Machida et al. (2010)

# Effect of magnetic fields and rotation

---

Consider a dense core of initial radius  $R$ , mass  $M$  and temperature  $T$

## Thermal support

- $E_{\text{th}}/E_{\text{grav}}$  **decreases** when  $R$  decreases

$$\frac{E_{\text{th}}}{E_{\text{grav}}} = \frac{3M/m_p kT}{2GM^2/R} \propto R$$

## Centrifugal support

- Angular momentum conservation
- $E_{\text{rot}}/E_{\text{grav}}$  **increases** when  $R$  decreases

$$j = R_0^2 \omega_0 = R^2 \omega(t)$$

$$\frac{E_{\text{rot}}}{E_{\text{grav}}} = \frac{MR^2\omega^2}{GM^2/R} \propto \frac{1}{R}$$

## Magnetic support

- Magnetic flux conservation
  - $E_{\text{mag}}/E_{\text{grav}}$  is **constant** when  $R$  decreases
- $\mu = (\Phi/M)_{\text{crit}}/(\Phi/M)$  (observations  $\mu \sim 2-5$ )

$$\phi \propto BR^2$$

$$\frac{E_{\text{mag}}}{E_{\text{grav}}} = \frac{B^2 R^3}{GM^2/R} \propto \left(\frac{\phi}{M}\right)^2$$

# Effect of magnetic fields and rotation

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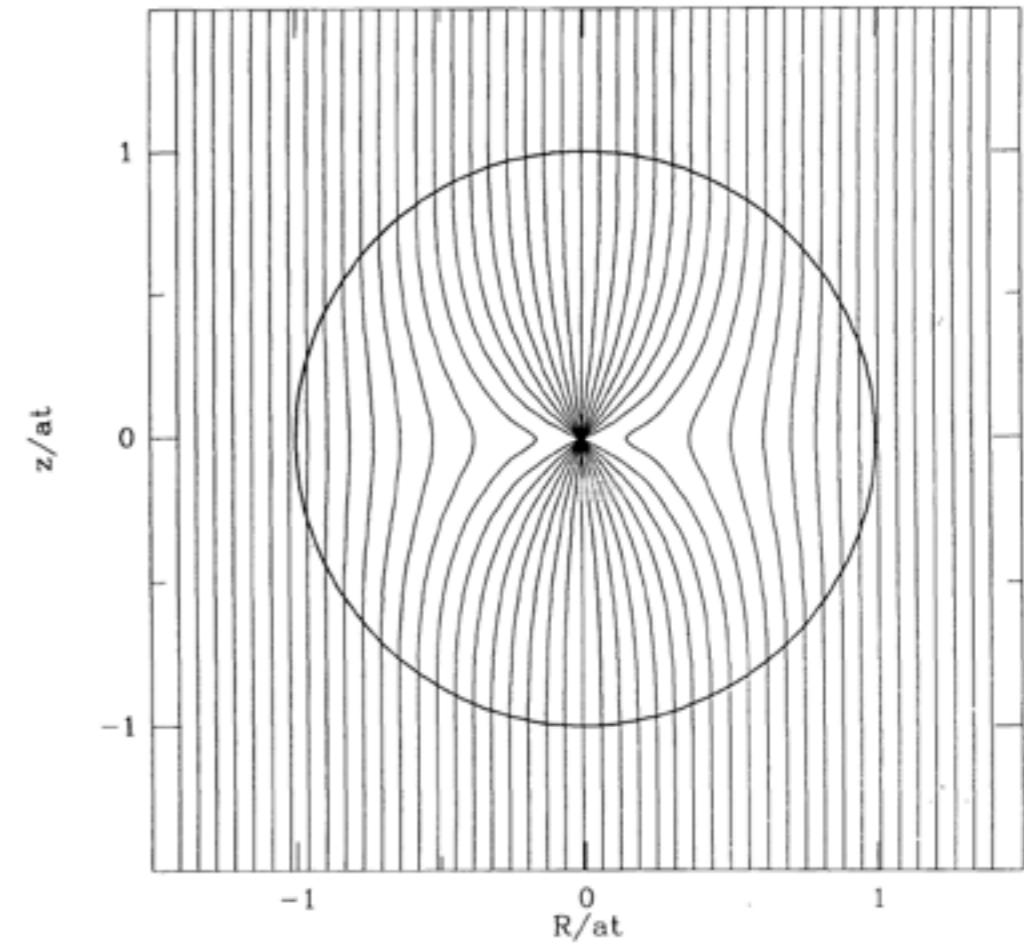
Consequences:

**Centrifugal forces become dominant**

- flattening of the envelope
- formation of a centrifugally supported disc

**Magnetic forces stay comparable to gravity**

- flattening of the envelope
- NO formation of a supported structure
- formation of a pseudo-disc (Galli & Shu 1993)

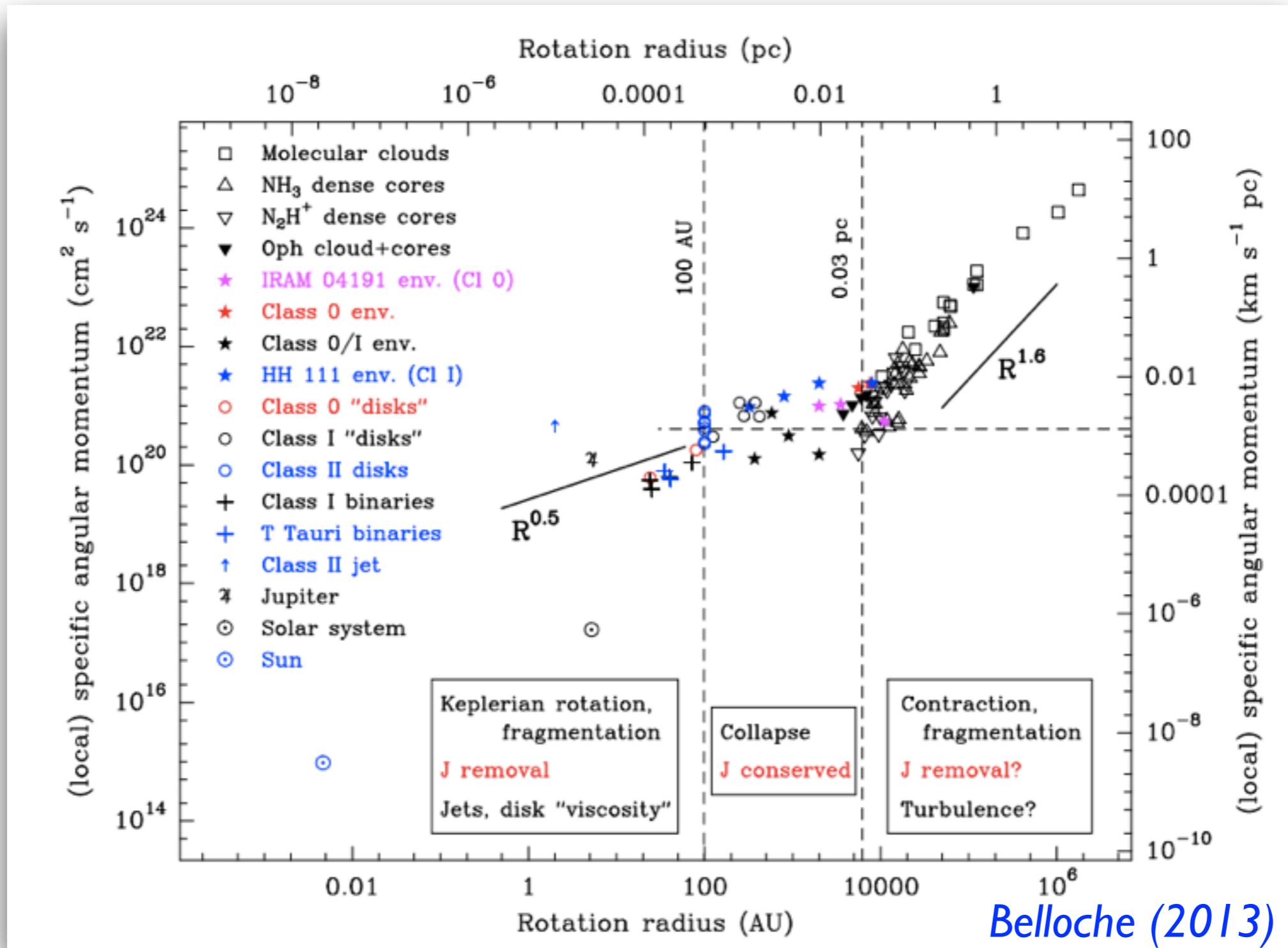


Galli & Shu 1993

**Magnetic fields brakes the cloud**

- transfer angular momentum from the inner part to the envelop

# Angular momentum conservation



# Magnetic flux problem

---

Consider a cloud of initial radius  $R=0.1$  pc,  $B \sim 10 \mu\text{G}$

- ✓ Magnetic flux  $\Phi = \pi B R^2 \sim 3 \times 10^{32} \text{ G cm}^2$
- ✓ if flux is conserved, at a solar radius ( $6.5 \times 10^{10} \text{ cm}$ ),  $B \sim 10^{10} \text{ G}$

→ Magnetic field in star is observed to be  $< 10^4 \text{ G}$

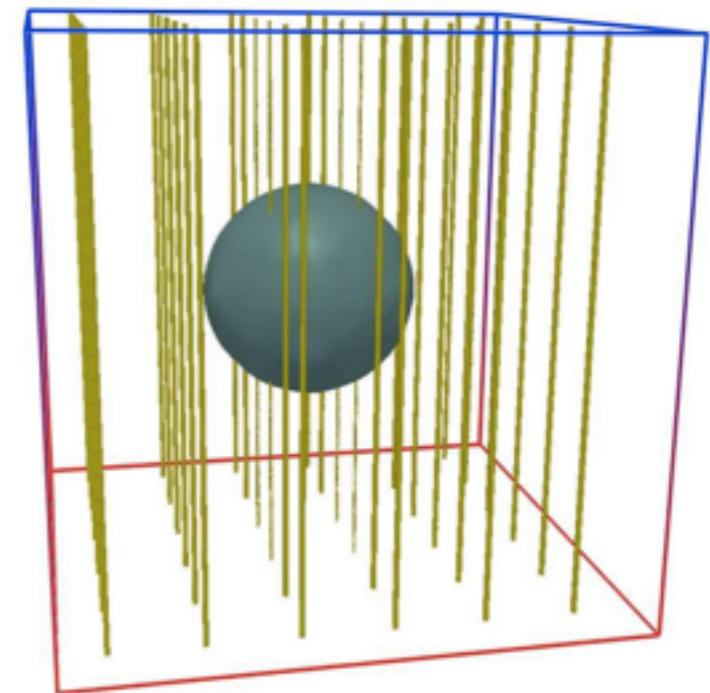
=> Magnetic flux as to be removed or transported away during gravitational collapse

# Numerical experiments

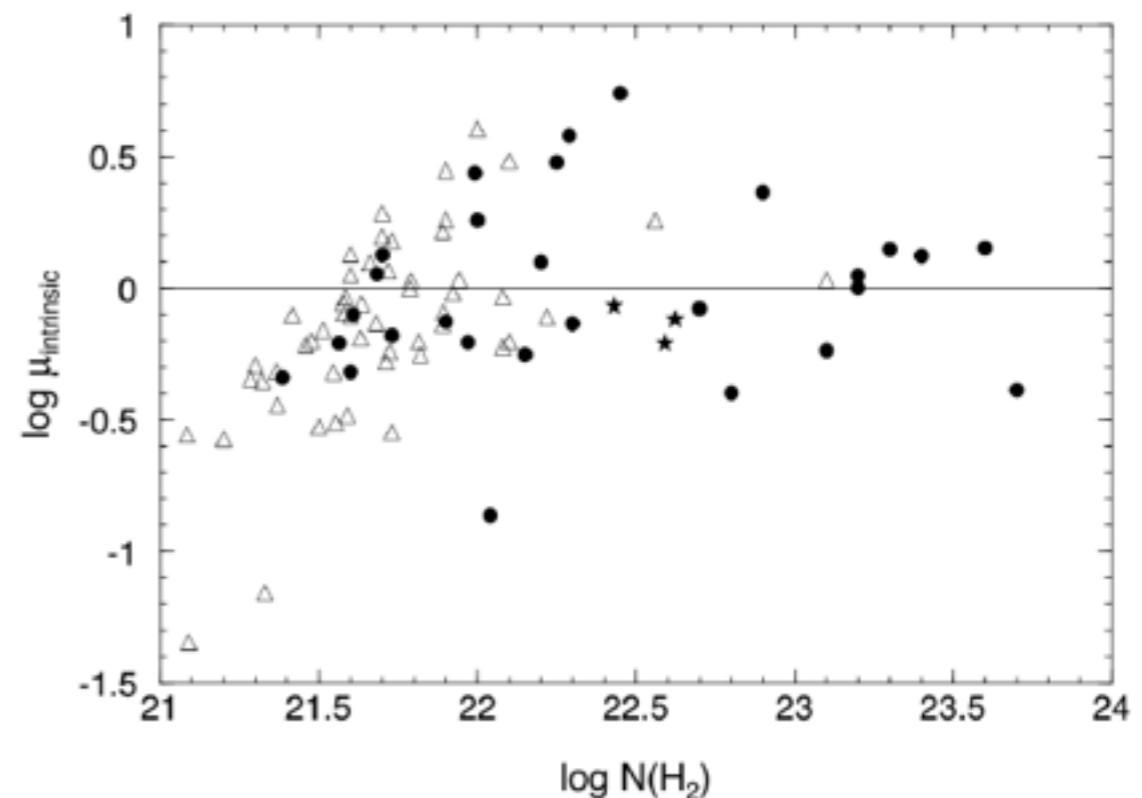
## Typical initial conditions:

- $1 M_{\odot}$  isolated dense core
- uniform / BE-like density profile
- uniform temperature (10 K,  $\alpha = E_{\text{th}}/E_{\text{grav}}$ )
- solid body / differential rotation ( $\beta = E_{\text{rot}}/E_{\text{grav}}$ )
- $m=2$  density perturbation / turbulent velocity field
- organised magnetic field

$$\mu = (\varphi/M)_{\text{crit}} / (\varphi/M) \text{ (observations } \mu \sim 2-5)$$



Refinement criterion solely based on  
the Jeans length

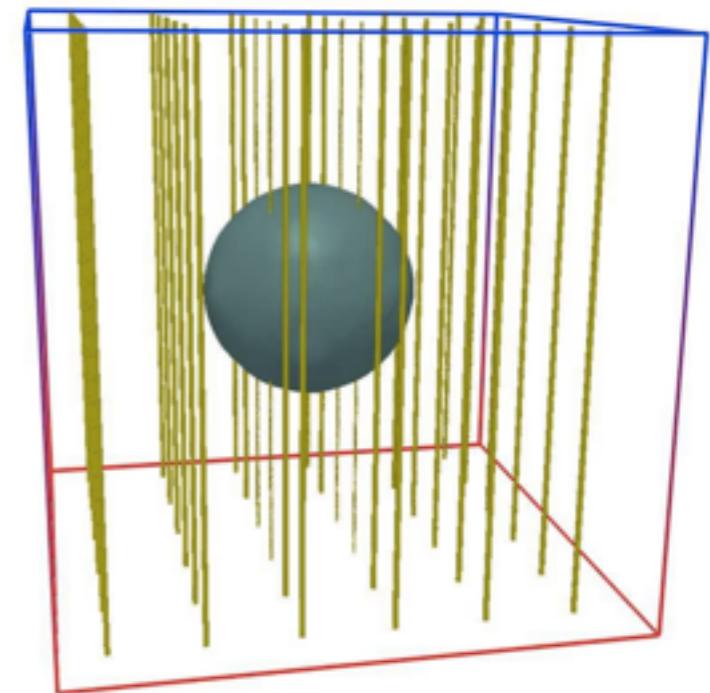


# Numerical experiments

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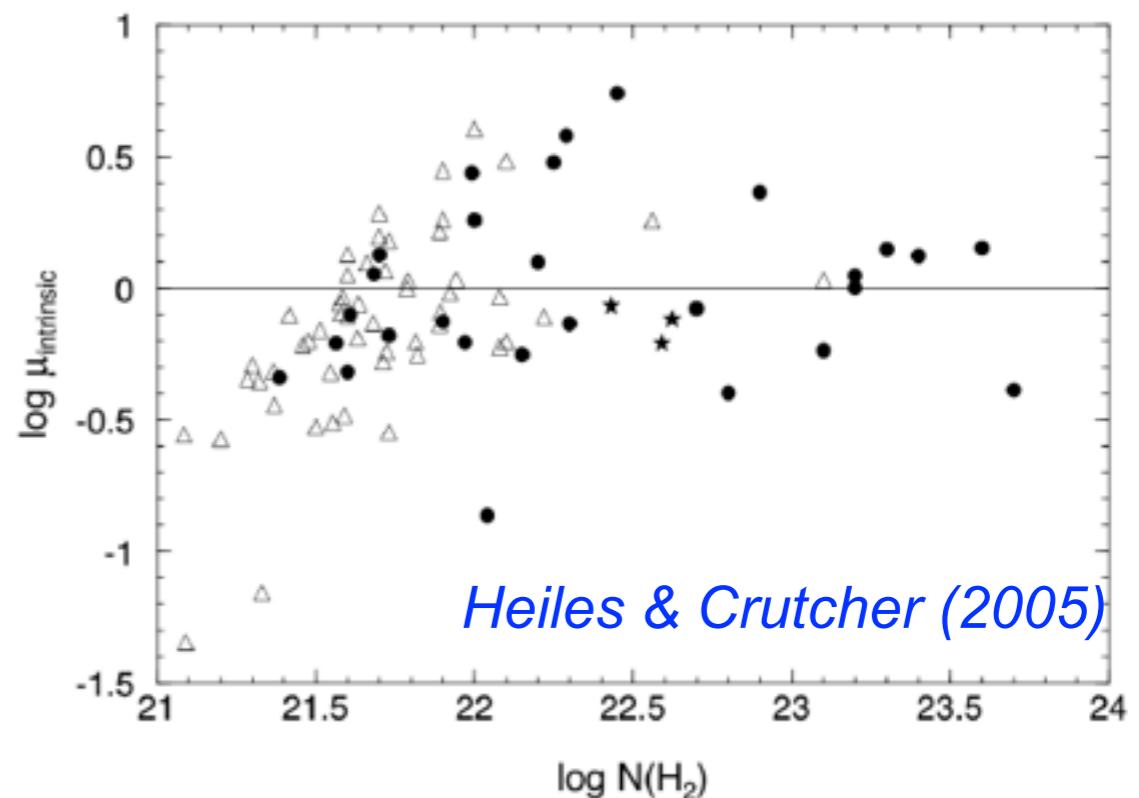
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Banerjee & Pudritz (2006)

Refinement criterion solely based on  
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# State-of-the-art

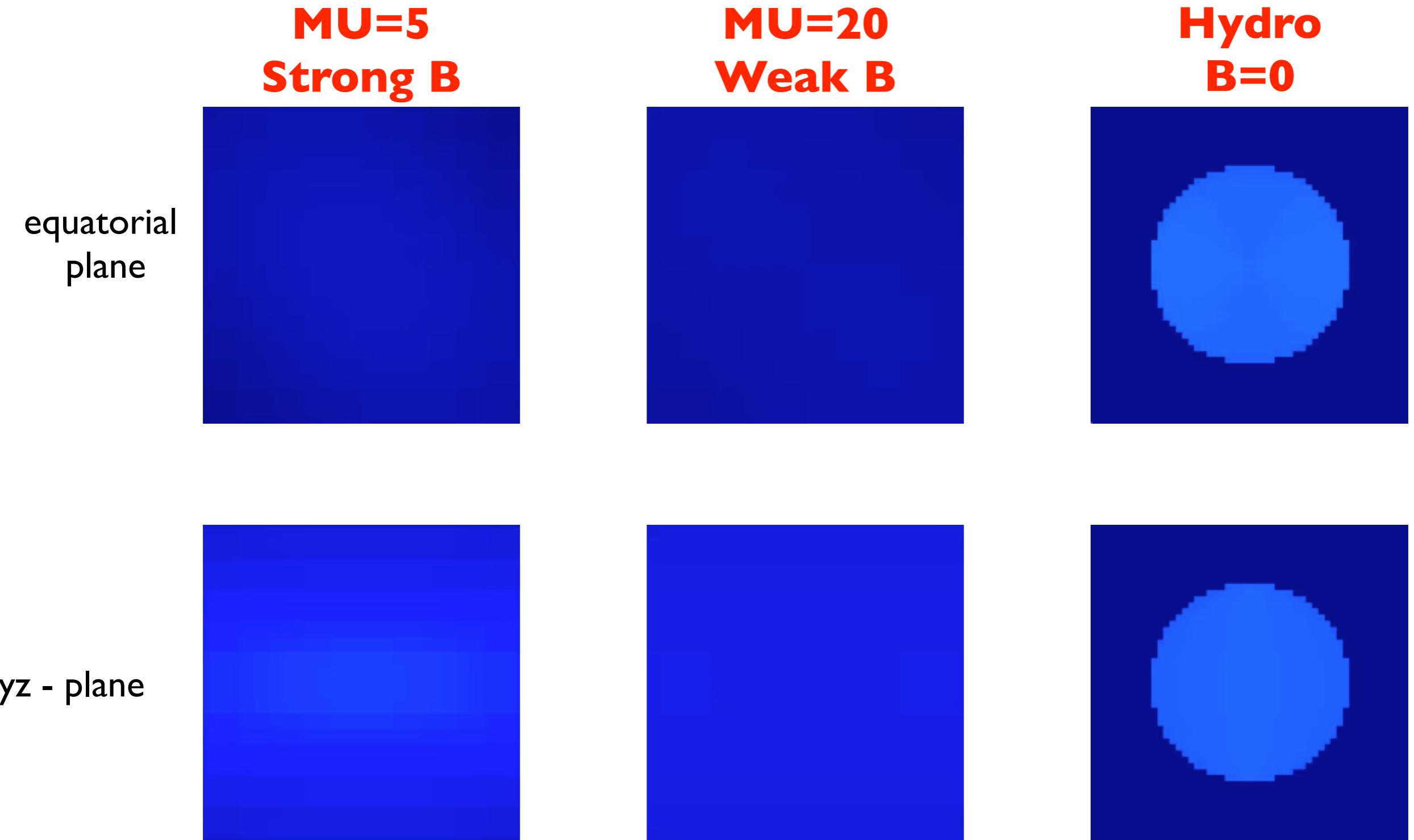
## 3D dynamical models make step-by-step necessary developments

- magnetic fields: ideal and non ideal MHD
- radiation hydrodynamics
- chemodynamics, but no retroaction
- cosmic rays
- inclusion of different feedback processes

$$\left\{ \begin{array}{l} \partial_t \rho + \nabla \cdot [\rho \mathbf{u}] = 0 \\ \partial_t \rho \mathbf{u} + \nabla \cdot [\rho \mathbf{u} \otimes \mathbf{u} + P \mathbb{I} - \mathbf{B} \otimes \mathbf{B}] = -\lambda \nabla E_r \\ \partial_t E_T + \nabla \cdot [\mathbf{u} (E_T + P) + \mathbf{B} (\mathbf{B} \cdot \mathbf{u})] = -\mathbb{P}_r \nabla : \mathbf{u} - \lambda \mathbf{u} \nabla E_r + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) \\ \partial_t E_r + \nabla \cdot [\mathbf{u} E_r] = -\mathbb{P}_r \nabla : \mathbf{u} + \nabla \cdot \left( \frac{c\lambda}{\rho \kappa_R} \nabla E_r \right) + \kappa_P \rho c (a_R T^4 - E_r) \\ \partial_t \mathbf{B} + \nabla \times \left[ \mathbf{u} \times \mathbf{B} - \frac{\mathbf{J} \times \mathbf{B}}{en_e} + \frac{[(\nabla \times \mathbf{B}) \times \mathbf{B}] \times \mathbf{B}}{\gamma_{AD} \rho \rho_i} - \frac{\mathbf{J}}{\sigma_{||}} \right] = 0 \end{array} \right.$$

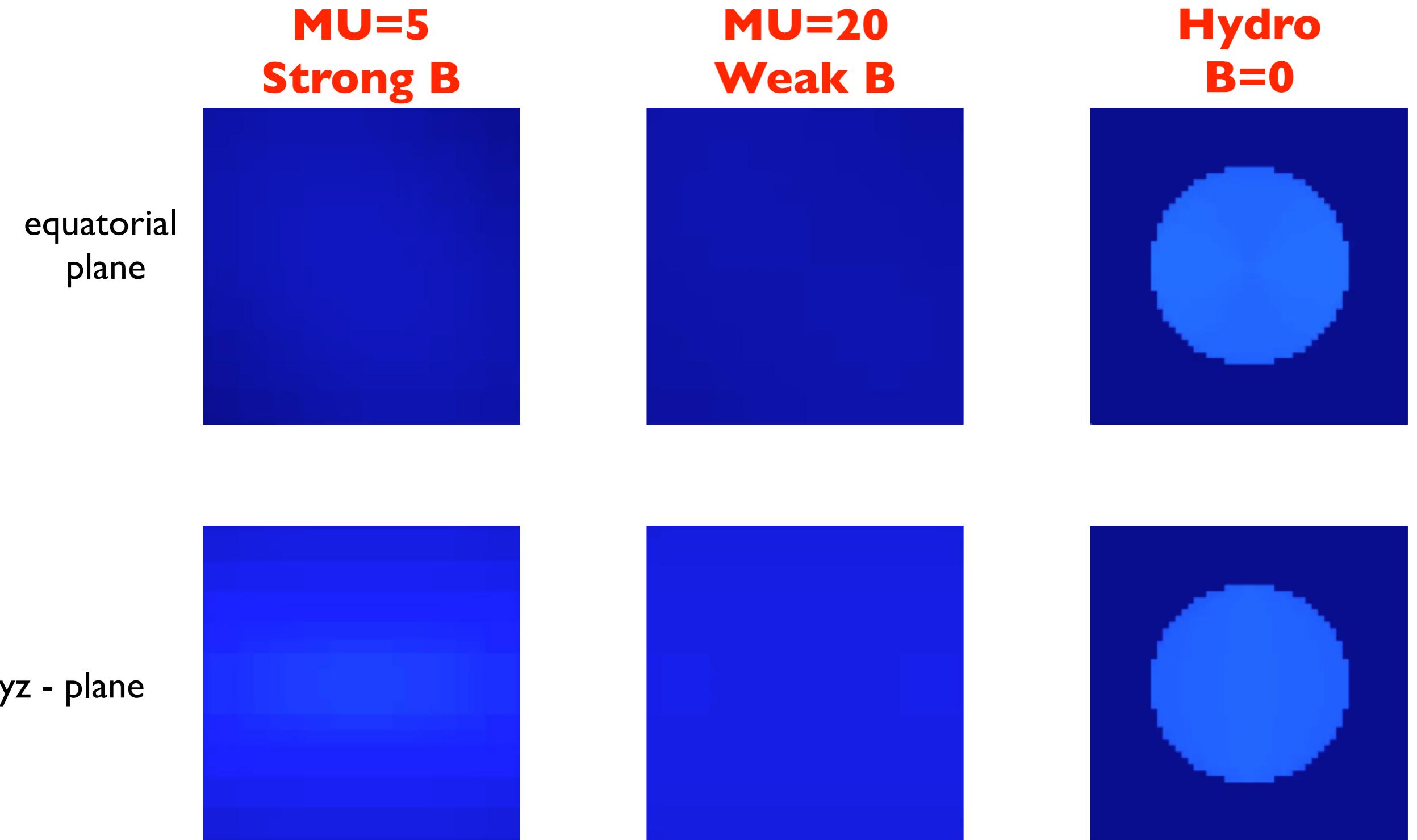
# Influence of the magnetization (ideal MHD)

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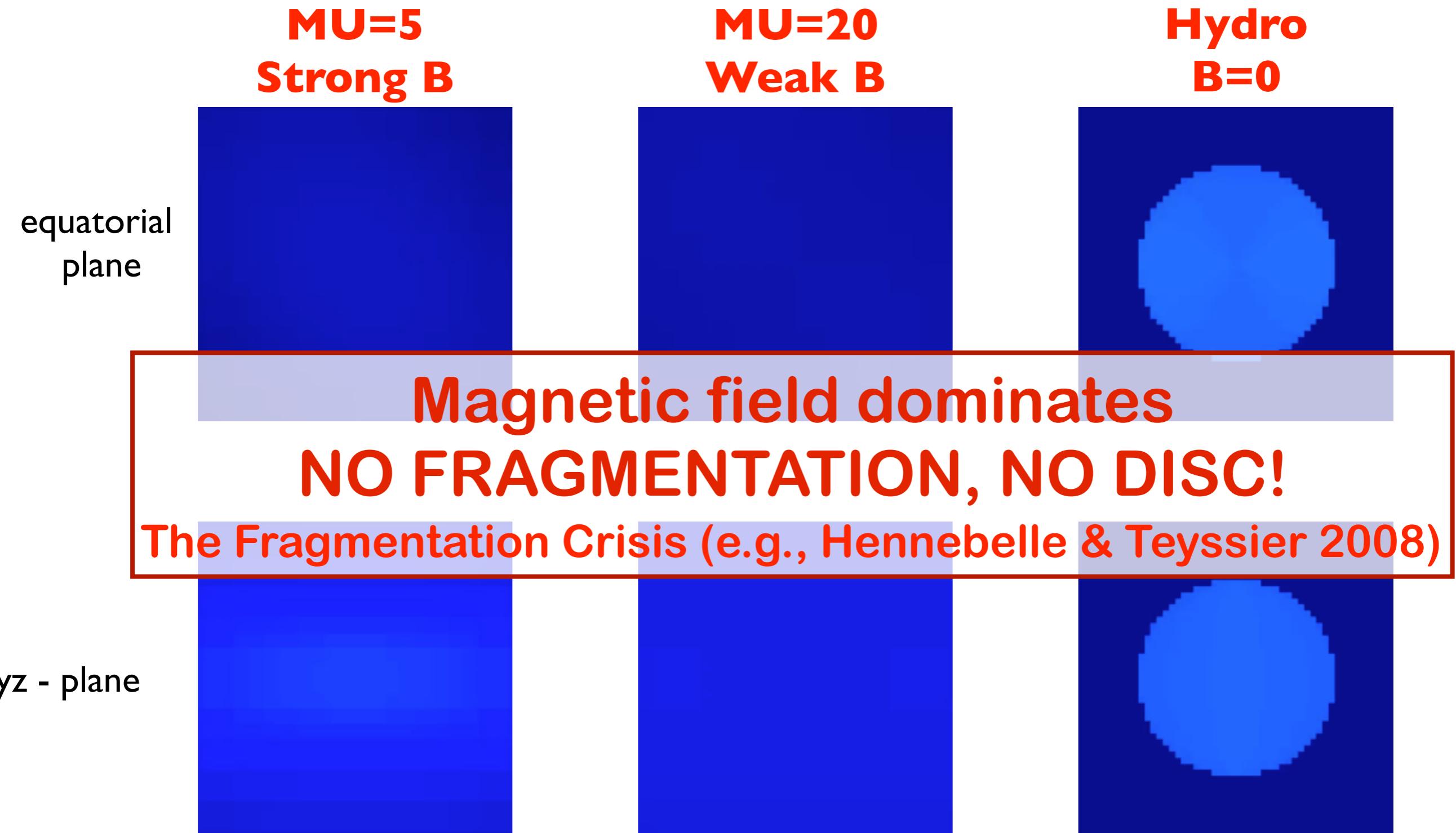


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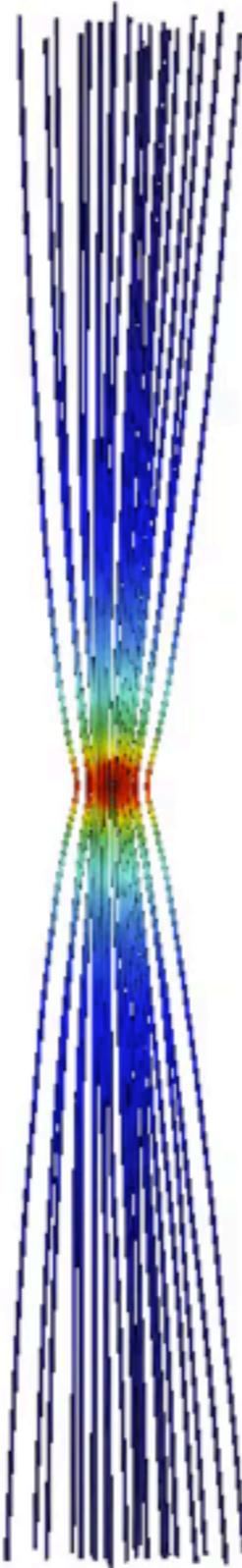


# Influence of the magnetization (ideal MHD)



# Dense core collapse

---

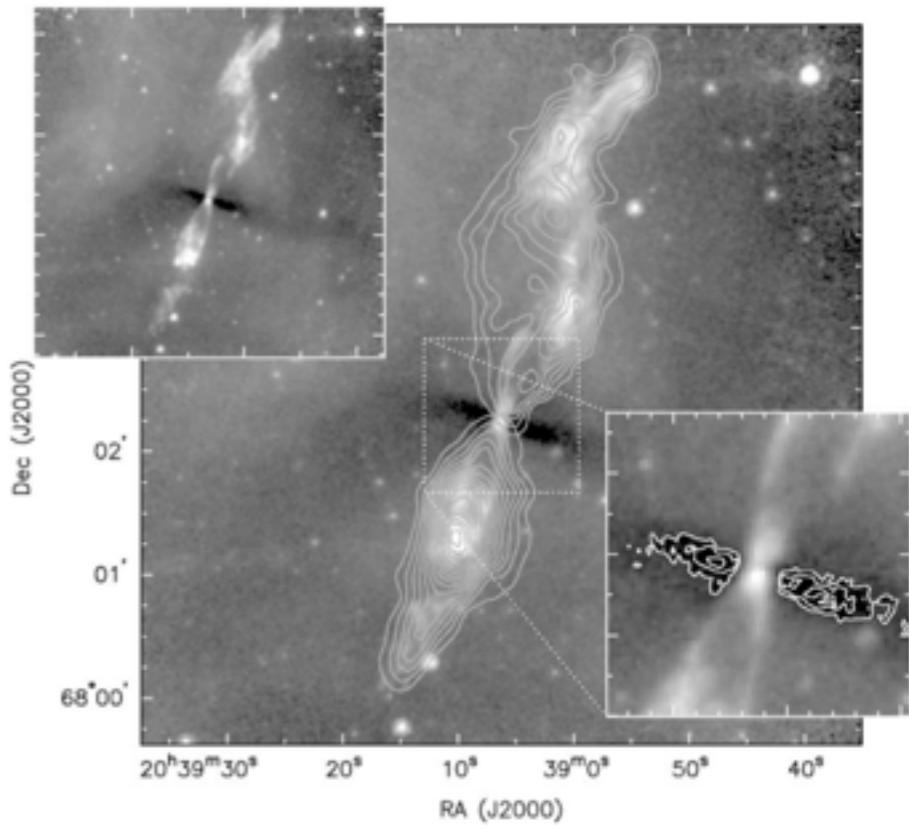
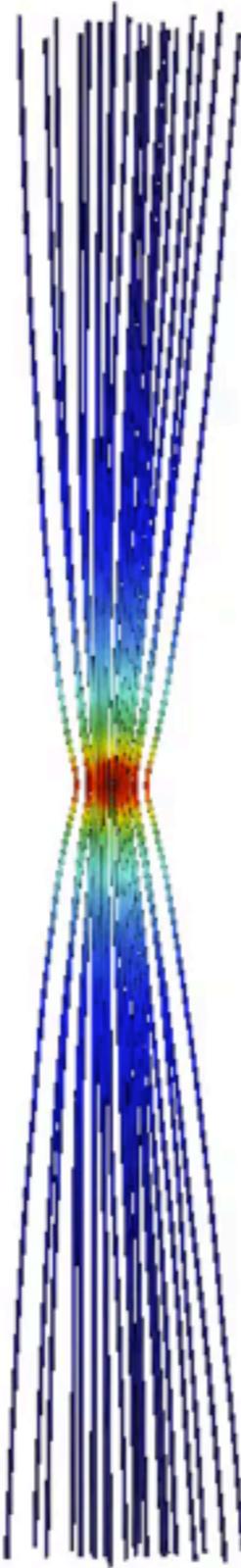


*Movie by Marc Joos*

# Dense core collapse

---

Movie by Marc Joos



*Looney et al. 2007*

# Disc formation in magnetised cores

---

- ✓ **Late formation**
  - end of class 0,  $M_{\text{env}} \ll M_{\text{env},0}$  (e.g., *Machida & Hosokawa 2013*)
- ✓ **Misalignment**
  - no reason for the rotation axis and the magnetic field to be aligned (e.g., *Hull et al. 2013*)
  - reduces magnetic braking efficiency (e.g. *Hennebelle & Ciardi 2009, Joos et al. 2012, Li et al. 2013*)
- ✓ **Turbulent diffusion**
  - reconnection events fast with Ohmic diffusion only, collective effect at larger scale (e.g. *Santos Lima et al. 2012, Joos et al. 2013, Seifried et al. 2013*)
- ✓ **Non-ideal MHD**
  - Ohm dissipation (*Tomida et al. 2013, 2015, Machida et al.*)
  - Hall effect (*Krasnopol'sky et al. 2011, Tsukamoto et al. 2015, Wurster et al. 2016*)
  - ambipolar diffusion (*Tsukamoto et al. 2015, Wurster et al. 2016*)

# Disc formation in magnetised cores

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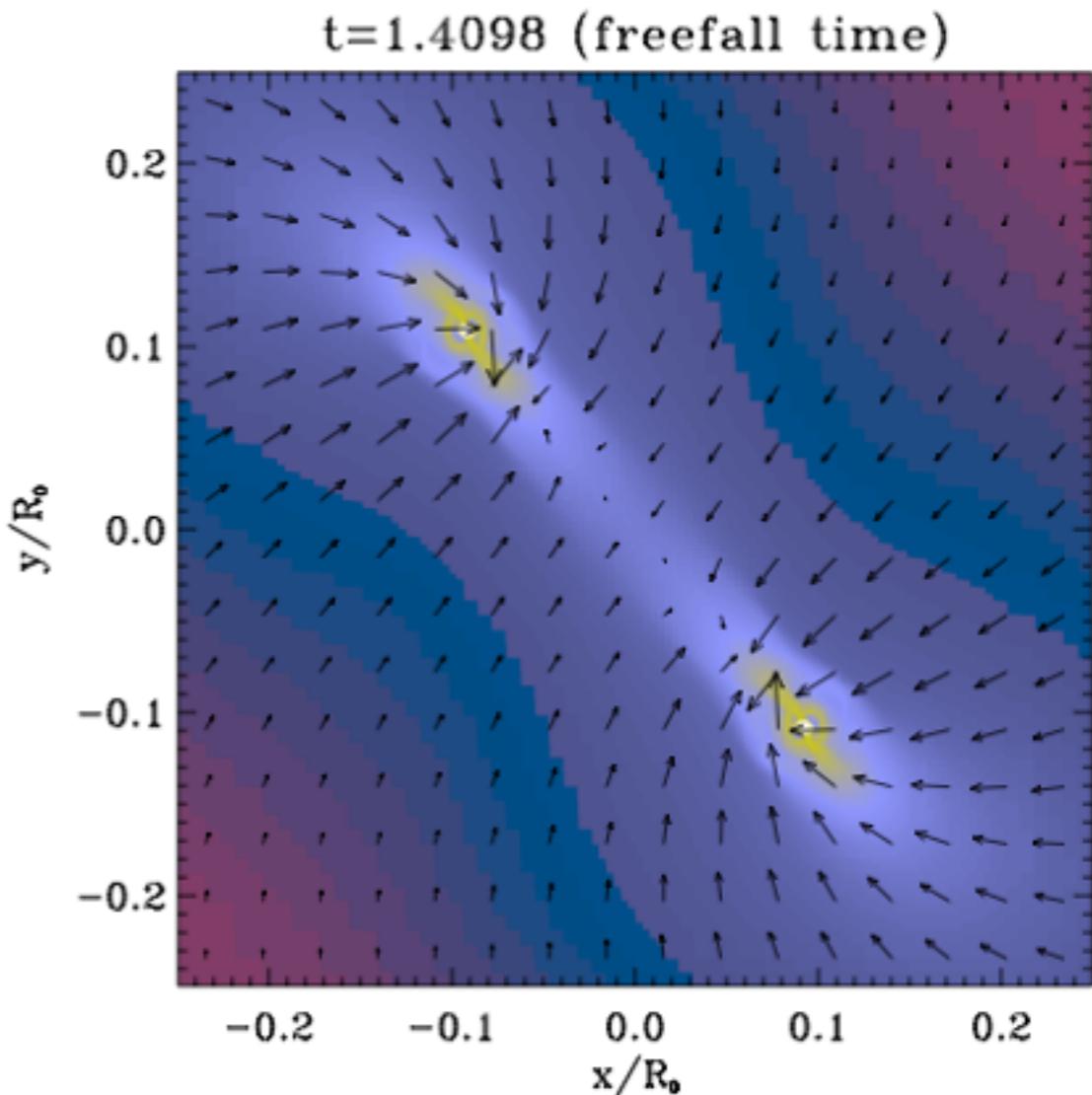
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  - ambipolar diffusion (*Tsukamoto et al. 2015, Wurster et al. 2016*)

# Solve the fragmentation crisis

---

- **Large scale fluctuations**  
(e.g. [Hennebelle & Teyssier 2008](#), [Price & Bate 2007](#))
  - ▶ could explain wide binaries

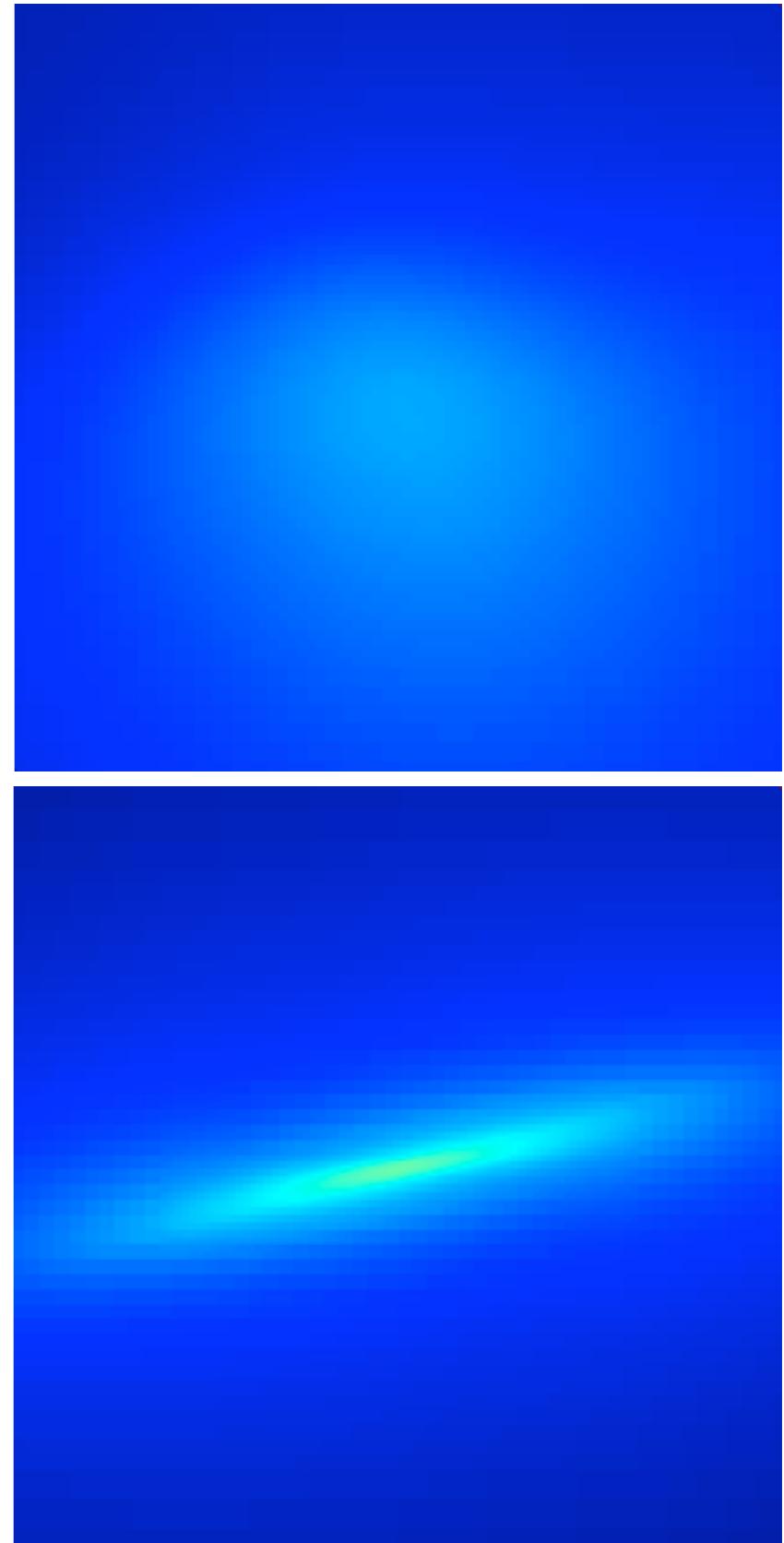
Amplitude perturbation  $A=0.5$



# Influence of misalignment

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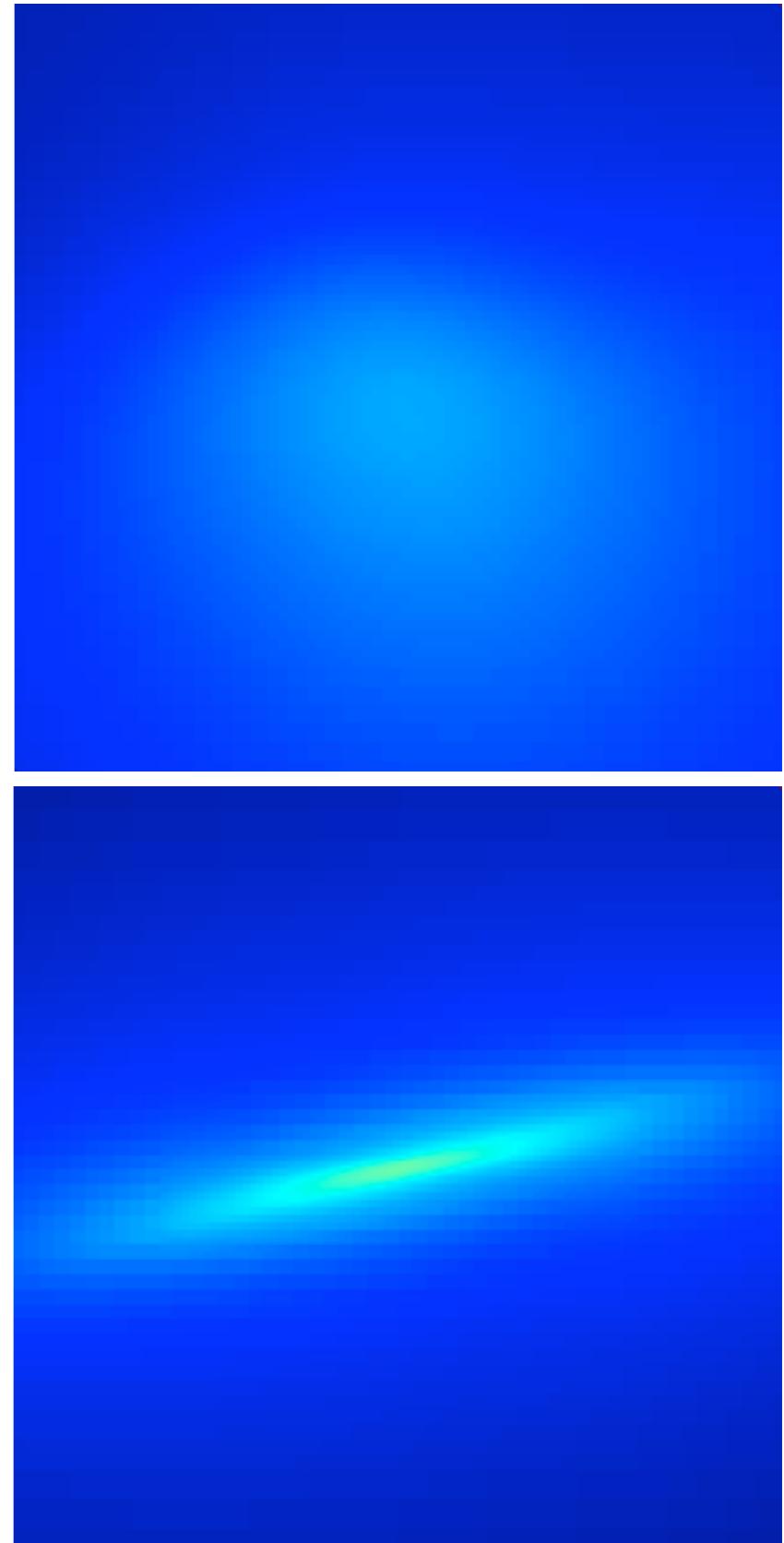
- Large scale fluctuations
- Angle B/rotation axis  
(Hennebelle & Ciardi 2009, Joos et al. 2012)



# Influence of misalignment

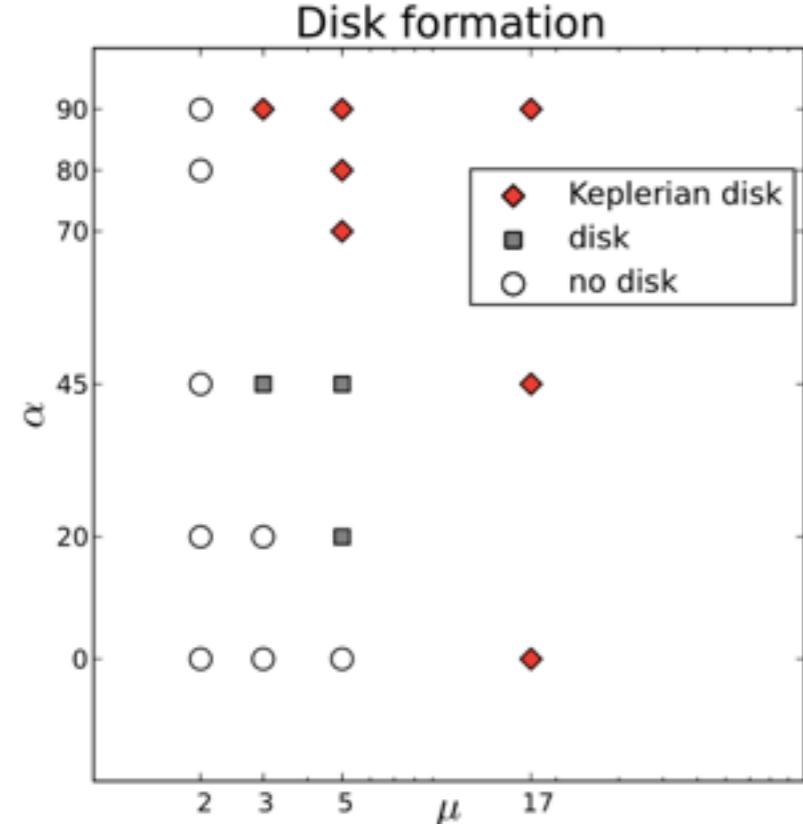
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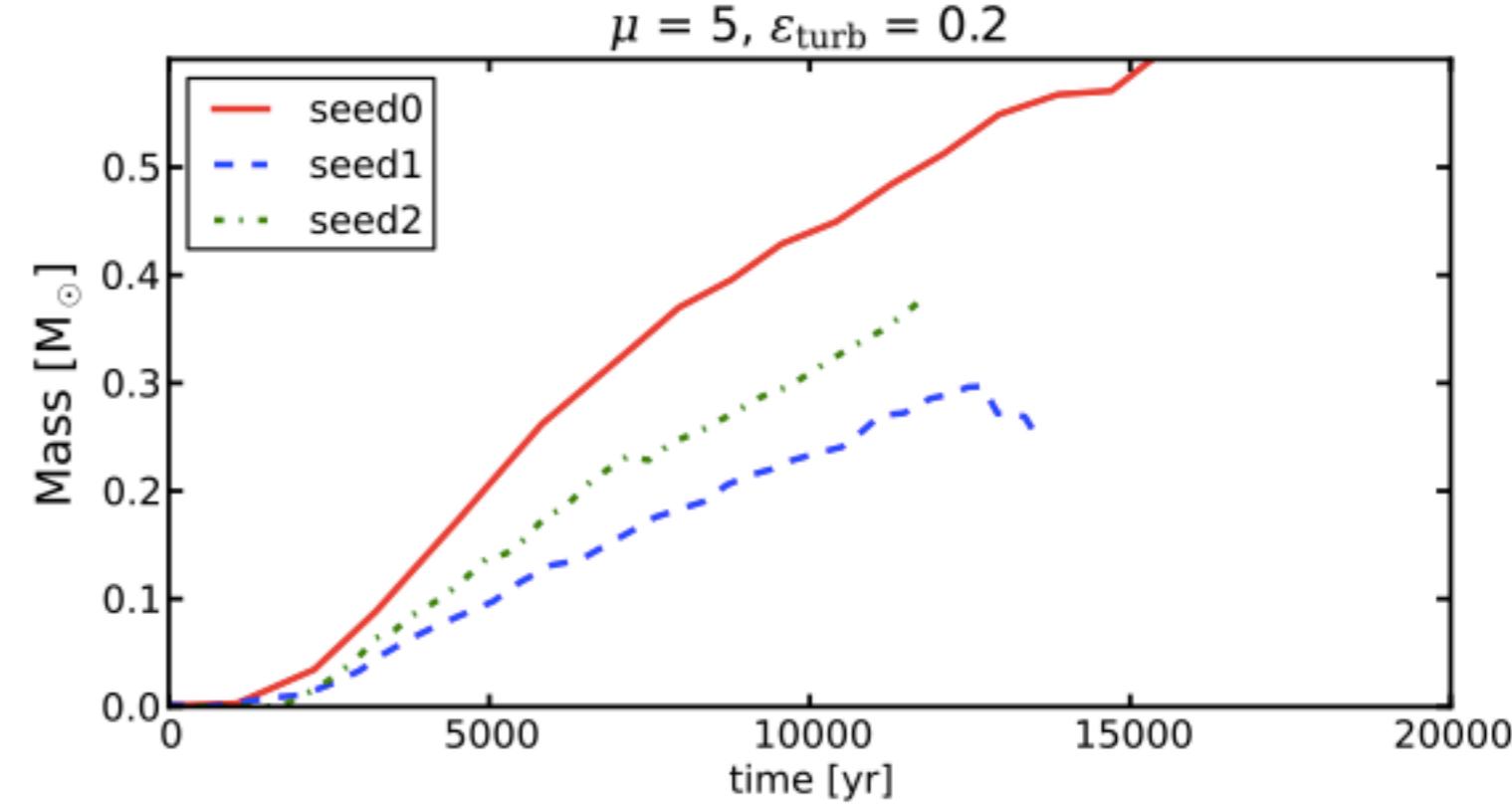


# Influence of turbulence and misalignment

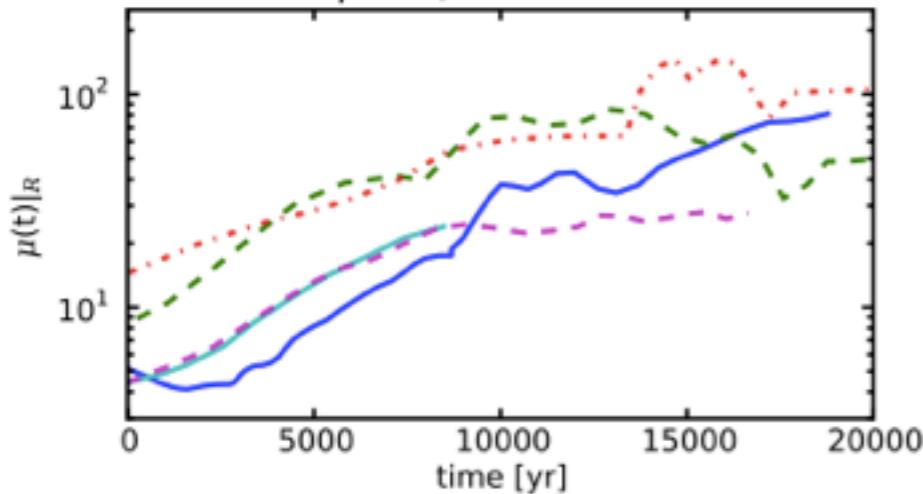
## Misalignment



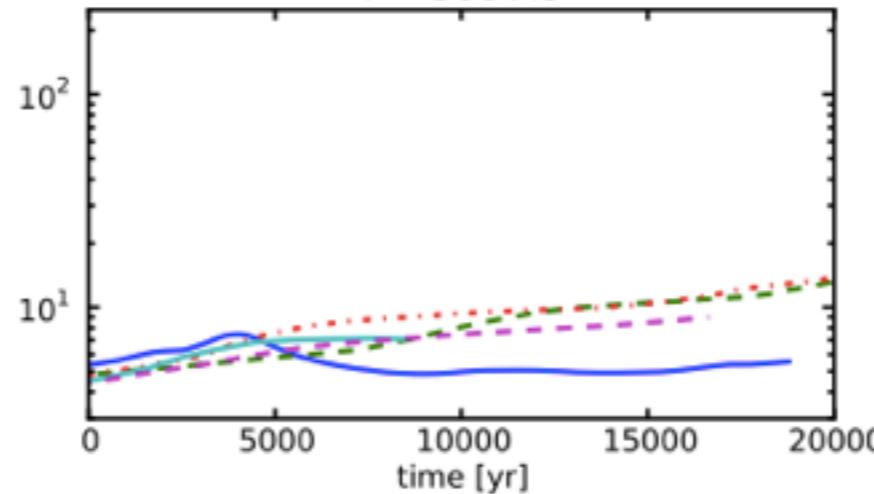
## Turbulence



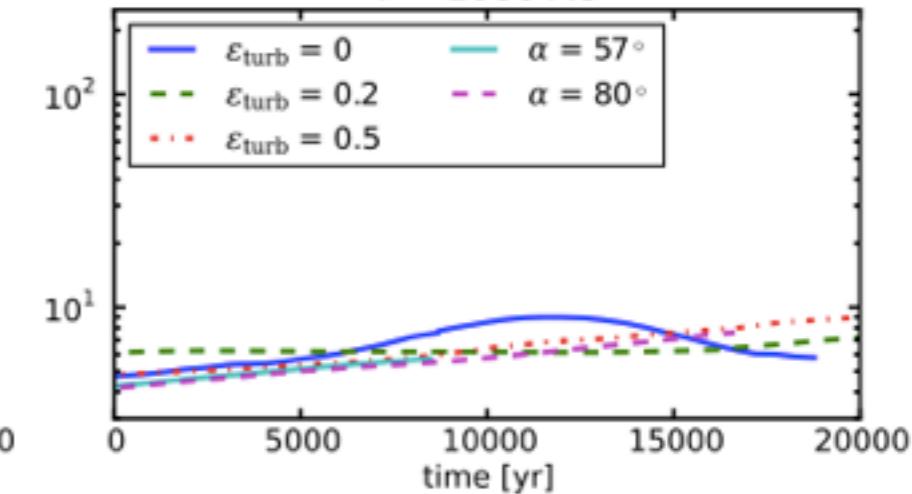
$\mu = 5, r < 100 \text{ AU}$



$r < 500 \text{ AU}$



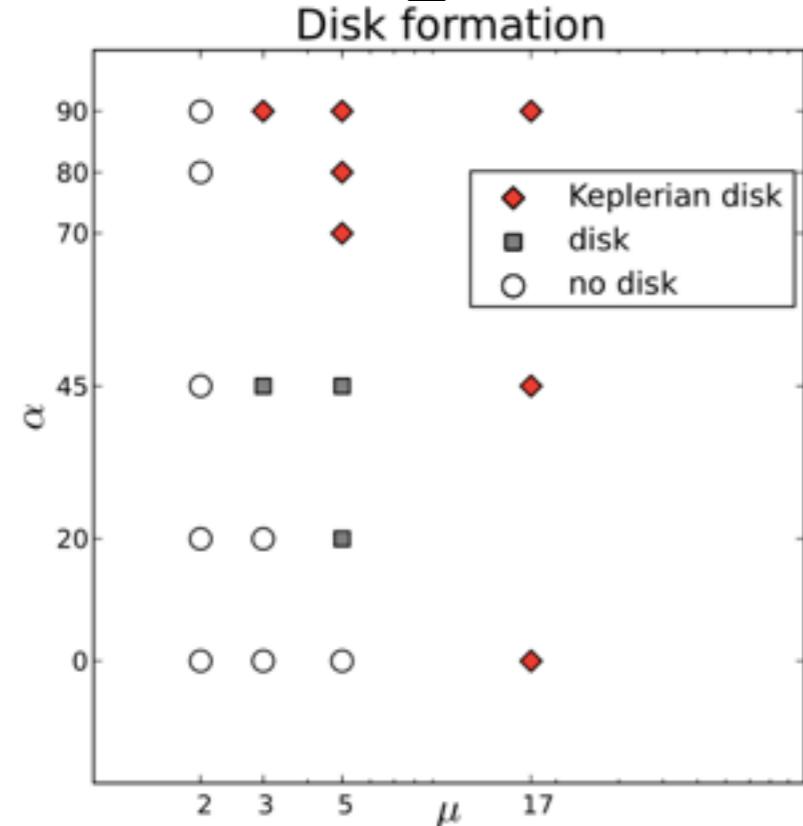
$r < 1000 \text{ AU}$



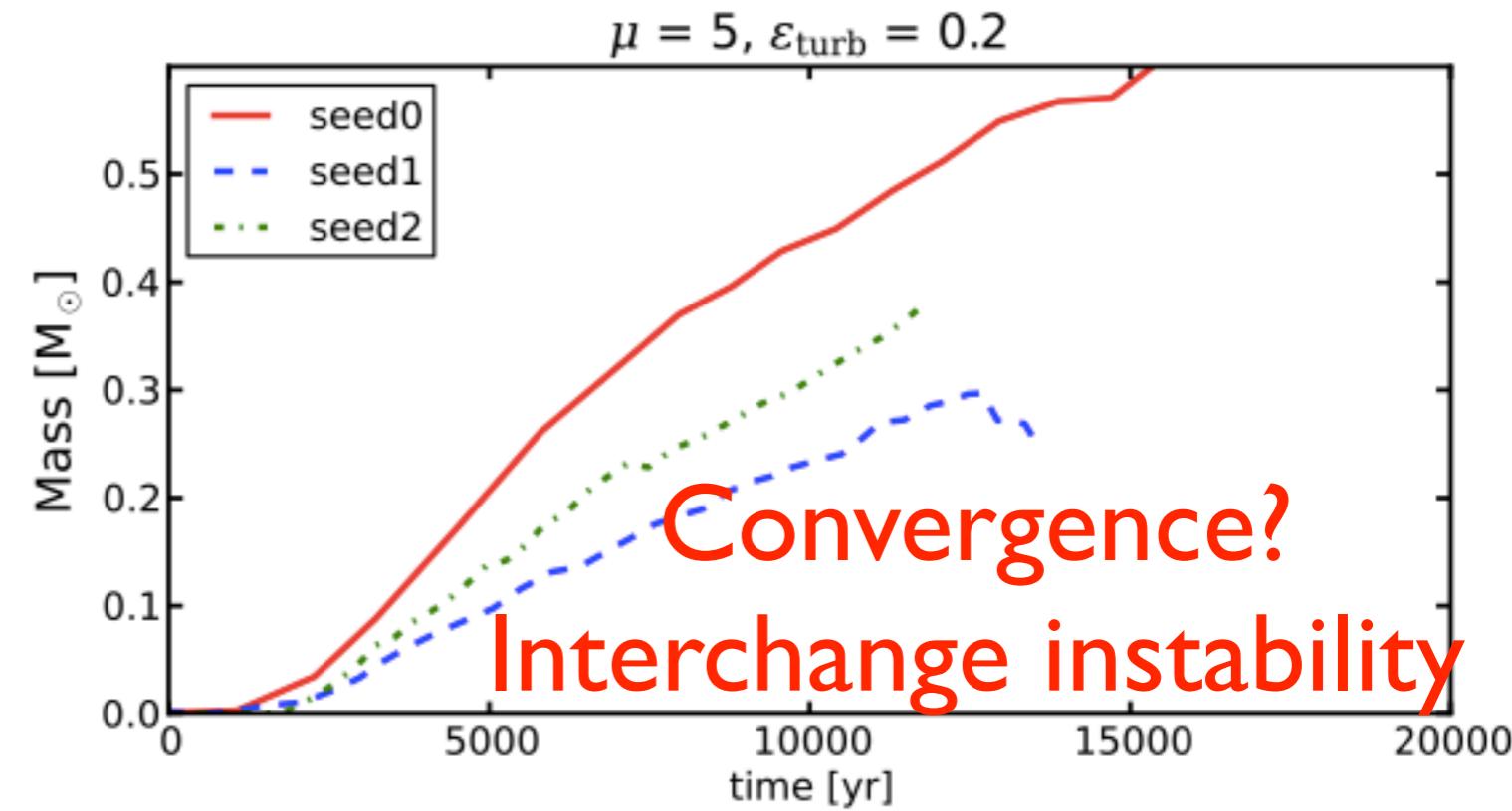
Joos et al. (2012, 2013)  
Ciardi & Hennebelle (2011)

# Influence of turbulence and misalignment

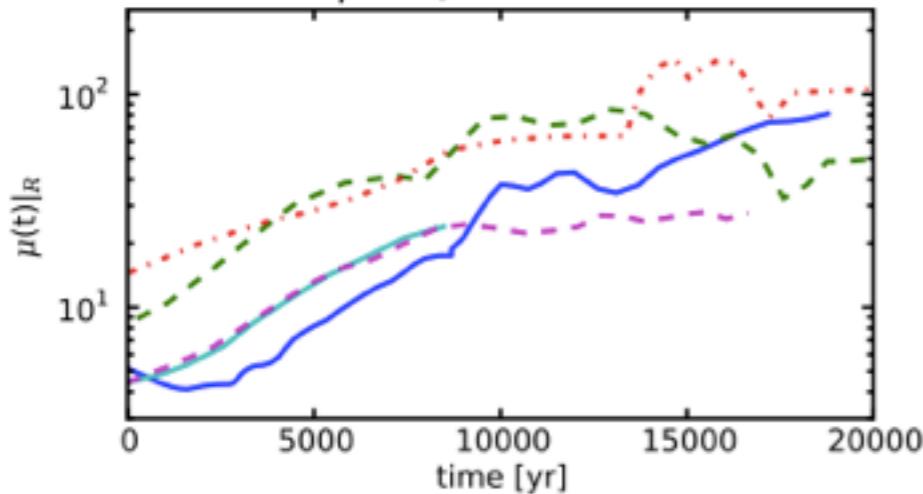
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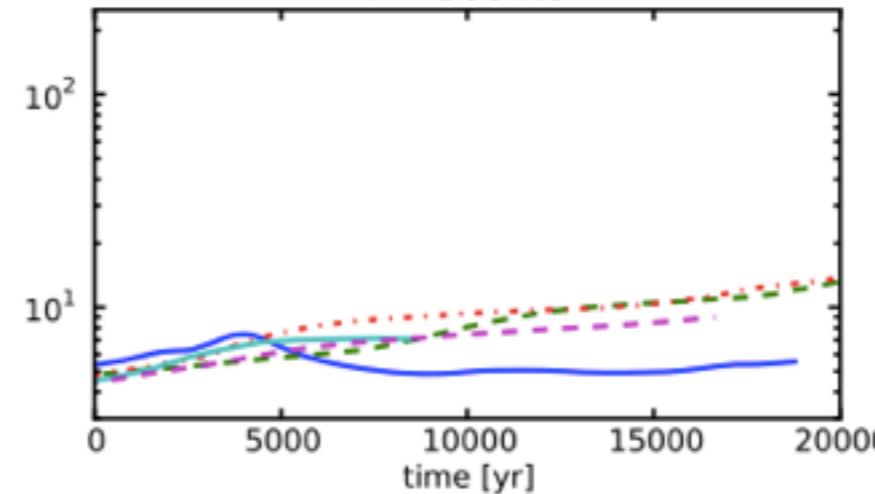
## Turbulence



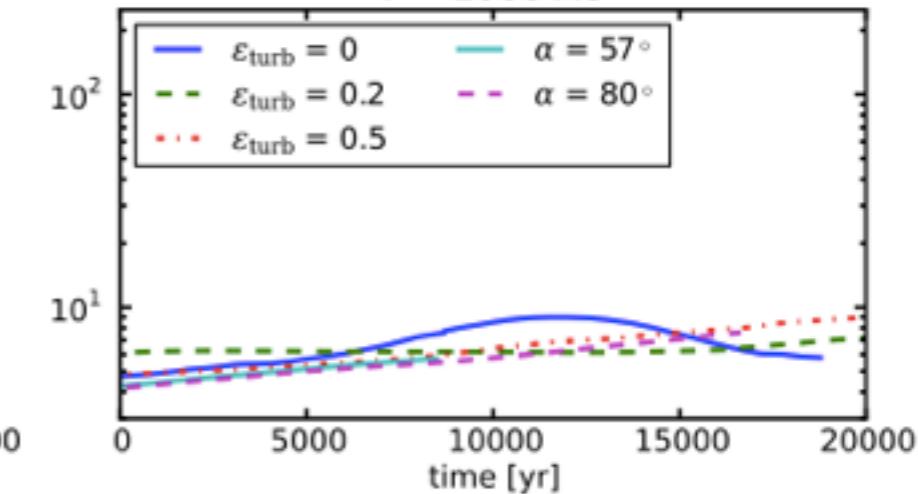
$\mu = 5, r < 100$  AU



$r < 500$  AU



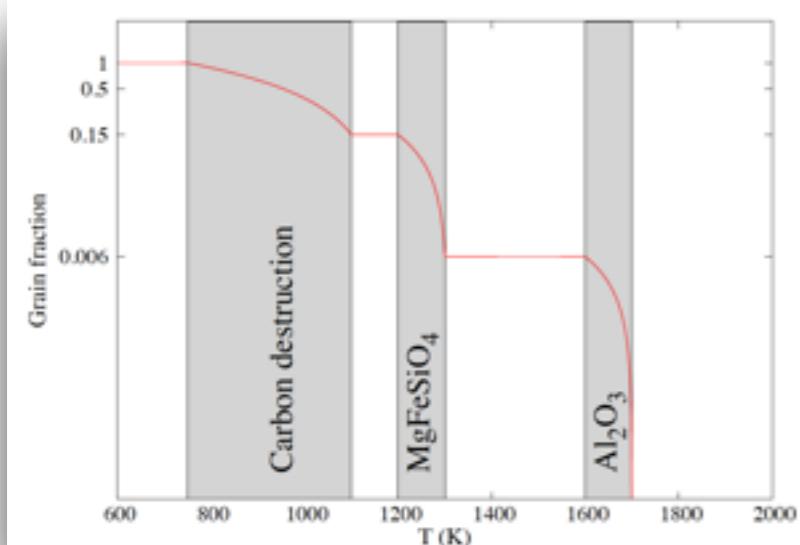
$r < 1000$  AU



# Equilibrium chemistry for non-ideal MHD

## ✓ Reduced chemical network dedicated for ionisation (based on the work by Umebayashi & Nakano 1990)

- H, He, C, O, metallic elements (Fe, Na, Mg, etc..)
- $H^+$ ,  $H_3^+$ ,  $He^+$ ,  $C^+$ , molecular and metallic ions
- bins in the dust grains size distribution ( $G$ ,  $G^+$ ,  $G^-$ )
- dust evaporation at  $T > 800$  K
- thermal ionisation of potassium ( $T > 1000$  K)
- neutral elements have constant abundances



- ✓ UMIST database for gas species (McElroy et al. 2013)
- ✓ Kunz & Mouschovias (2009) for interactions with and between grains

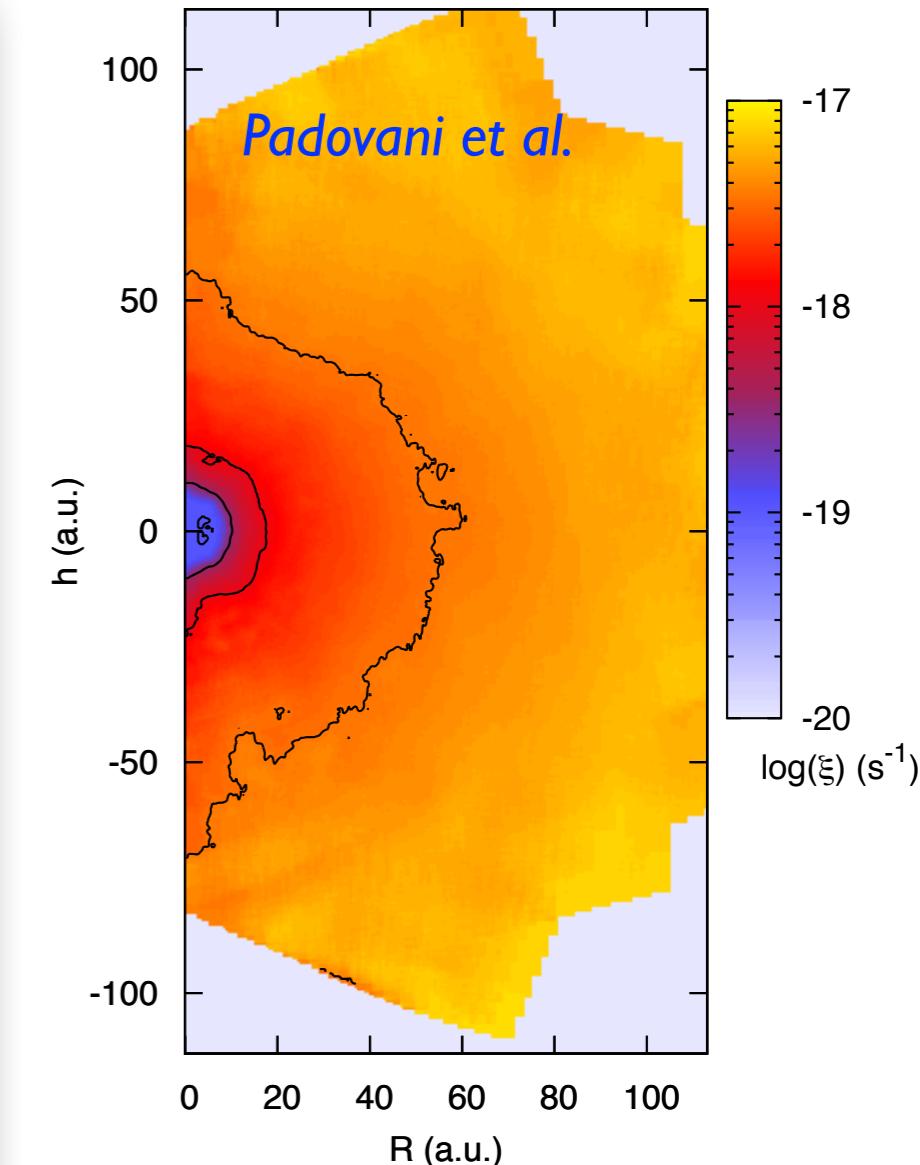
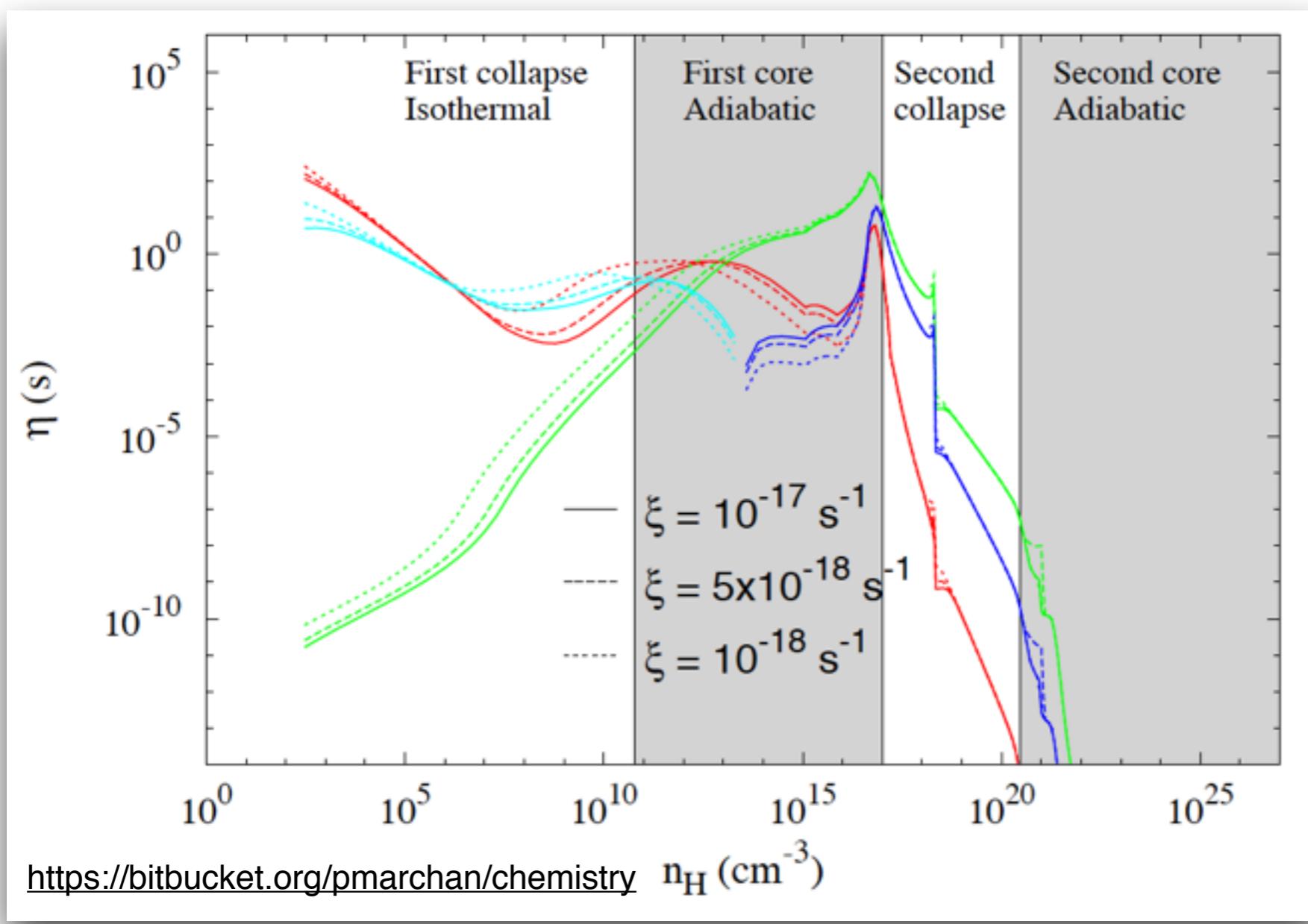
## ✓ Goal: compute a 3D table of abundances:

- depends on temperature, density and CR ionisation
- used on-the-fly in 3D calculations to compute resistivities

Reaction	$\alpha$	$\beta$	$\gamma$
$H^+ + O \rightarrow H + O^+$	$6.86 \times 10^{-10}$	0.26	0
$H^+ + O_2 \rightarrow H + O_2^+$	$2.00 \times 10^{-9}$	0.00	0
$H^+ + M \rightarrow H + M^+$	$1.10 \times 10^{-9}$	0.00	0
$He^+ + H_2 \rightarrow He + H^+ + H$	$3.70 \times 10^{-14}$	0.00	35
$He^+ + CO \rightarrow He + C^+ + O$	$1.60 \times 10^{-9}$	0.00	0
$He^+ + O_2 \rightarrow He + O^+ + O$	$1.10 \times 10^{-9}$	0.00	0
$H_3^+ + CO \rightarrow H_2 + HCO^+$	$1.36 \times 10^{-9}$	-0.14	0
$H_3^+ + O \rightarrow H_2 + OH^+$	$7.98 \times 10^{-10}$	-0.16	0
$H_3^+ + O_2 \rightarrow H_2 + O_2H^+$	$9.30 \times 10^{-10}$	0.00	0
$H_3^+ + M \rightarrow H_2 + H + M^+$	$1.10 \times 10^{-9}$	0.00	0
$C^+ + H_2 \rightarrow CH_2^+ + h\nu$	$2.00 \times 10^{-16}$	0.00	0
$C^+ + O_2 \rightarrow CO^+ + O$	$3.42 \times 10^{-10}$	0.00	0
$C^+ + O_2 \rightarrow CO + O^+$	$4.54 \times 10^{-10}$	0.00	0
$C^+ + M \rightarrow C + M^+$	$1.10 \times 10^{-9}$	0.00	0
$m^+ + M \rightarrow m + M^+$	$2.90 \times 10^{-9}$	0.00	0
$H^+ + e^- \rightarrow H + h\nu$	$3.50 \times 10^{-12}$	-0.75	0
$He^+ + e^- \rightarrow He + h\nu$	$5.36 \times 10^{-12}$	-0.5	0
$H_3^+ + e^- \rightarrow H + H + H$	$2.34 \times 10^{-8}$	-0.52	0
$H_3^+ + e^- \rightarrow H_2 + H$			
$C^+ + e^- \rightarrow C + h\nu$	$2.36 \times 10^{-12}$	-0.29	0
$m^+ + e^- \rightarrow m_1 + m_2$	$2.40 \times 10^{-7}$	-0.69	0
$M^+ + e^- \rightarrow M + h\nu$	$2.78 \times 10^{-12}$	-0.68	0
$H_2 \rightarrow H_2^+ + e^-$		$1.2 \times 10^{-17}$	
$H_2 \rightarrow H^+ + H + e^-$		$2.86 \times 10^{-19}$	
$He \rightarrow He^+ + e^-$		$6.58 \times 10^{-18}$	

Marchand et al. (2016)

# Equilibrium chemistry for non-ideal MHD: results



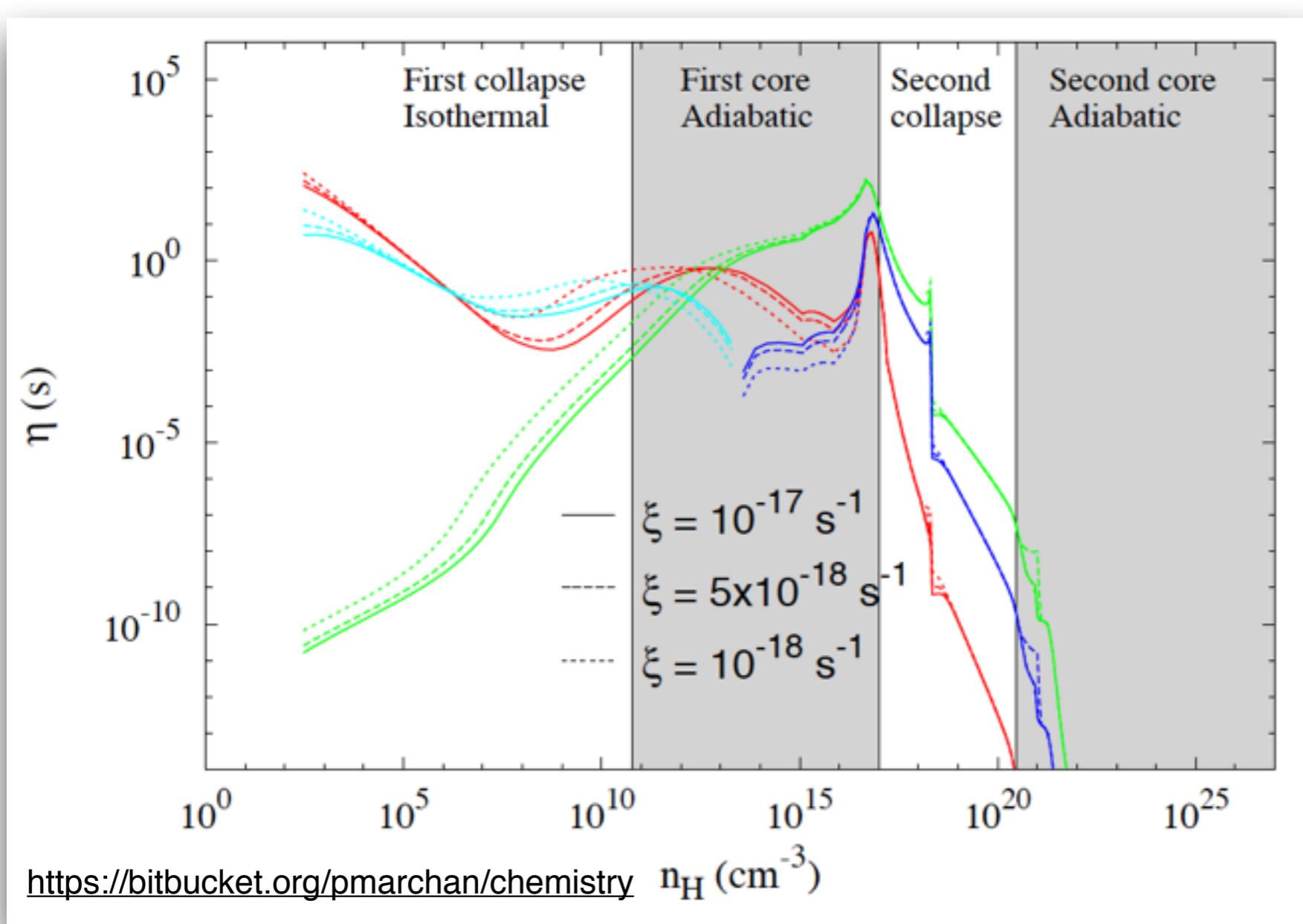
*CR ionisation rate in  
the core interior*

1/ **Grain** is the most important parameter

2/ Needs at least 20 bins in dust grain size distribution to converge...

*Marchand et al. (2016)*

# Equilibrium chemistry for non-ideal MHD: results



$$\eta_{\Omega} = \frac{1}{\sigma_{\parallel}},$$
$$\eta_{\text{H}} = \frac{\sigma_{\text{H}}}{\sigma_{\perp}^2 + \sigma_{\text{H}}^2},$$
$$\eta_{\text{AD}} = \frac{\sigma_{\perp}}{\sigma_{\perp}^2 + \sigma_{\text{H}}^2} - \frac{1}{\sigma_{\parallel}},$$

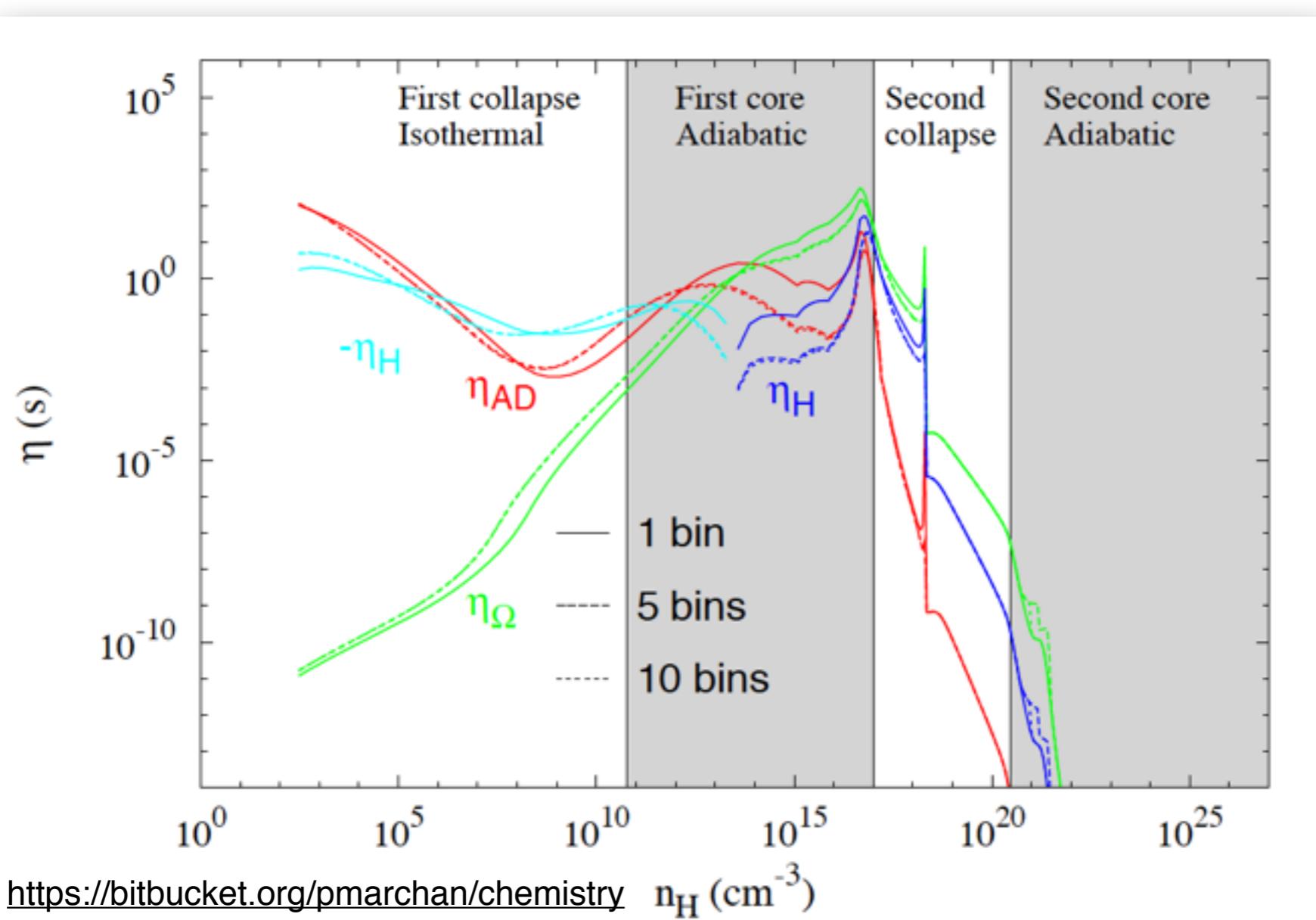
$$\sigma_{\parallel} = \sum_i \sigma_i,$$
$$\sigma_{\perp} = \sum_i \frac{\sigma_i}{1 + (\omega_i \tau_{in})^2},$$
$$\sigma_{\text{H}} = - \sum_i \frac{\sigma_i \omega_i \tau_{in}}{1 + (\omega_i \tau_{in})^2}.$$

1/ **Grain** is the most important parameter

2/ Needs at least 20 bins in dust grain size distribution to converge...

*Marchand et al. (2016)*

# Equilibrium chemistry for non-ideal MHD: results



1/ **Grain** is the most important parameter

2/ Needs at least 10 bins in dust grain size distribution to converge...

$$\eta_\Omega = \frac{1}{\sigma_{\parallel}},$$
$$\eta_H = \frac{\sigma_H}{\sigma_{\perp}^2 + \sigma_H^2},$$
$$\eta_{AD} = \frac{\sigma_{\perp}}{\sigma_{\perp}^2 + \sigma_H^2} - \frac{1}{\sigma_{\parallel}},$$

$$\sigma_{\parallel} = \sum_i \sigma_i,$$
$$\sigma_{\perp} = \sum_i \frac{\sigma_i}{1 + (\omega_i \tau_{in})^2},$$
$$\sigma_H = - \sum_i \frac{\sigma_i \omega_i \tau_{in}}{1 + (\omega_i \tau_{in})^2}.$$

Applications: effect of ambipolar diffusion

# Generalised Ohm's law

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B})$$

$$-\eta_\Omega(\nabla \times \mathbf{B}) \quad \text{Ohmic diffusion}$$

$$-\eta_H \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\} \quad \text{Hall effect}$$

# Hall effect

$$-\eta_{AD} \frac{\mathbf{B}}{B} \times \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\} \quad \text{ambipolar diffusion}$$

# Applications: effect of ambipolar diffusion

---

## Generalised Ohm's law

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left[ \mathbf{v} \times \mathbf{B} - \eta_{\Omega} (\nabla \times \mathbf{B}) - \eta_H \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\} - \eta_{AD} \frac{\mathbf{B}}{B} \times \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\} \right]$$

Ohmic diffusion      Hall effect      ambipolar diffusion

# Applications: effect of ambipolar diffusion

## Generalised Ohm's law

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \left[ \mathbf{v} \times \mathbf{B} \right]$$

$$- \eta_\Omega (\nabla \times \mathbf{B})$$

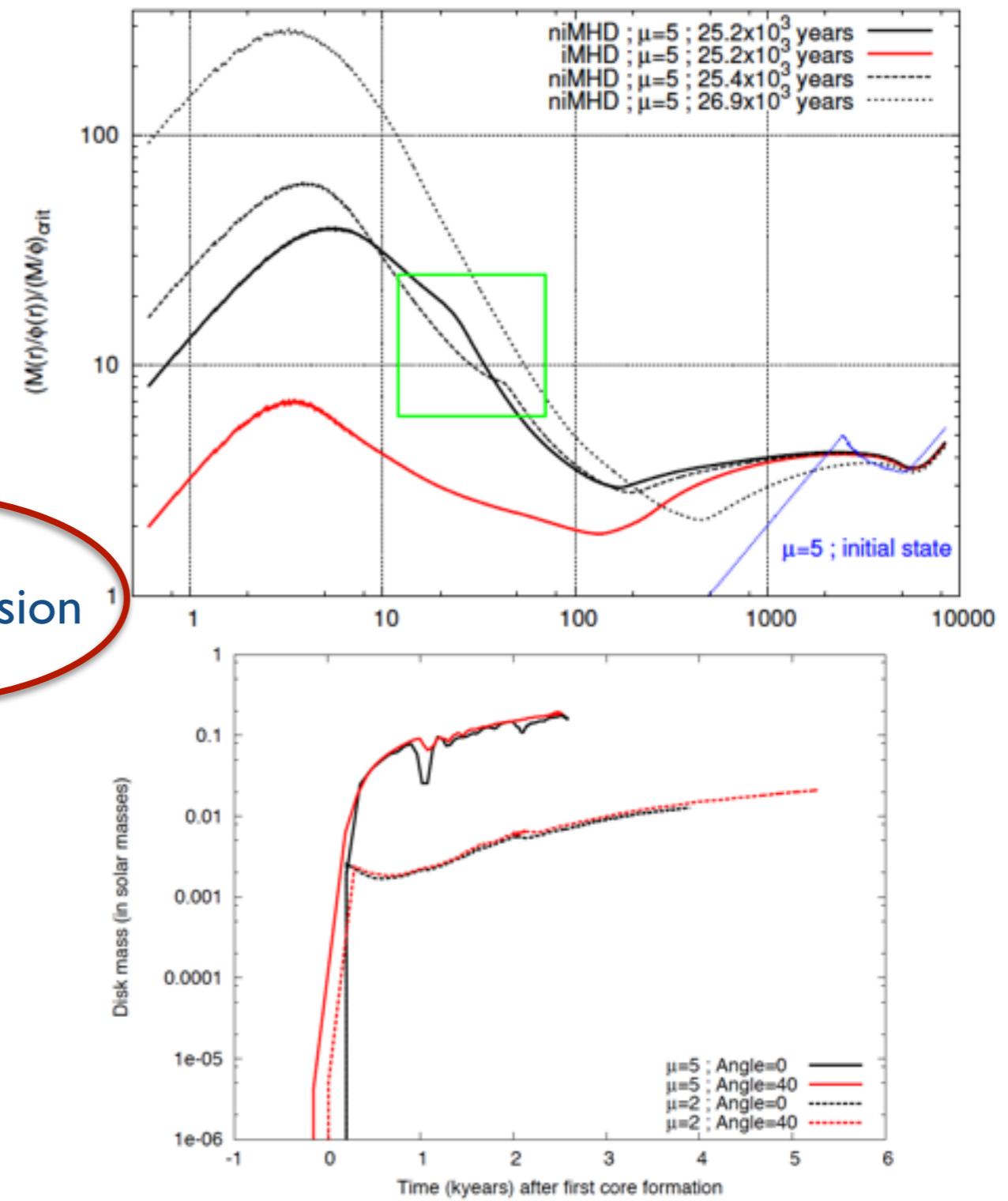
$$- \eta_H \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\}$$

$$- \eta_{AD} \frac{\mathbf{B}}{B} \times \left\{ (\nabla \times \mathbf{B}) \times \frac{\mathbf{B}}{B} \right\}$$

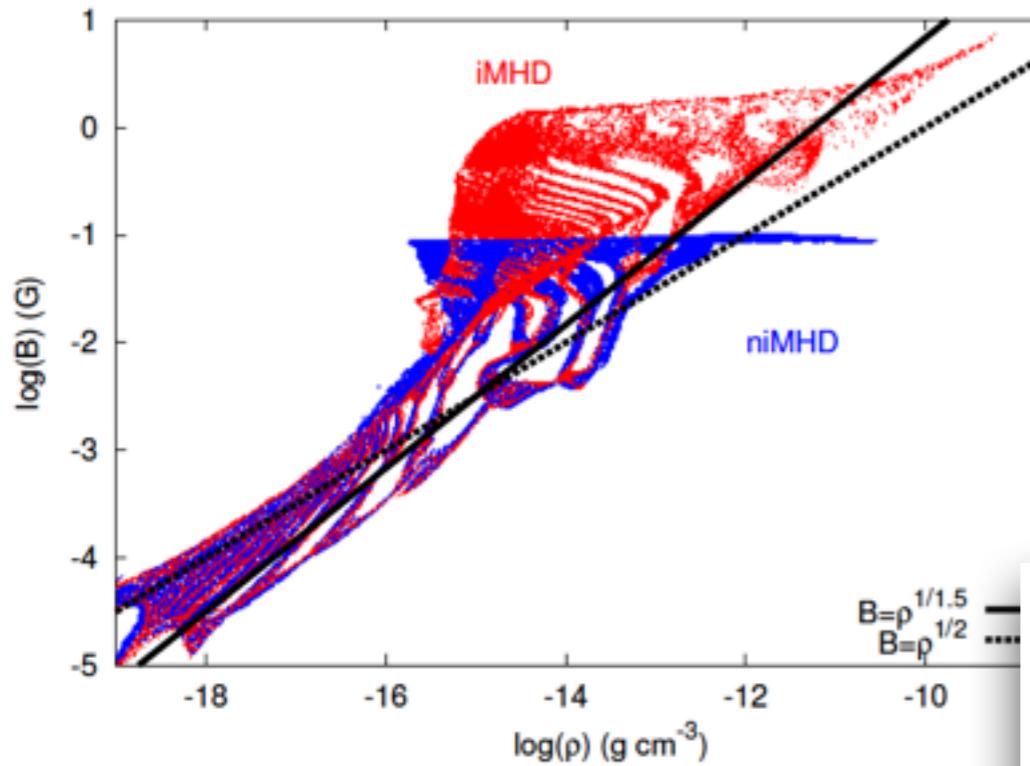
Ohmic diffusion

Hall effect

ambipolar diffusion



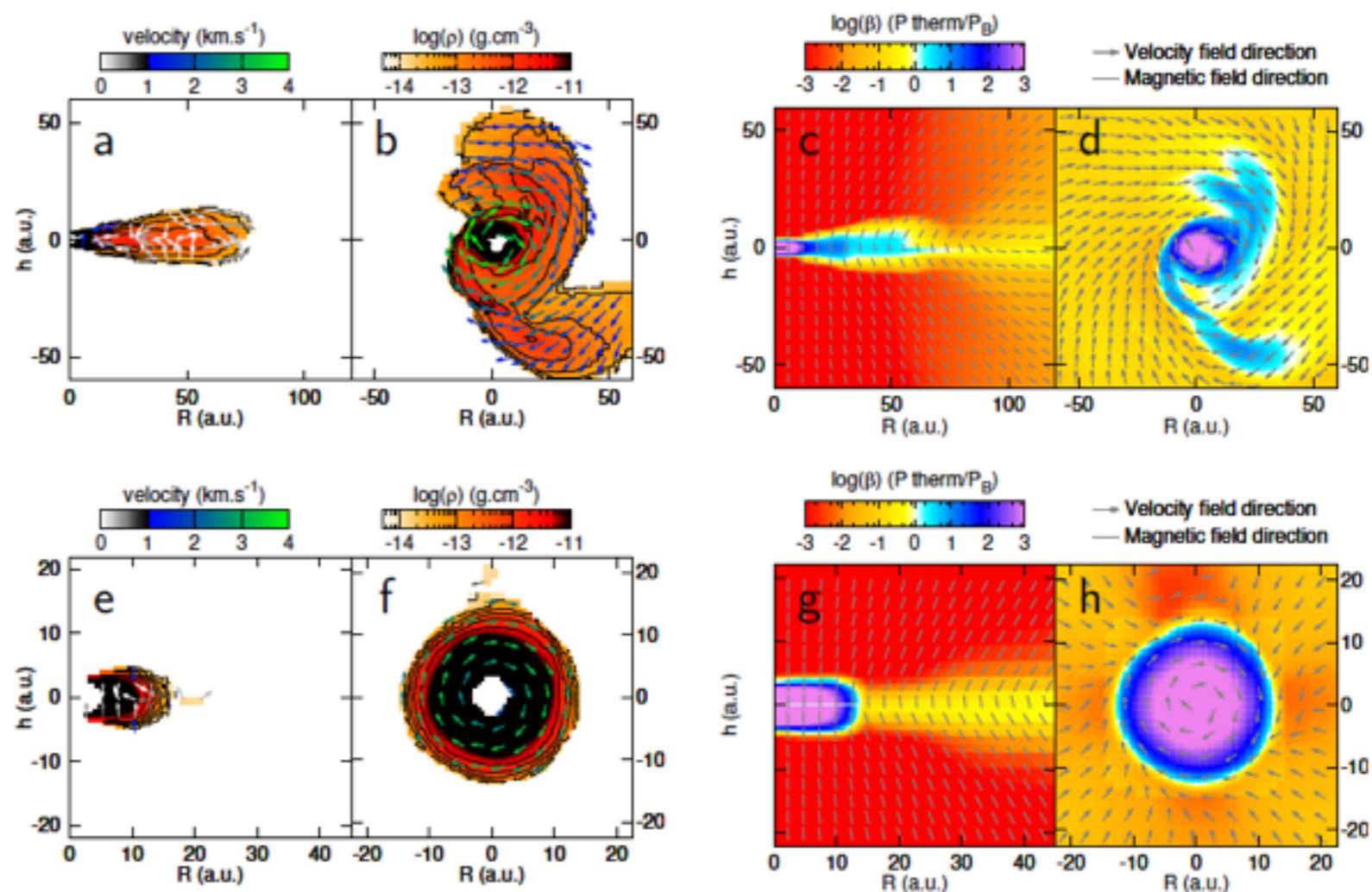
# Applications: effect of ambipolar diffusion



- Rotationally supported disc formation ( $R \sim 50$  AU) - consistent with obs.
- disc size **depends** on misalignment
- $P_{\text{therm}}/P_{\text{mag}} > 1$  within discs
- **poloidal** magnetic field  
 $\Rightarrow$  initial conditions for protoplanetary discs studies

*Masson et al. 2016*

- formation of a **plateau** at  $B \sim 0.1$  G
- **reorganisation** of magnetic field lines (essentially **poloidal**)  
 $\Rightarrow$  **reduced magnetic braking**
- mass and radius of first core do not change
- **weaker outflows** compared to ideal MHD

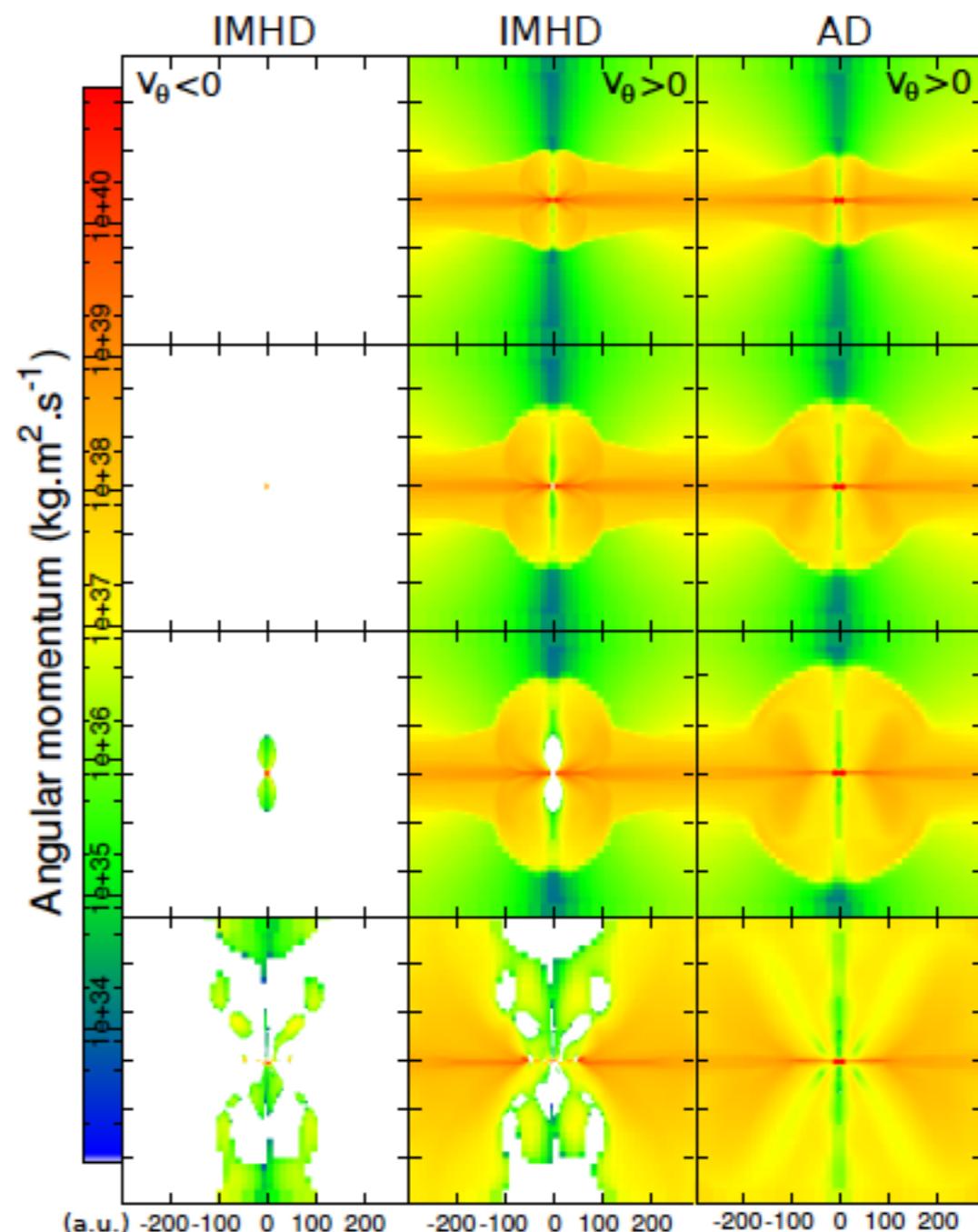


# Influence of non-ideal MHD

---

## Rotation and interchange instability

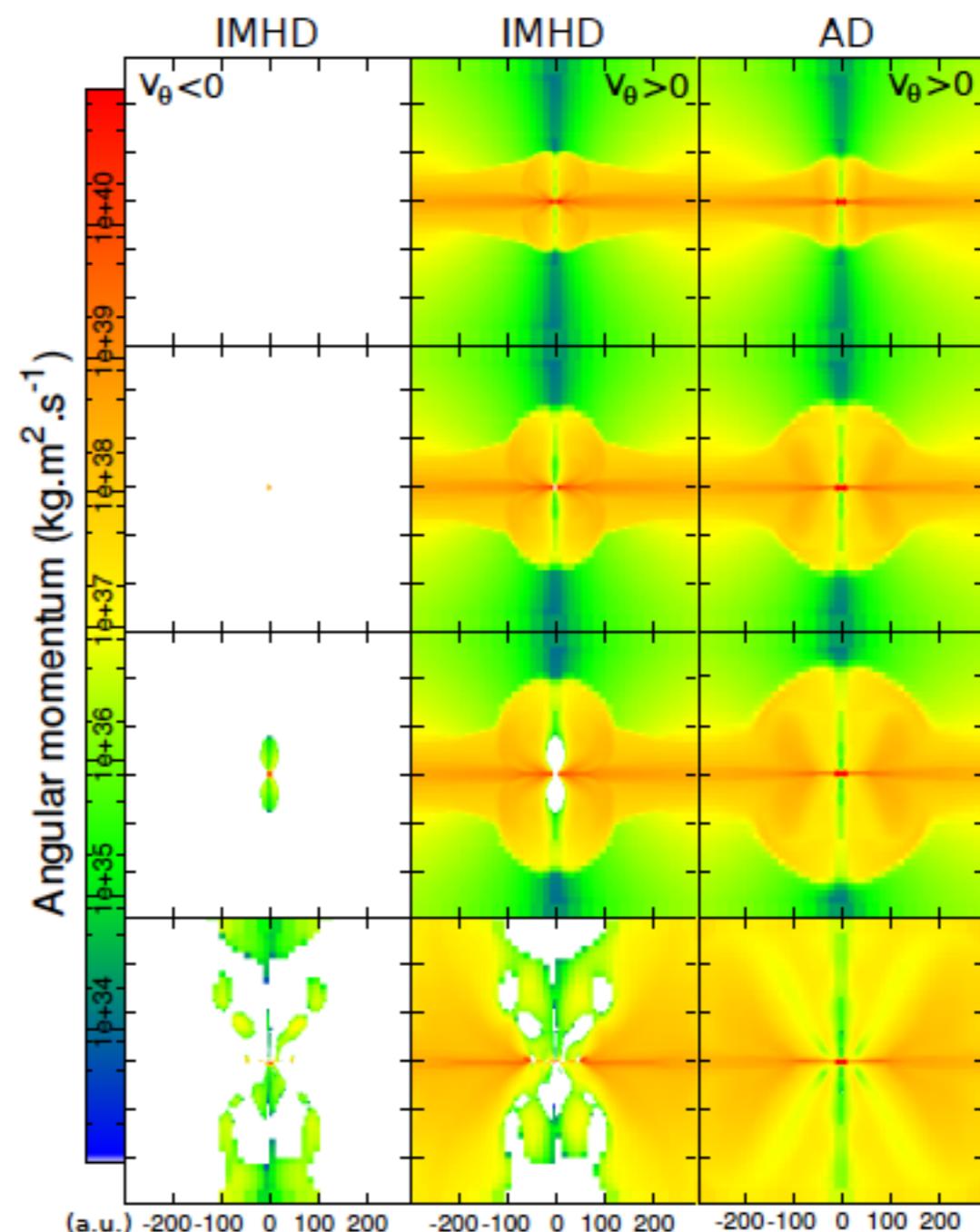
- reduce magnetic braking  
(suppress counter-rotation found in ideal MHD)



# Influence of non-ideal MHD

## Rotation and interchange instability

- reduce magnetic braking  
(suppress counter-rotation found in ideal MHD)



# Influence of non-ideal MHD

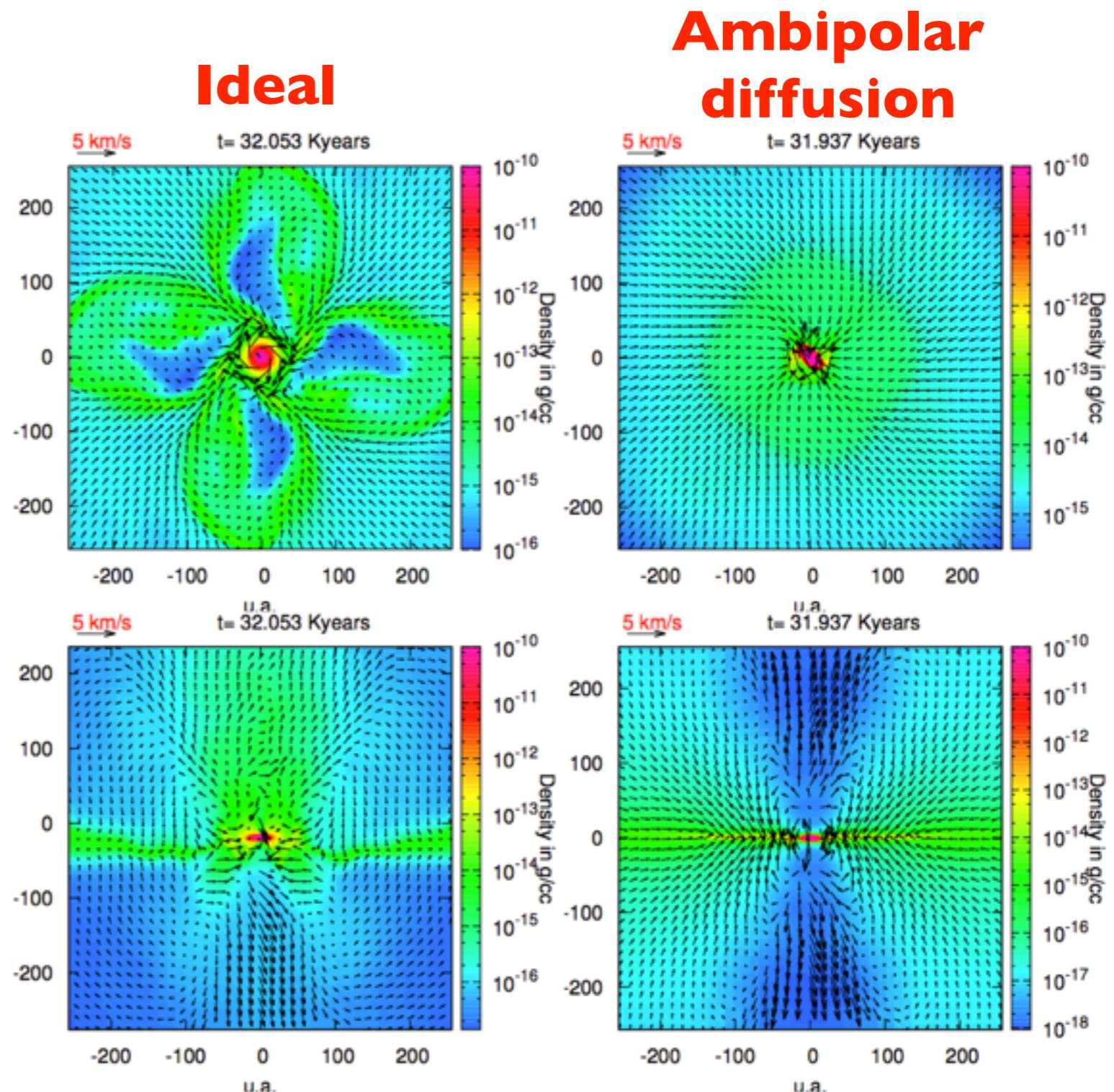
## Disc formation and interchange instability

- reduce magnetic braking  
(suppress counter-rotation found in ideal MHD)

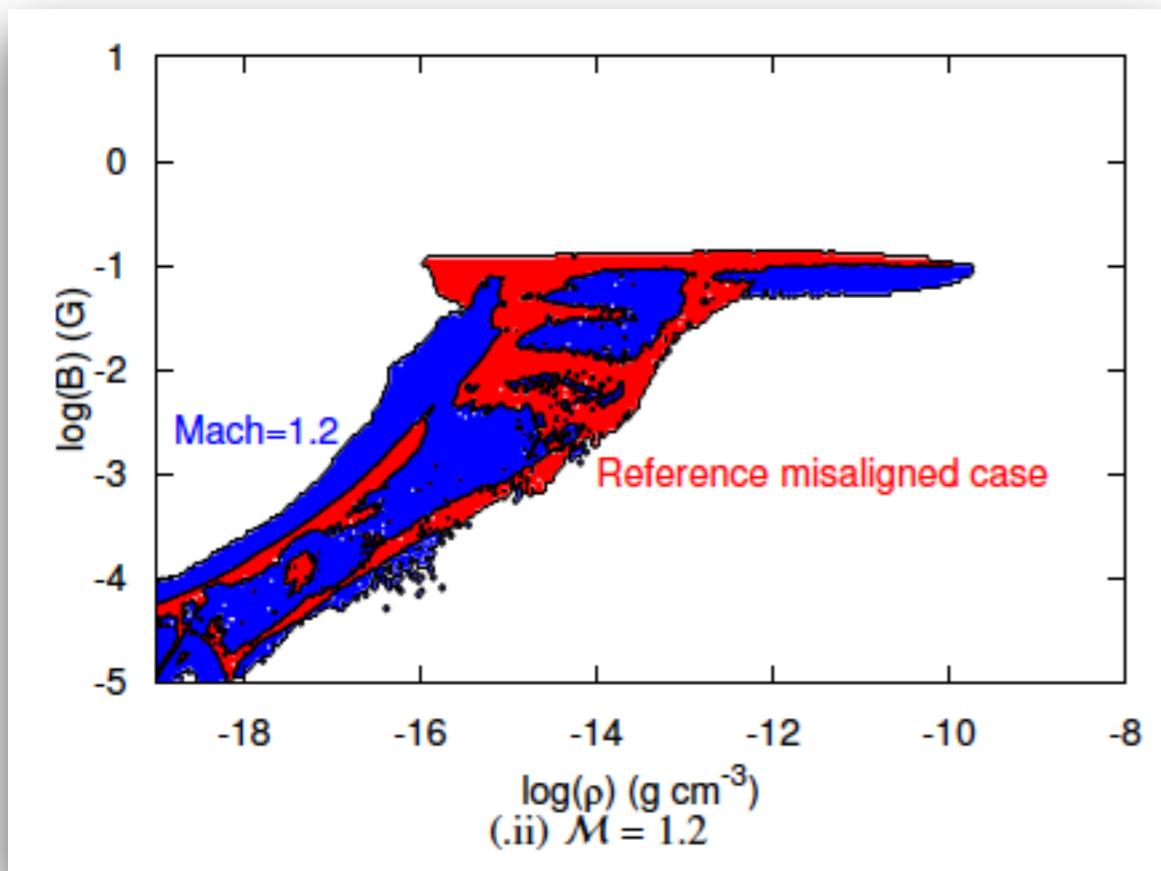
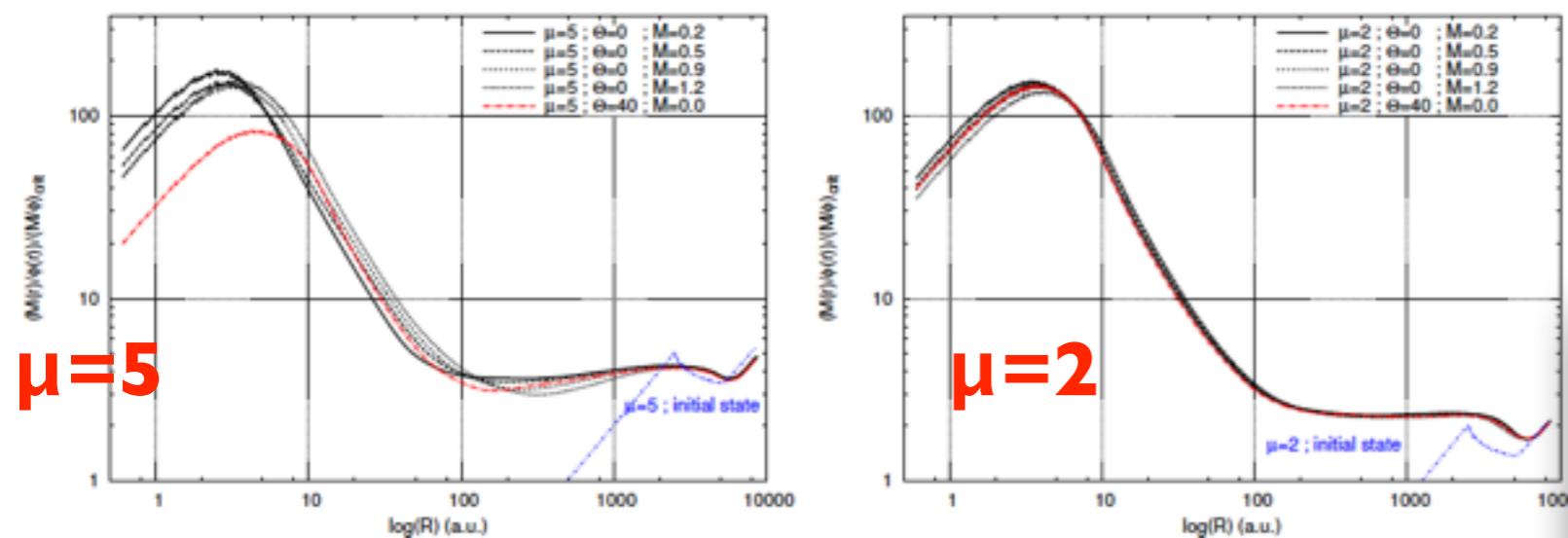
- similar qualitative results in the turbulent case

but

- magnetic pressure is greatly reduced in the disc with AD
- changes at the first core scale
- diffusion is \*controlled\*

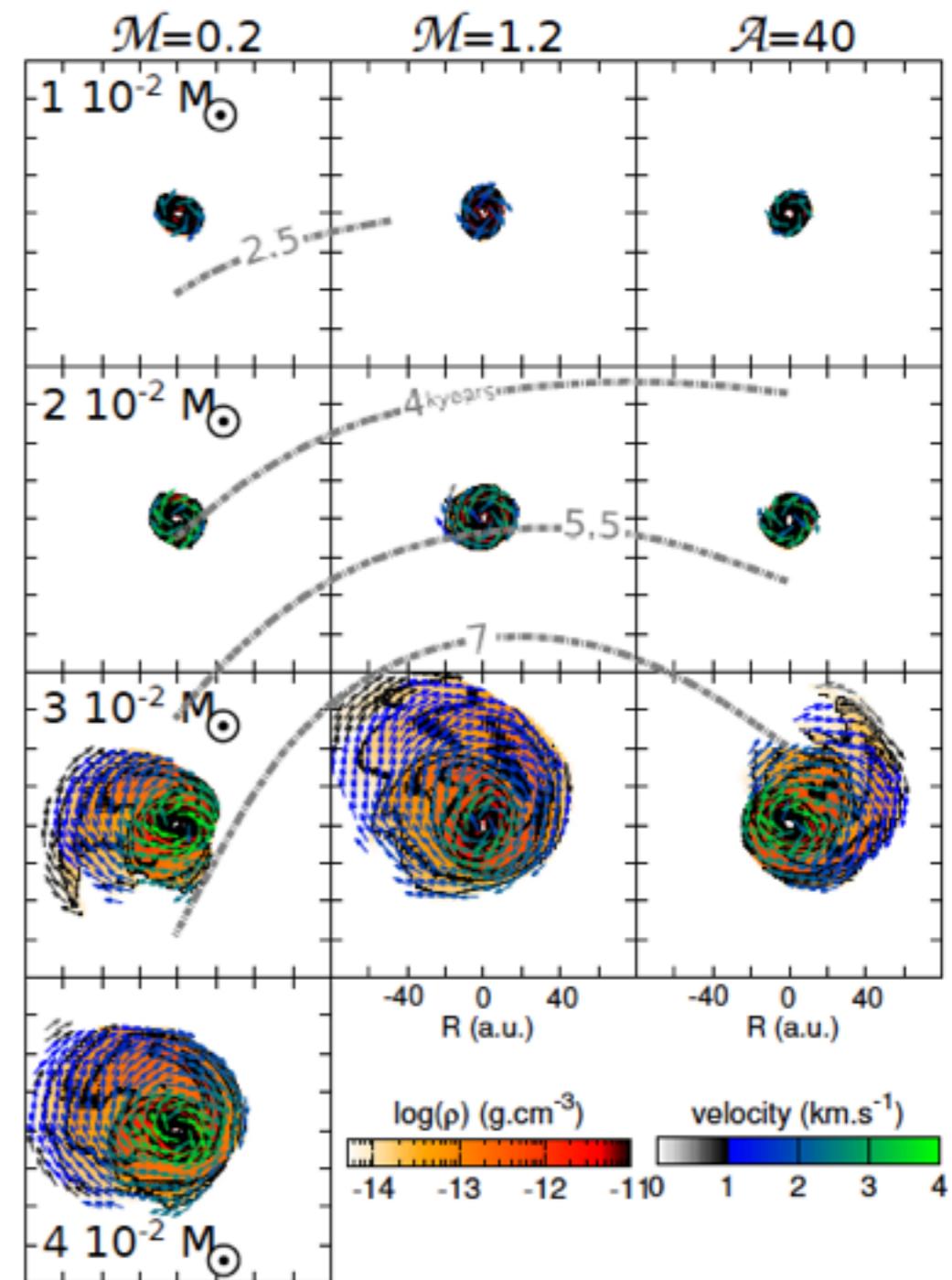


# Turbulence & ambipolar diffusion

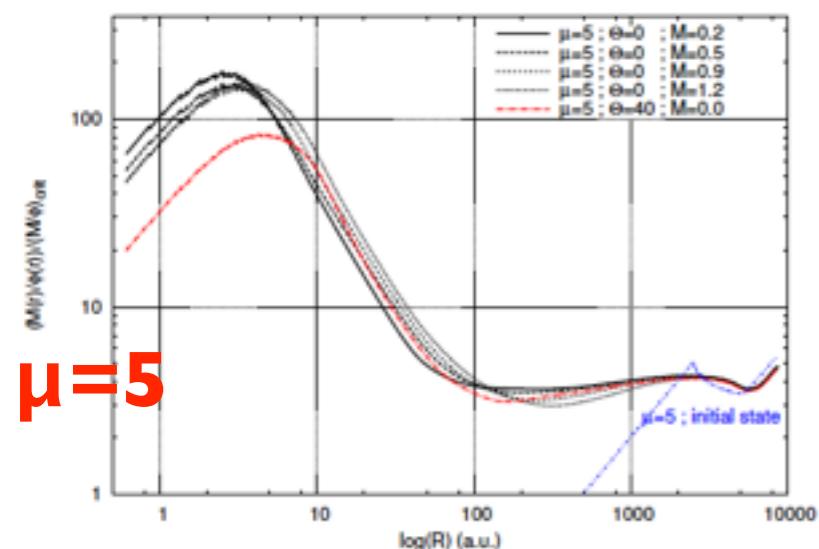


Masson et al. in prep.

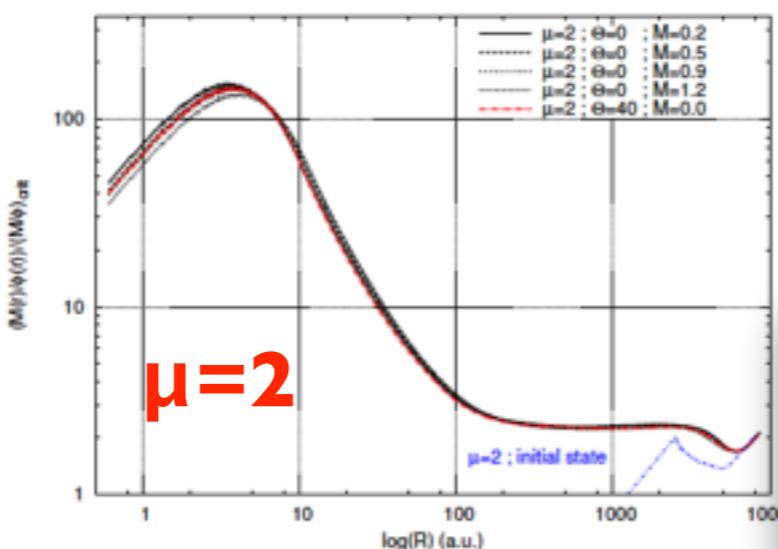
- disc size **does not depend** on turbulence level  
=> combination between turbulent diffusion and ambipolar diffusion?



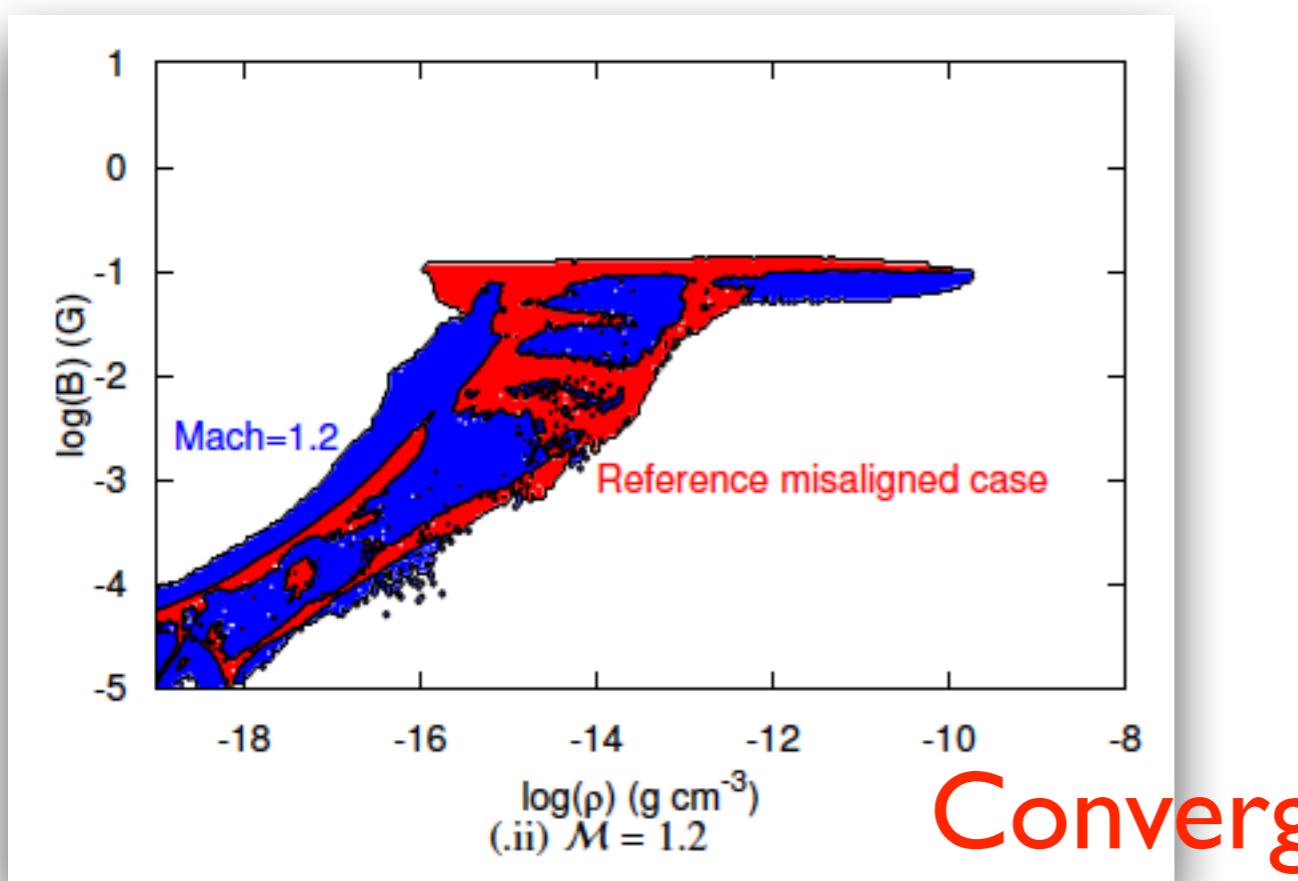
# Turbulence & ambipolar diffusion



**μ=5**



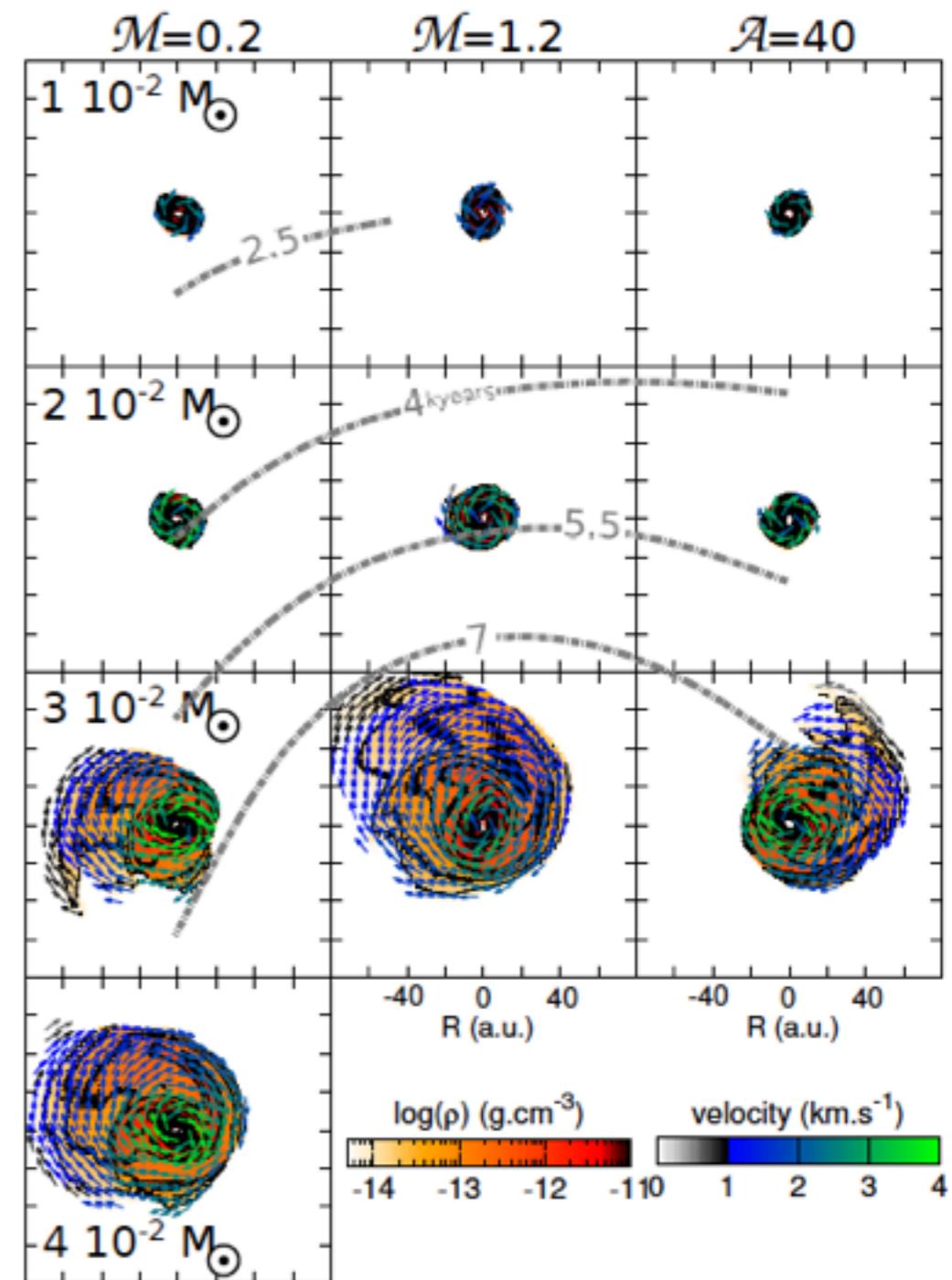
**μ=2**



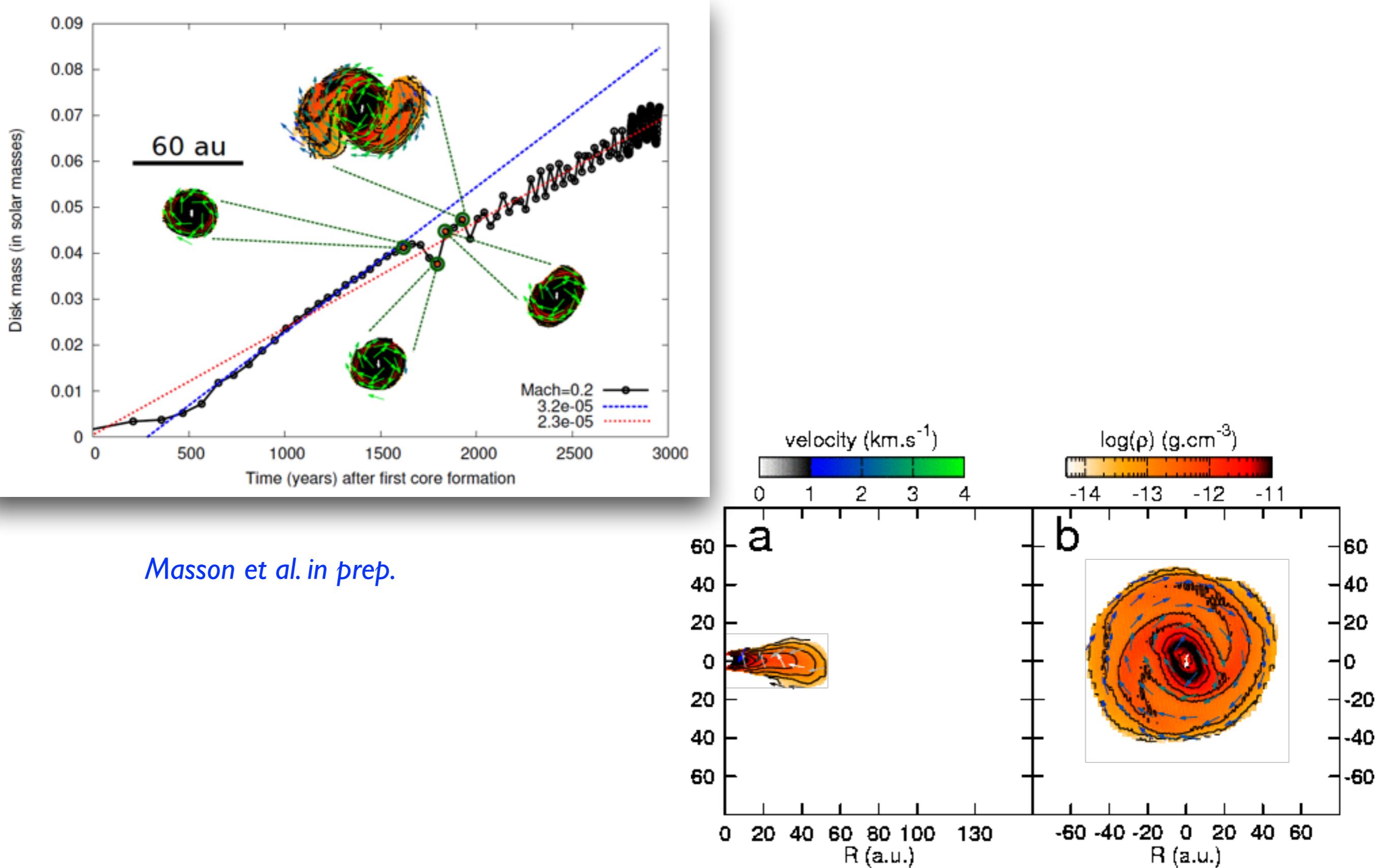
**Convergence!**

Masson et al. in prep.

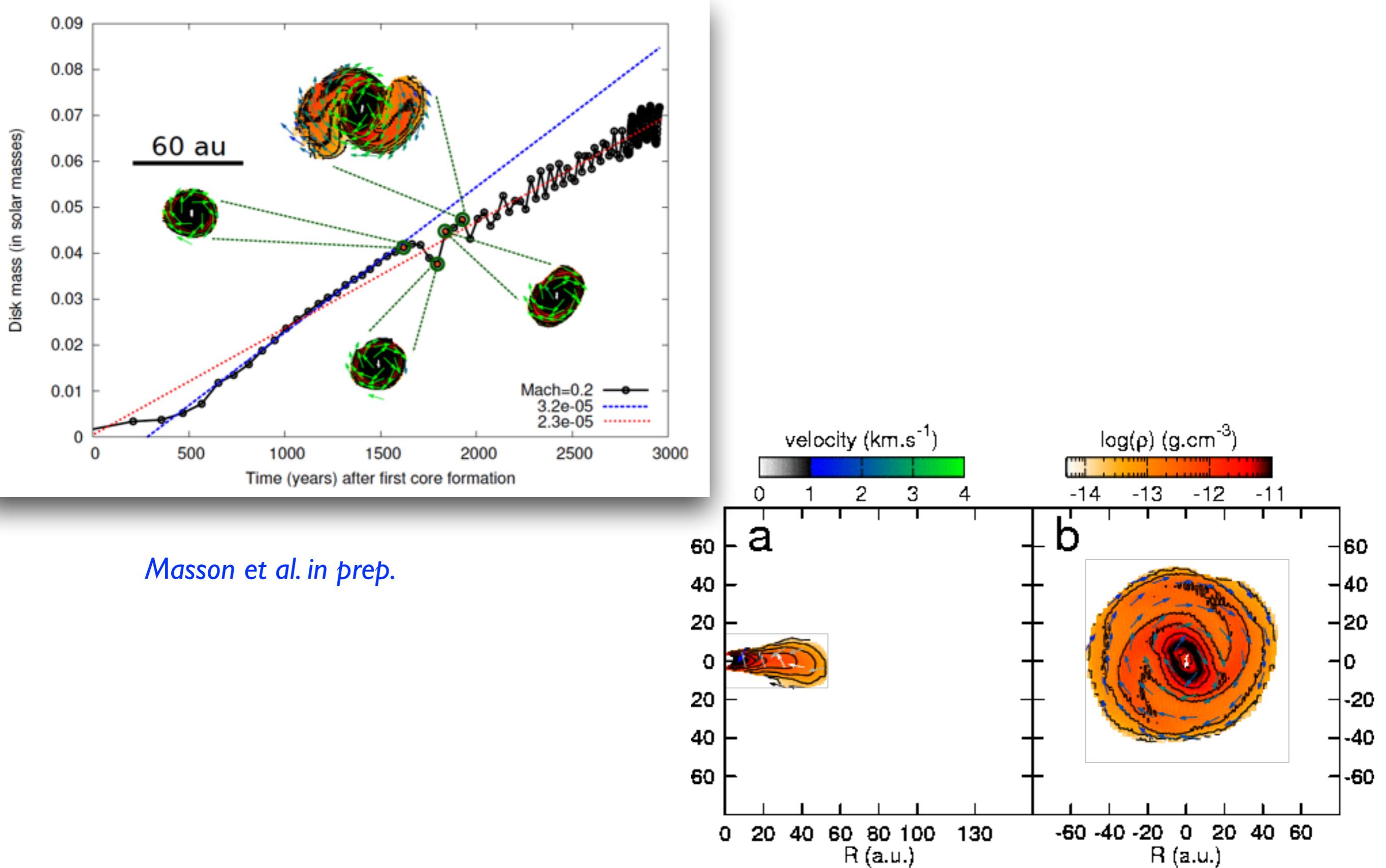
- disc size **does not depend** on turbulence level  
=> combination between turbulent diffusion and ambipolar diffusion?



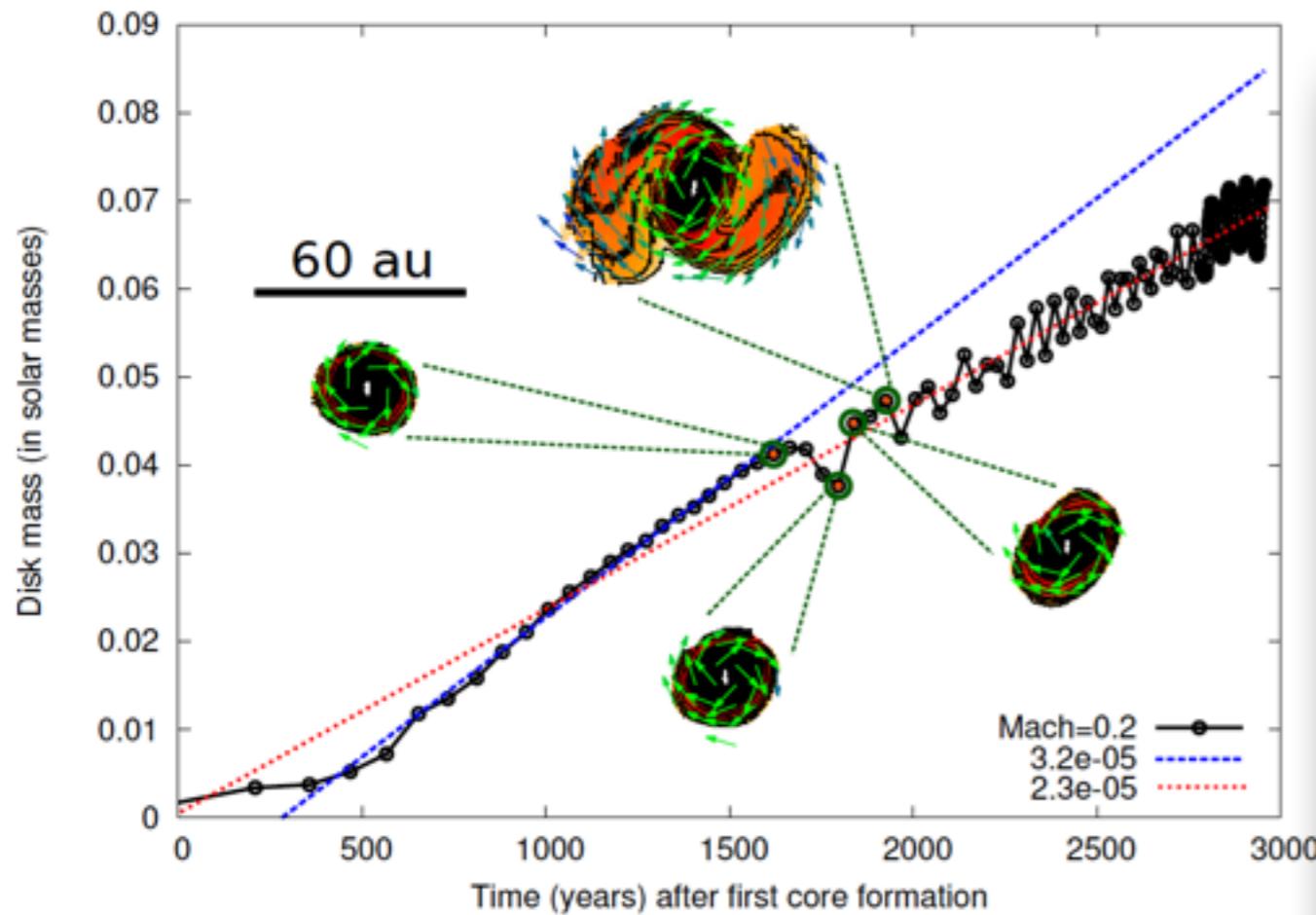
# Late evolution



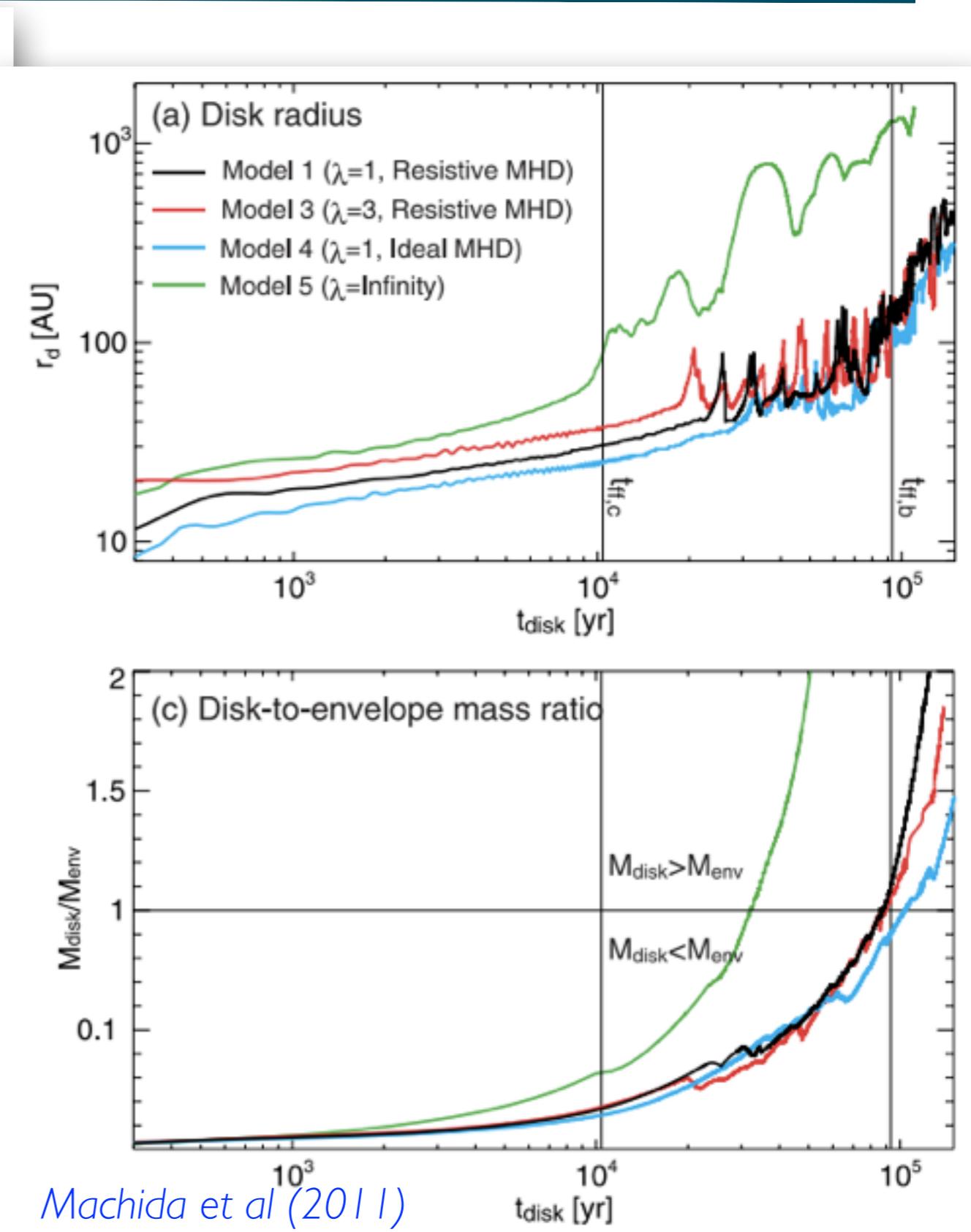
# Late evolution



# Late evolution



Masson et al. in prep.



# Magnetically regulated disc size with AD

*Hennebelle et al. (2016)*

$$\begin{aligned}\tau_{\text{far}} &\simeq \frac{B_\phi h}{B_z v_\phi} \\ \tau_{\text{diff}} &\simeq \frac{4\pi h^2}{c^2 \eta_{\text{AD}}} \frac{B_z^2 + B_\phi^2}{B_z^2} \simeq \frac{4\pi h^2}{c^2 \eta_{\text{AD}}}\end{aligned}$$

$$\begin{aligned}\tau_{\text{br}} &\simeq \frac{\rho v_\phi 4\pi h}{B_z B_\phi} \\ \tau_{\text{rot}} &\simeq \frac{2\pi r}{v_\phi}\end{aligned}$$

$$r_{\text{d,AD}} \simeq 18 \text{ au}$$

$$\times \delta^{2/9} \left( \frac{\eta_{\text{AD}}}{0.1 \text{ s}} \right)^{2/9} \left( \frac{B_z}{0.1 \text{ G}} \right)^{-4/9} \left( \frac{M_{\text{d}} + M_*}{0.1 M_{\odot}} \right)^{1/3}$$

- disc size **does not depend** on turbulence level
- weak dependance on the mass

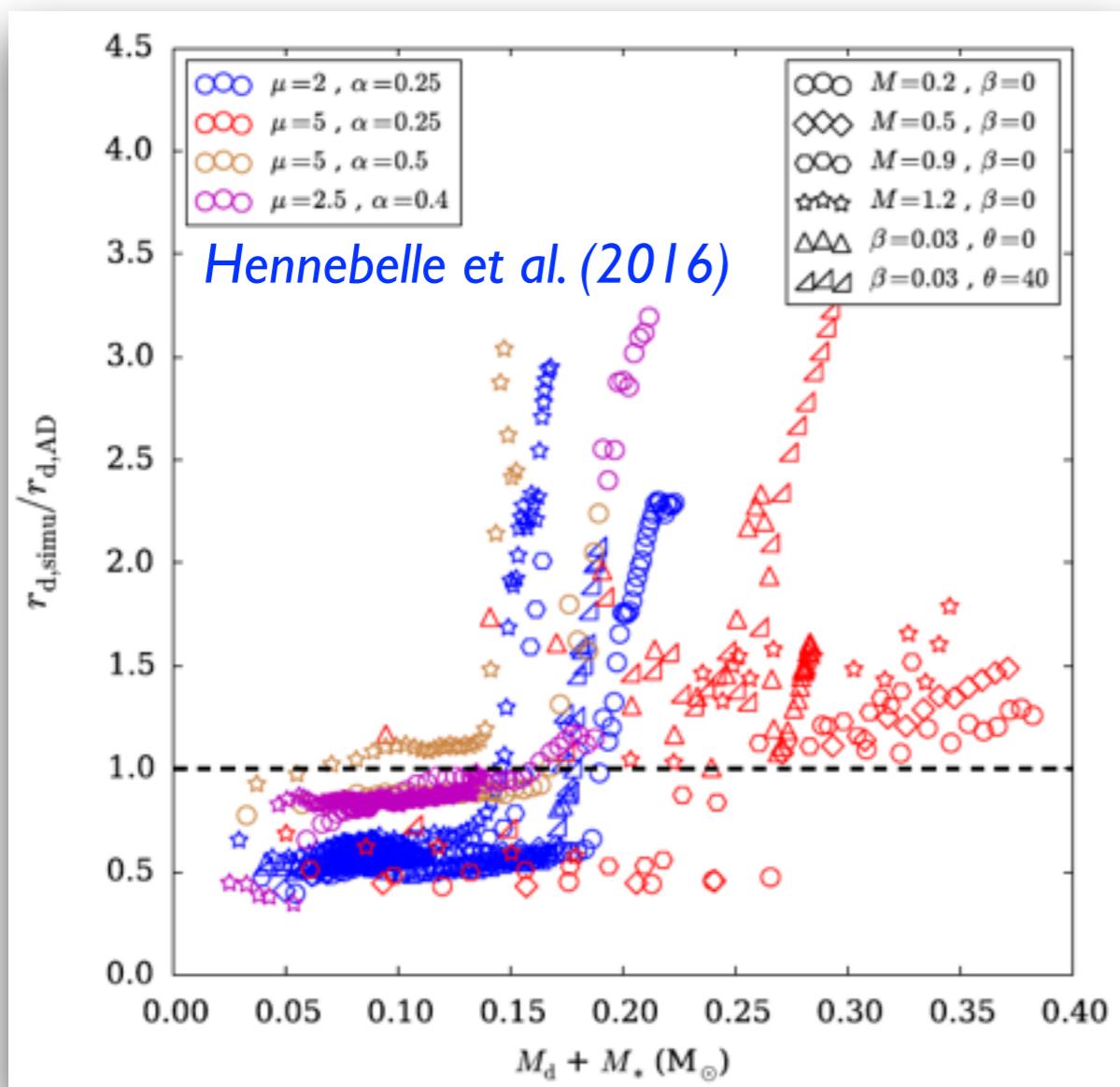
VS.

$$r_{\text{d,hydro}} \simeq \frac{\Omega_0^2 R_0^4}{4\pi/3 \rho_0 R_0^3 G} = 3\beta R_0 = 106 \text{ AU} \frac{\beta}{0.02} \left( \frac{M}{0.1 M_{\odot}} \right)^{1/3} \left( \frac{\rho_0}{10^{-18} \text{ g cm}^{-3}} \right)^{-1/3}$$

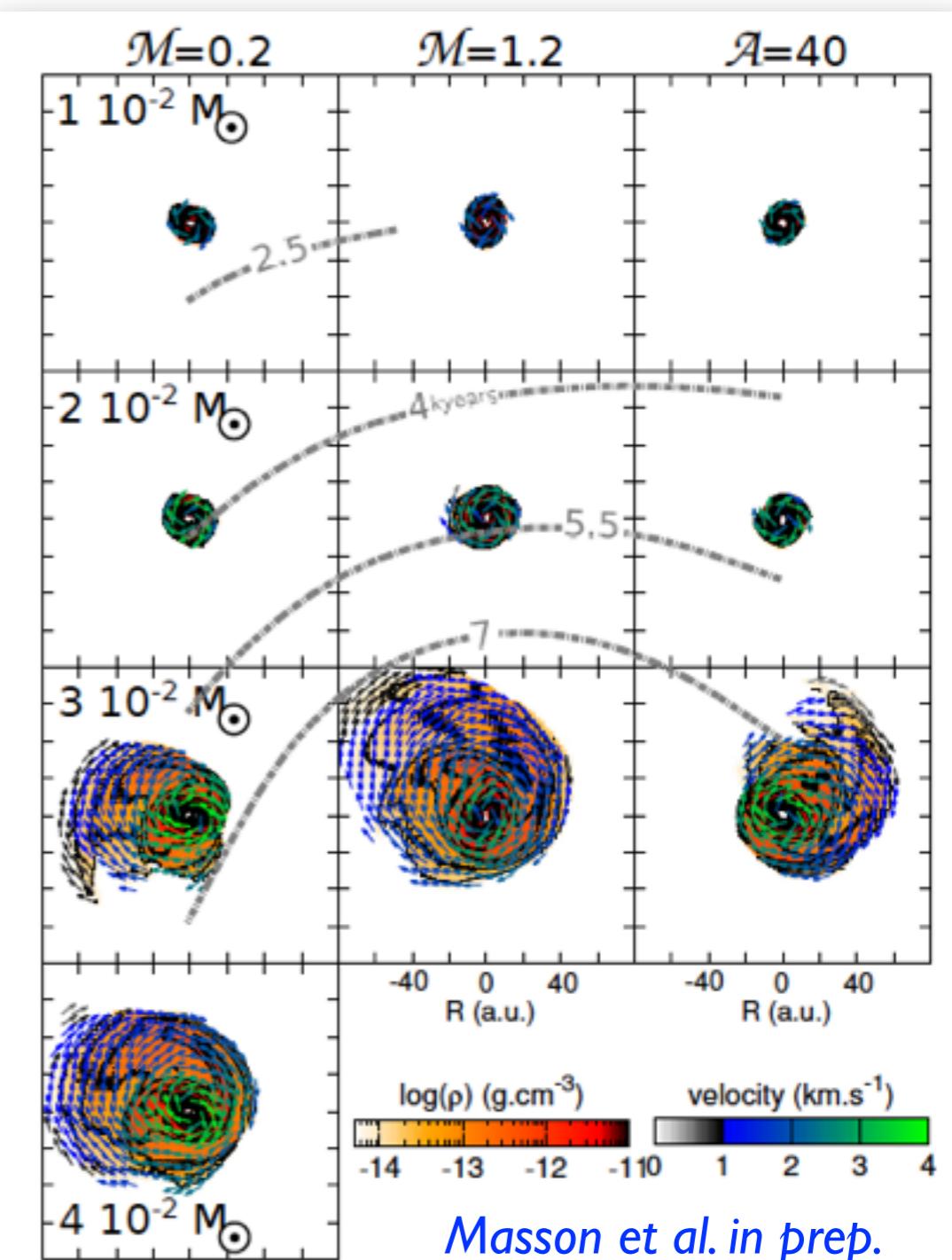
# Magnetically regulated disc size with AD

$$r_{d,AD} \simeq 18 \text{ au}$$

$$\times \delta^{2/9} \left( \frac{\eta_{AD}}{0.1 \text{ s}} \right)^{2/9} \left( \frac{B_z}{0.1 \text{ G}} \right)^{-4/9} \left( \frac{M_d + M_*}{0.1 M_\odot} \right)^{1/3}$$



- disc size **does not depend** on turbulence level
- weak dependence on the mass

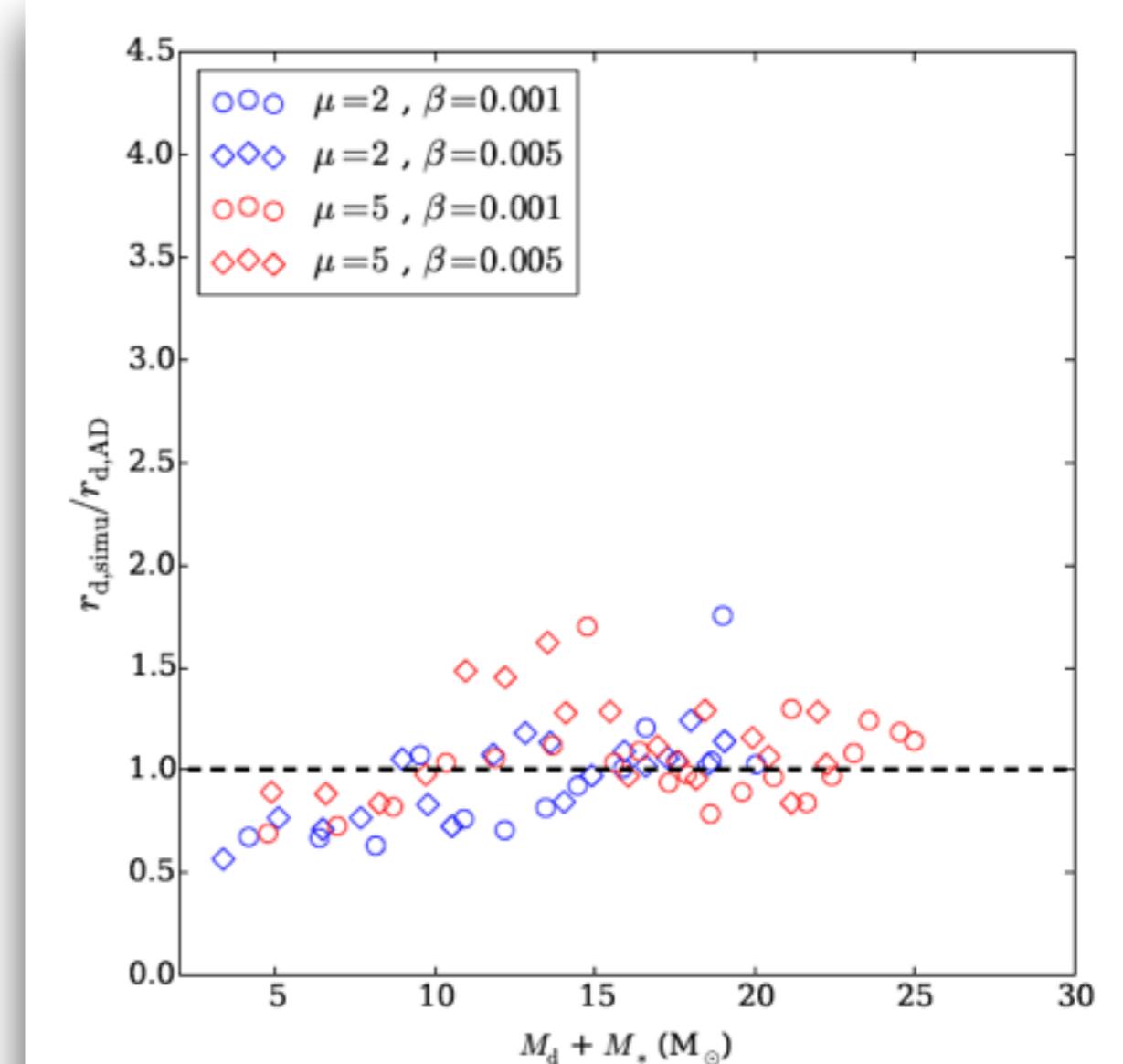
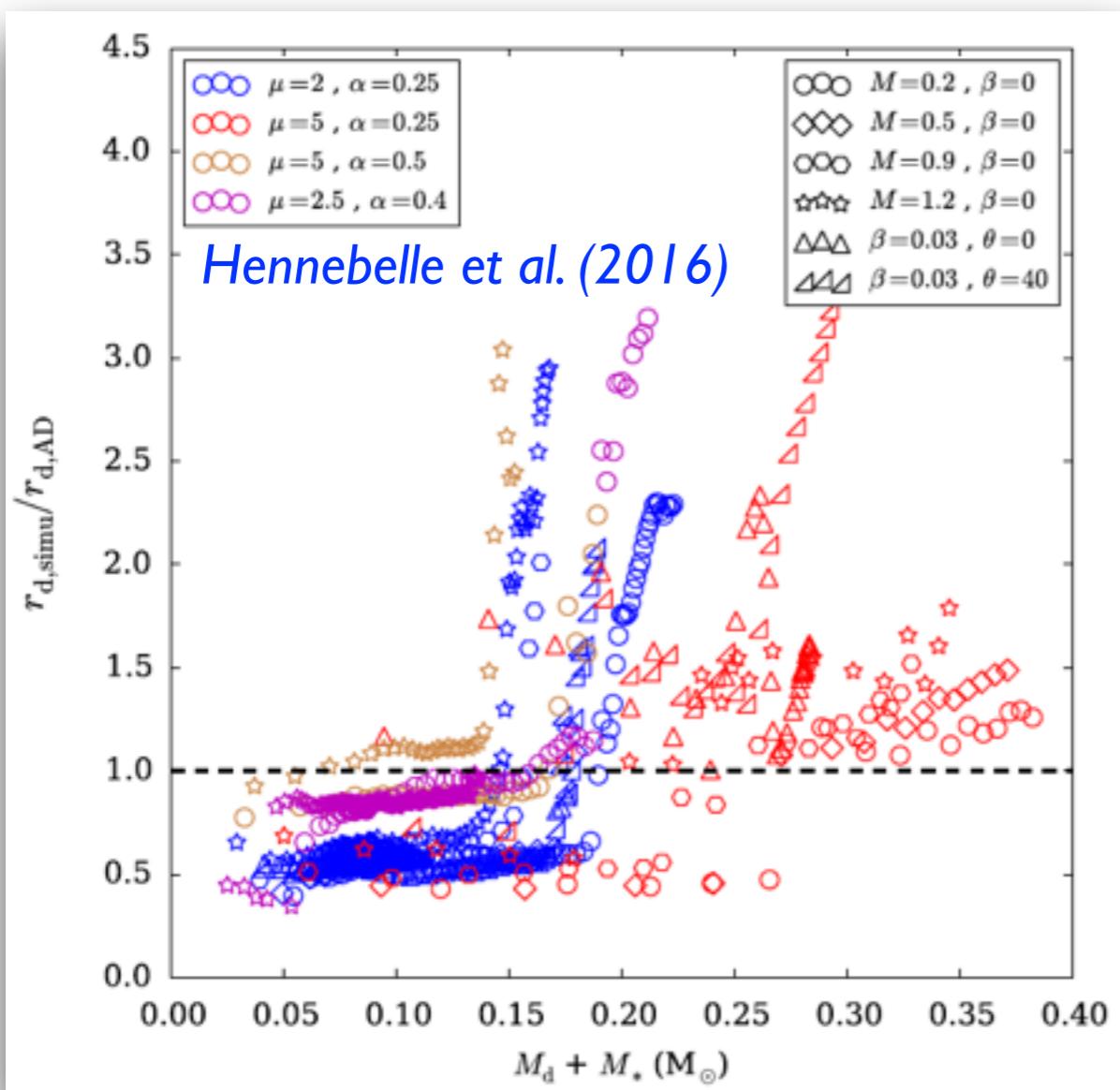


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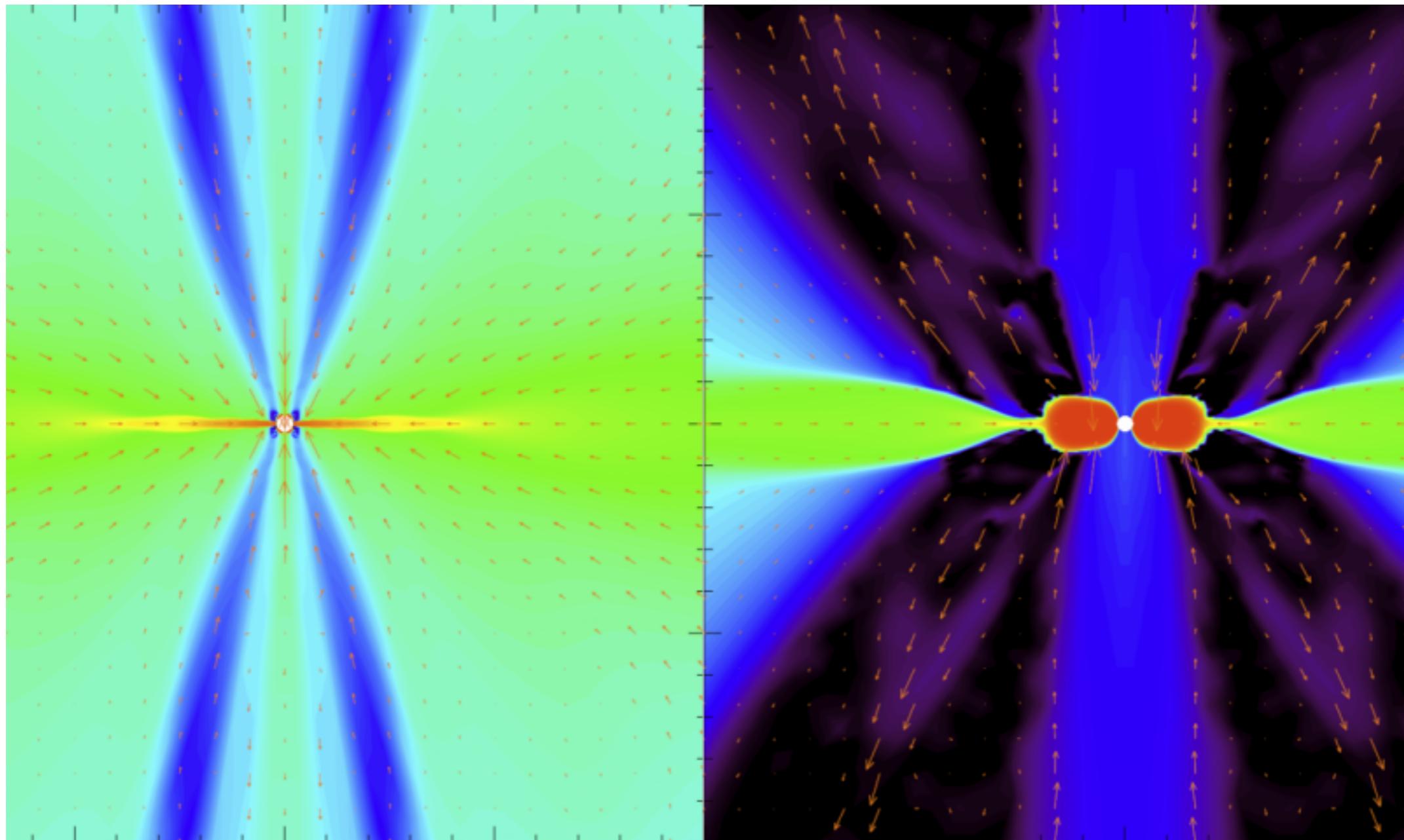
- disc size **does not depend** on turbulence level
- weak dependence on the mass



✓ Works for massive stars as well!

# Effect of dust grains

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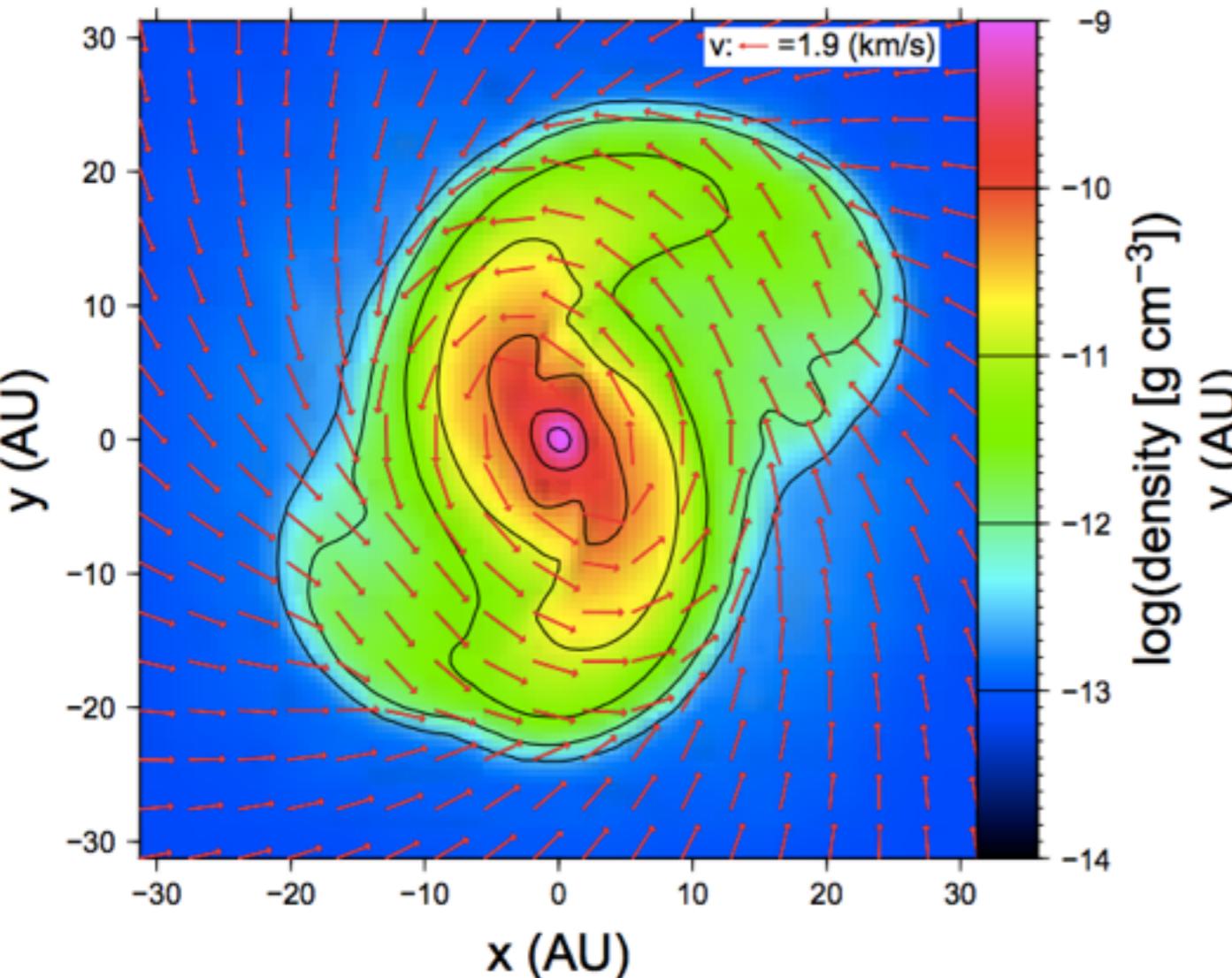


Small grains  
standard MRN  
 $a_{\min} = 0.005 \text{ } \mu\text{m}, a_{\max} = 0.25 \text{ } \mu\text{m}$

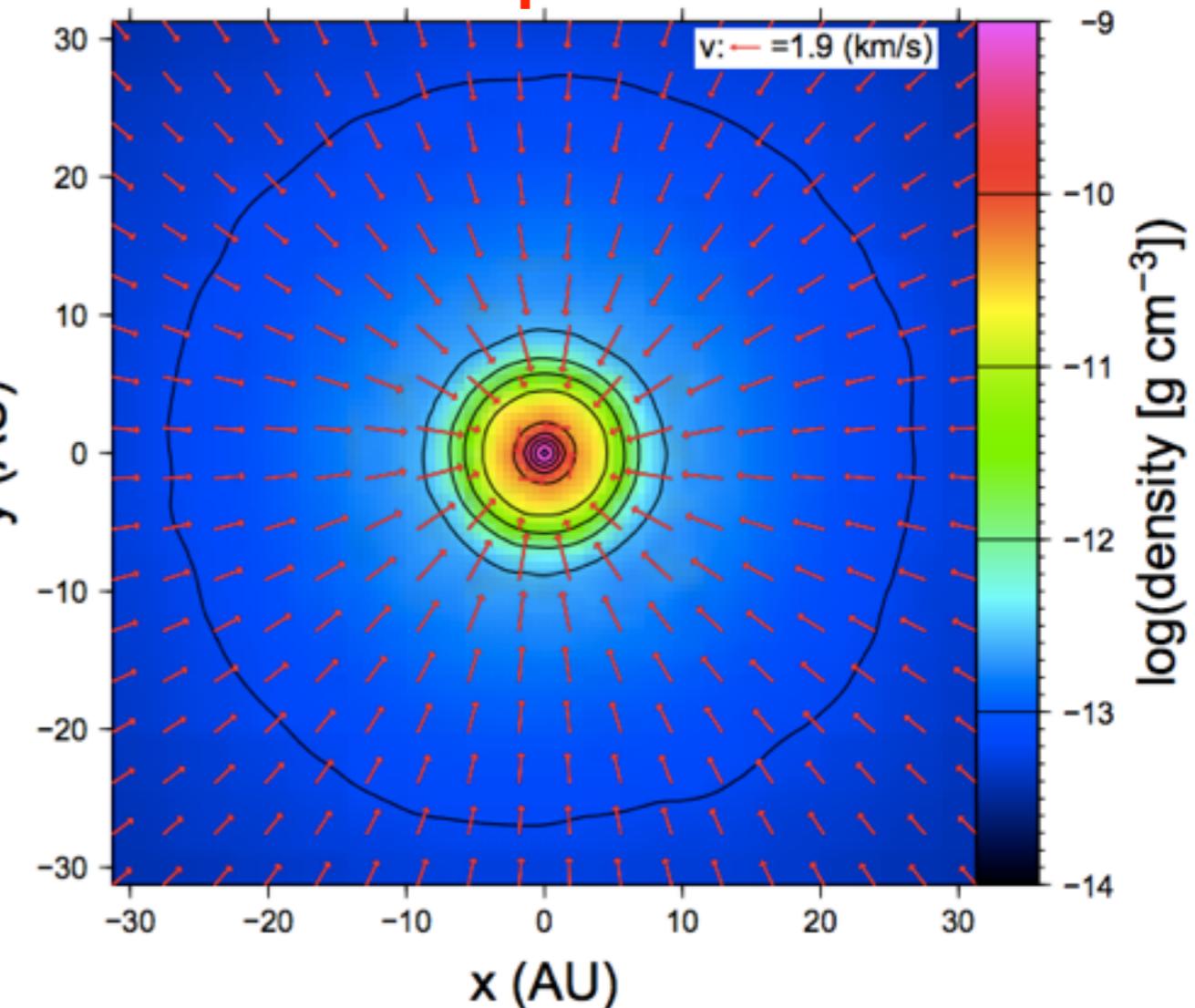
Large grains  
truncated MRN  
 $a_{\min} = 0.1 \text{ } \mu\text{m}, a_{\max} = 0.25 \text{ } \mu\text{m}$   
*Zhao et al (2016)*

# Hall effect

parallel



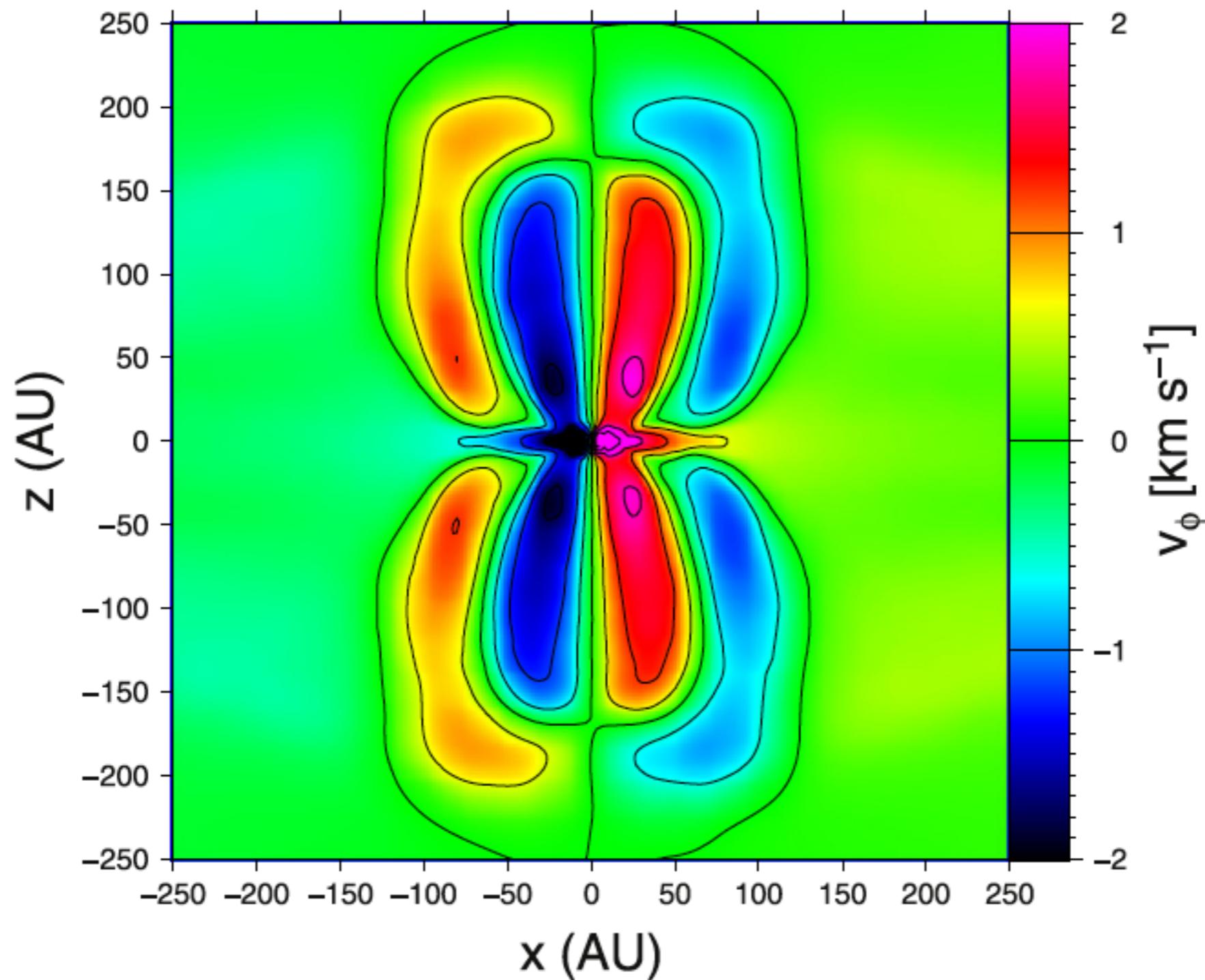
anti-parallel



- Hall effect depends on the magnetic field orientation
- Bi-modality of disc properties
- non-aligned configuration?

# Hall effect

---

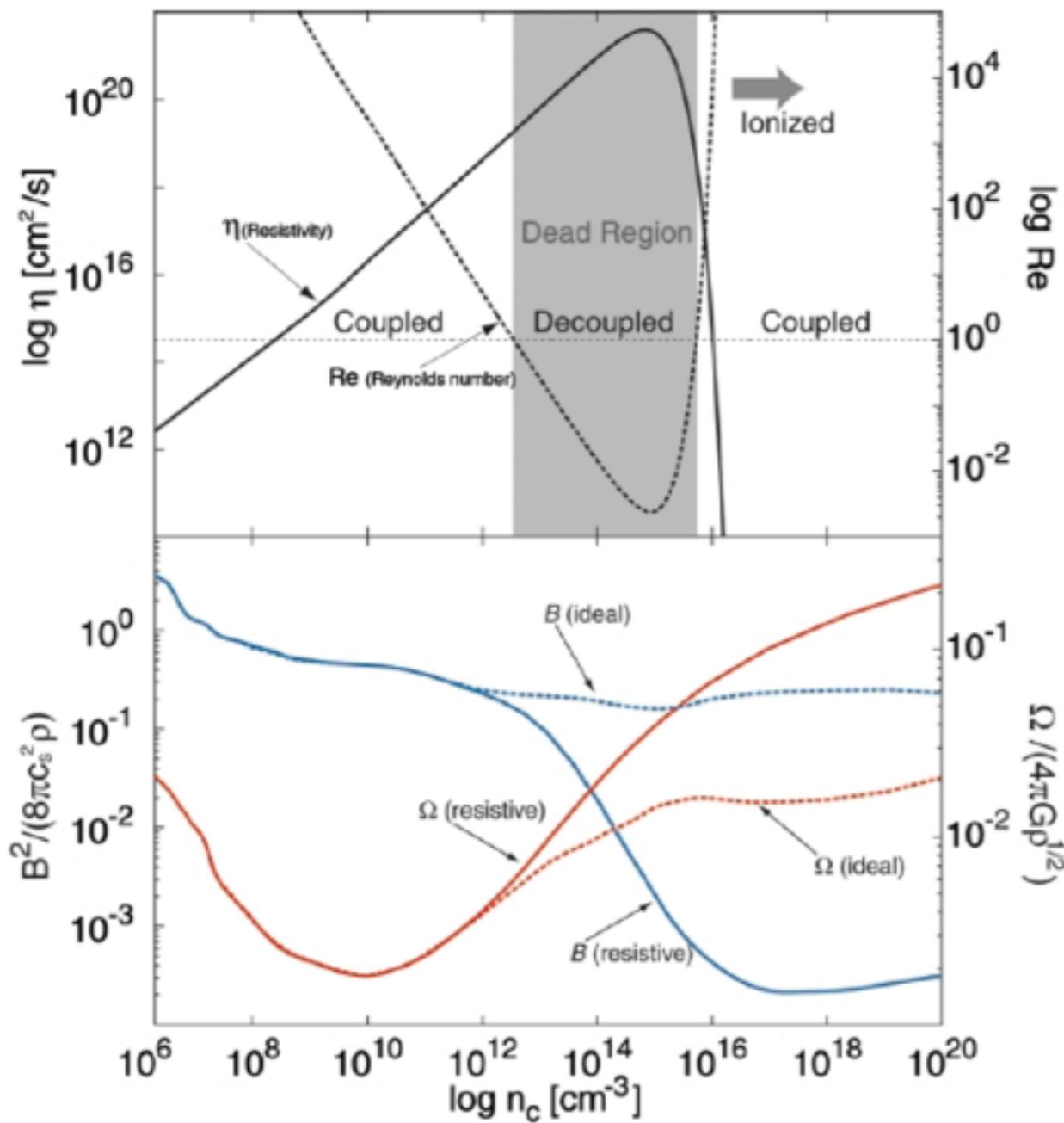


- Counter-rotating envelope

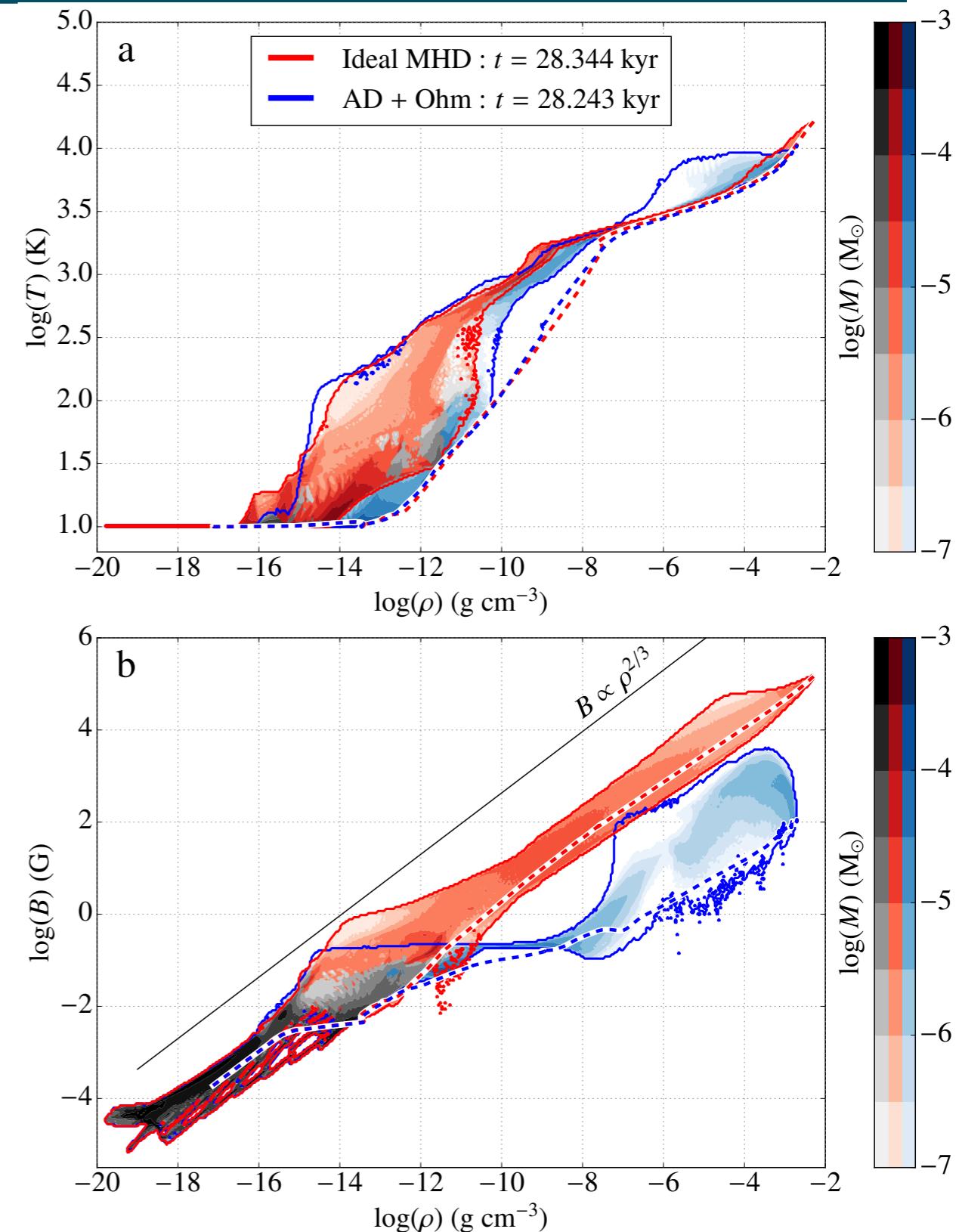
Tsukamoto et al. (2015)

# 2nd collapse

Magnetic flux reduced by  $\sim 3$  orders of magnitude only with ambipolar diffusion and Ohmic diffusion



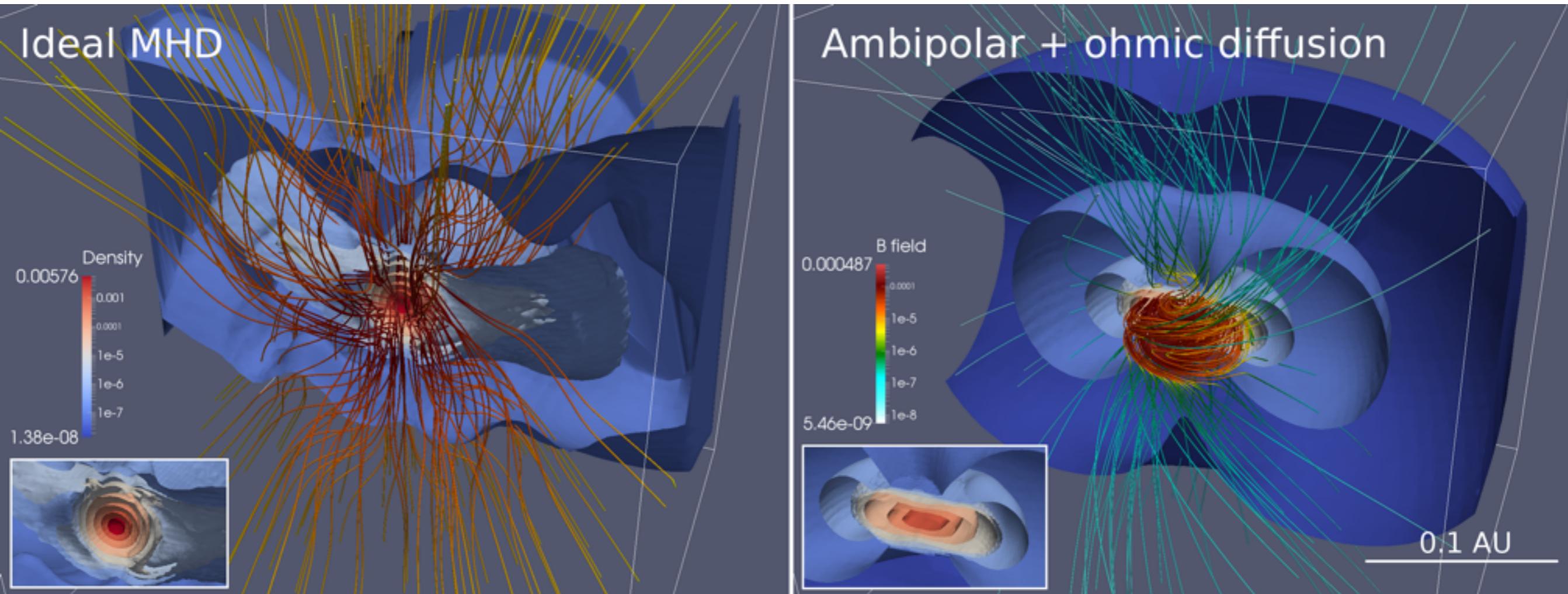
Machida et al (2008)



Vaytet et al (in prep.)

# 2nd collapse

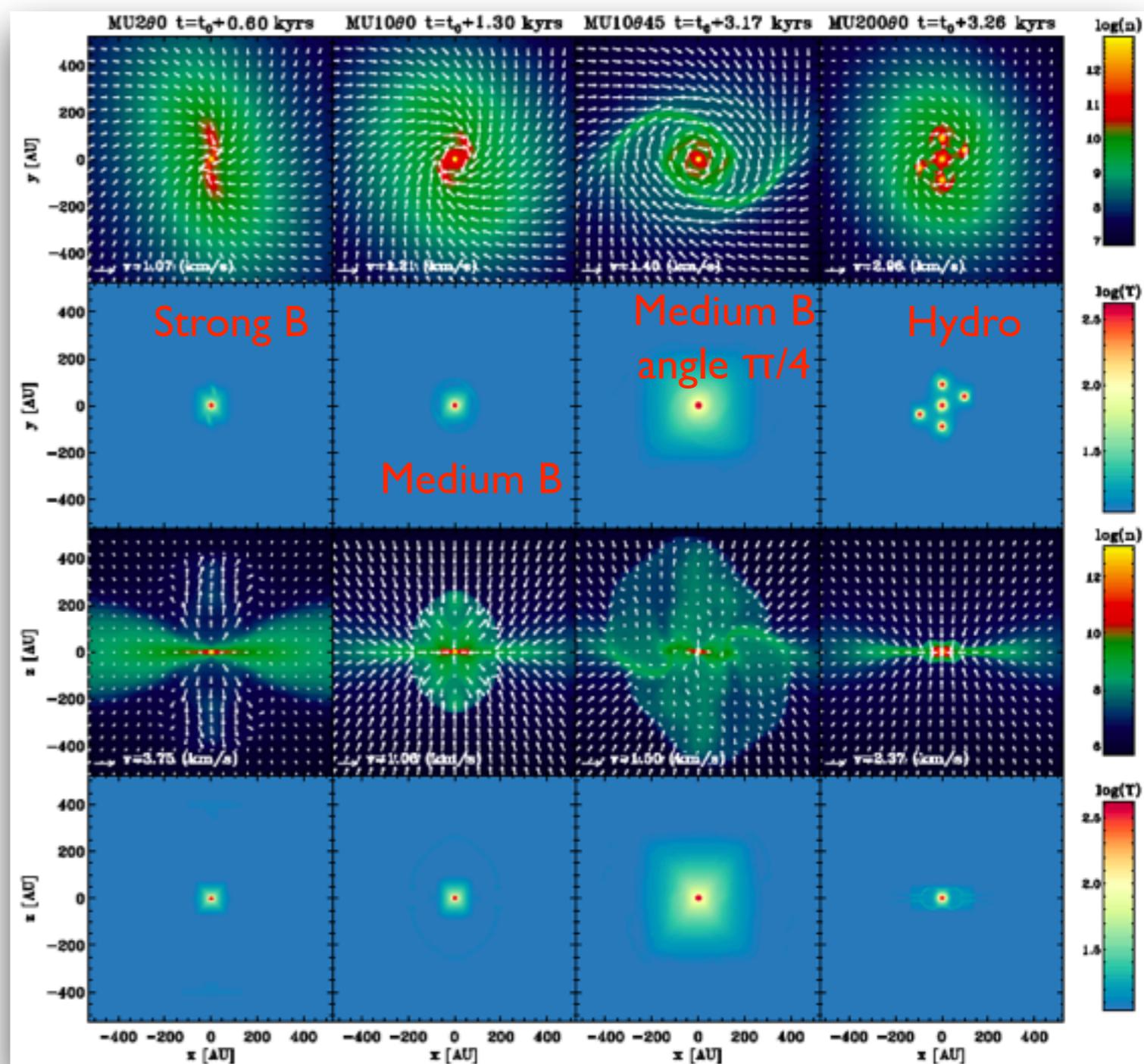
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Vaytet et al (in prep.)

# Dynamical chemical evolution w tracer particles

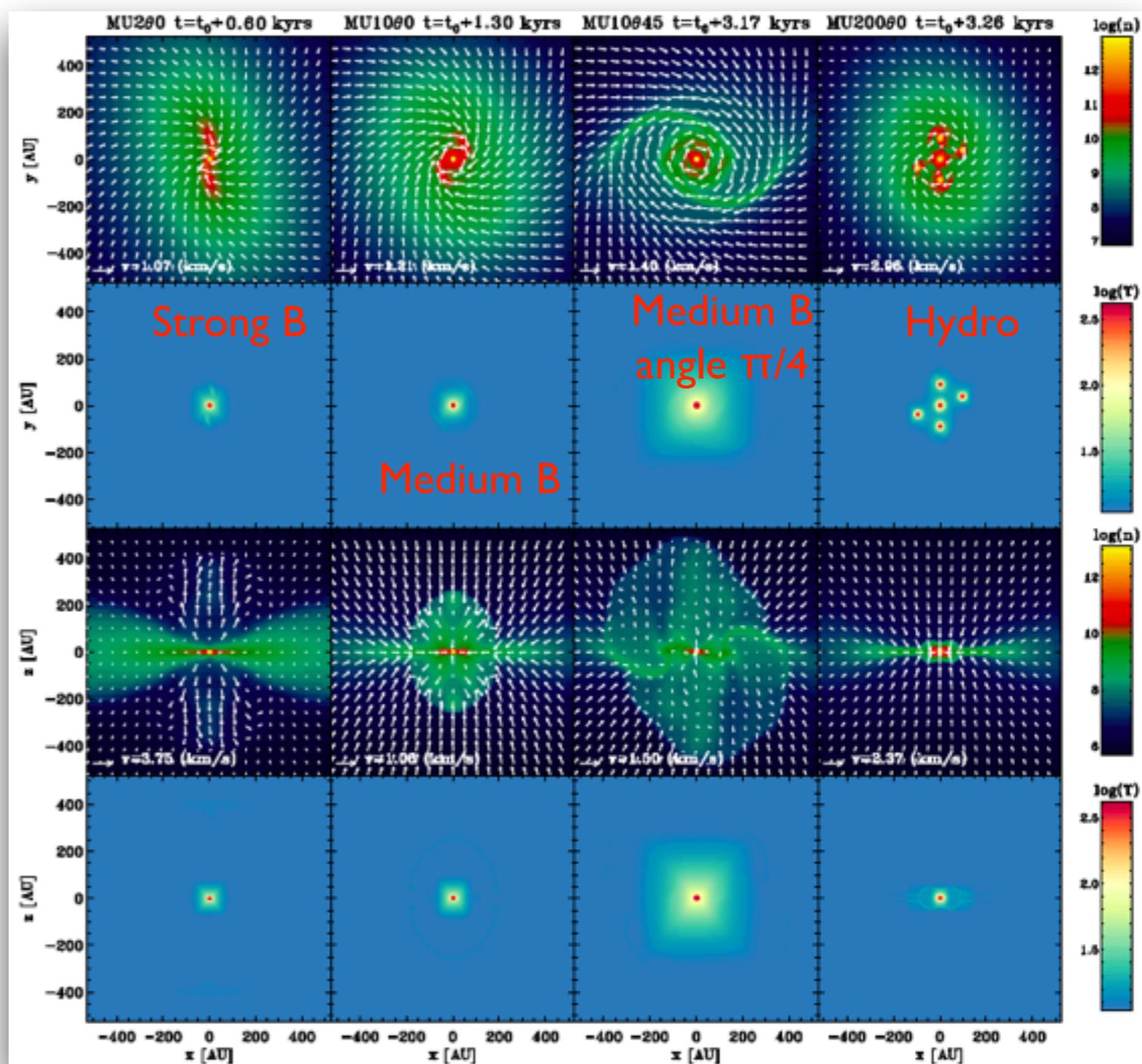
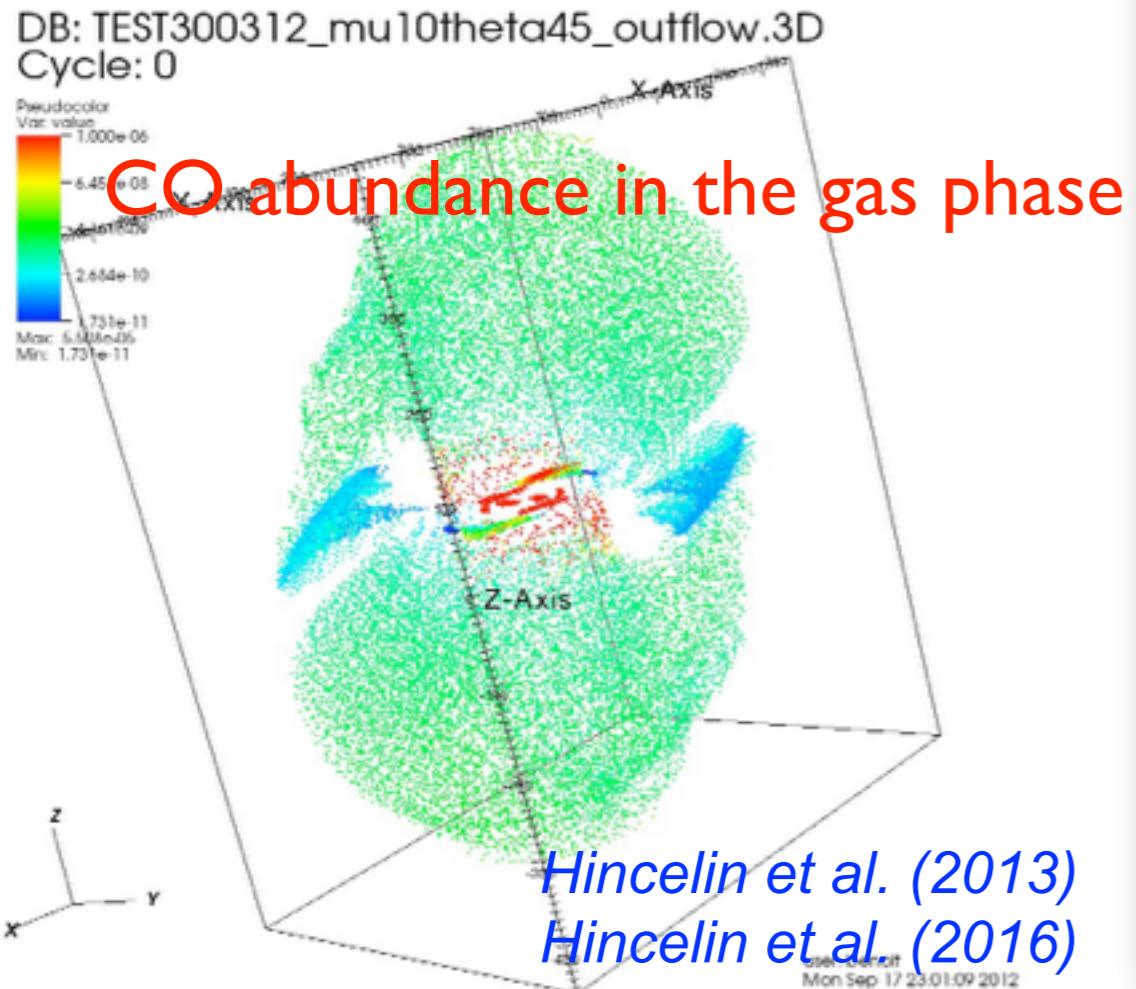
- $10^6$  tracer particles & store position, temperature & density
  - $1 M_\odot$  dense core collapse with 3 different magnetisation and 1 different angle
  - Compute the chemistry using the Bordeaux **NAUTILUS** full gas-grain chemistry code (655 species,  $>6000$  reactions)
  - 50 000 CPU hours for chemistry
- ✓ Access to the 3D abundances within the collapsing dense cores  
✓ Account for hysteresis effects



*Hincelin et al. (2013)*  
*Hincelin et al. (2016)*

# Dynamical chemical evolution w tracer particles

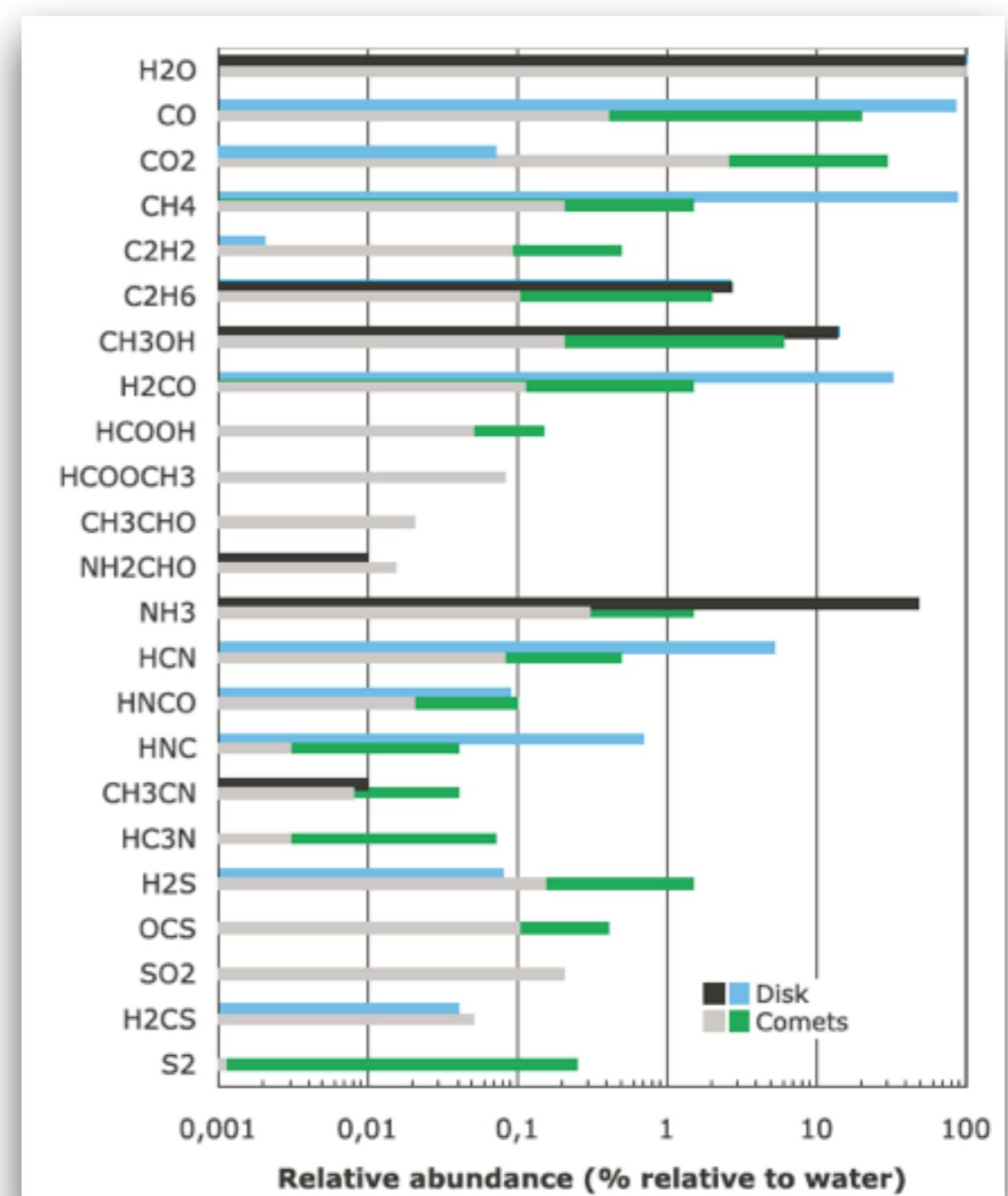
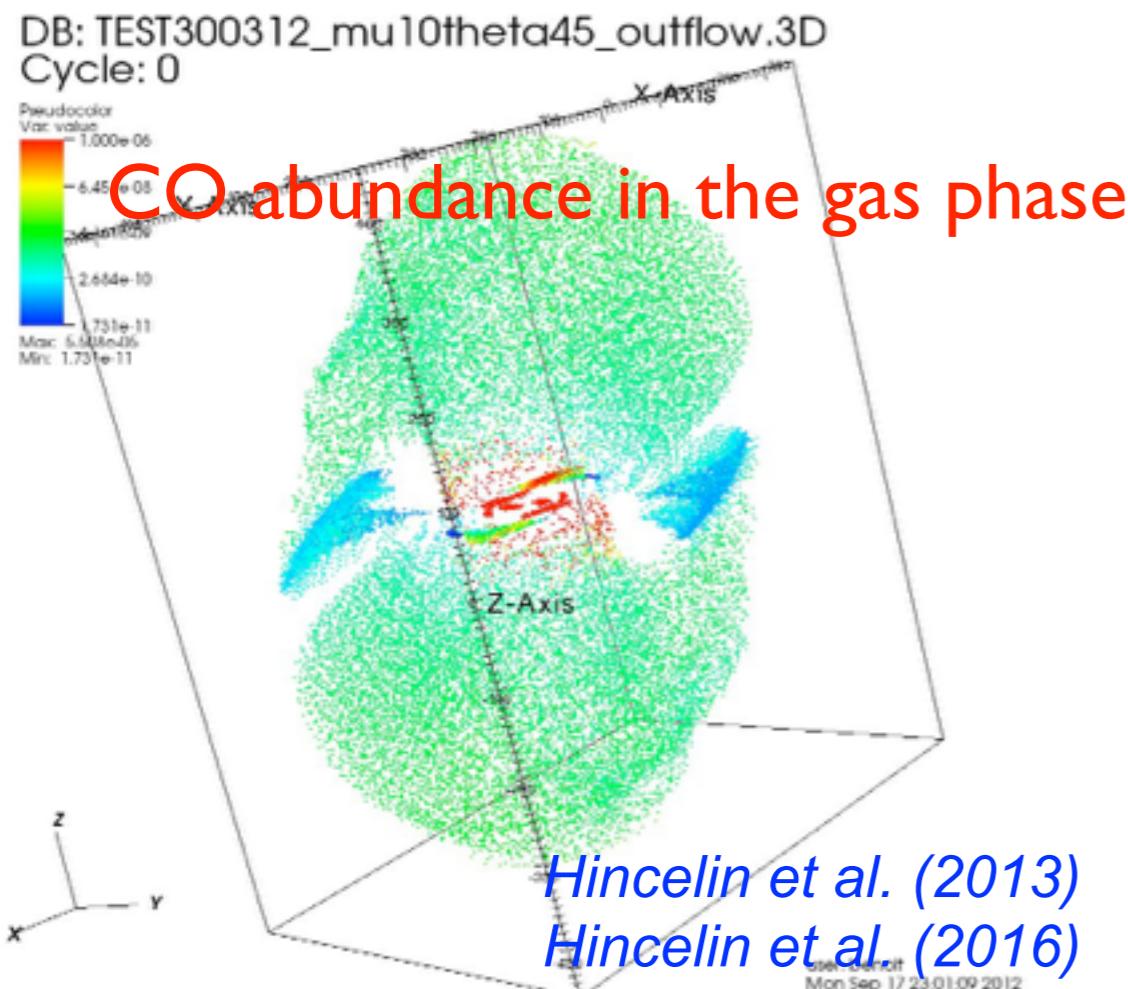
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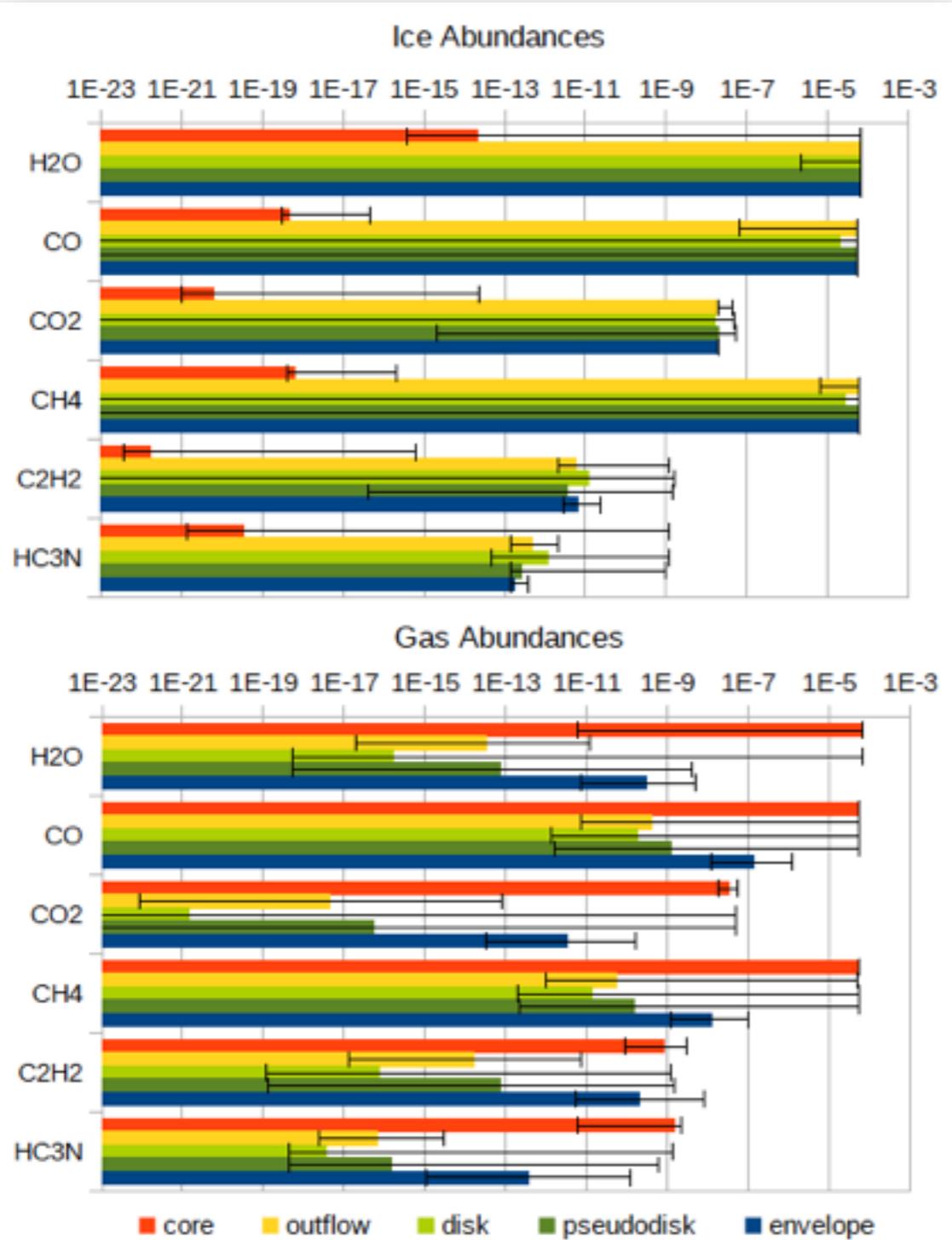
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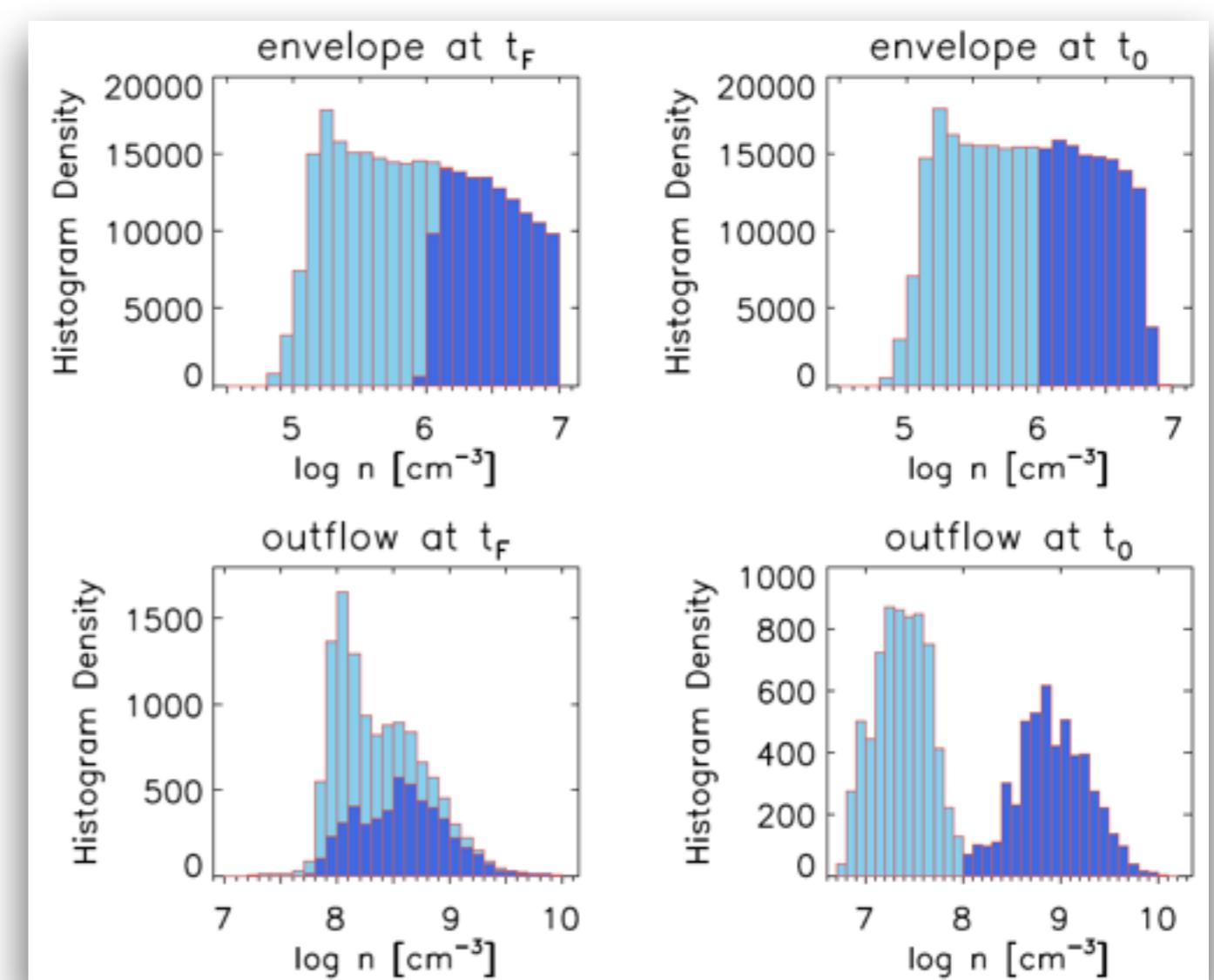


# Dynamical chemical evolution w tracer particles



*Hincelin et al., 2016  
see also Ruaud et al.*

- total abundance (gas+ice) unchanged from the parent cloud to the disc;
- mixing of particles with **different histories**;
- tracers identification of the different **components**: core, disc, pseudo-disc, outflow, and envelop

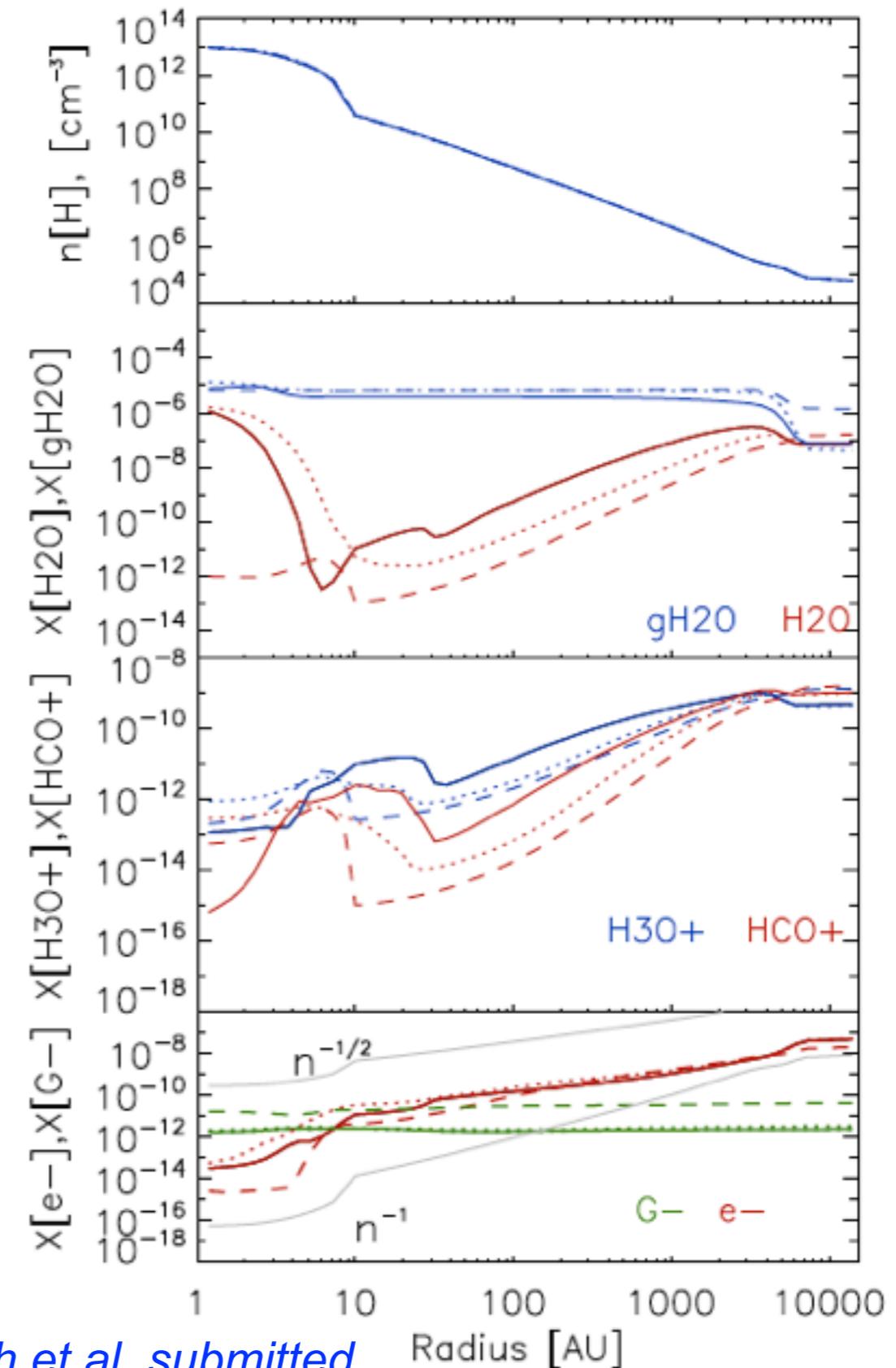
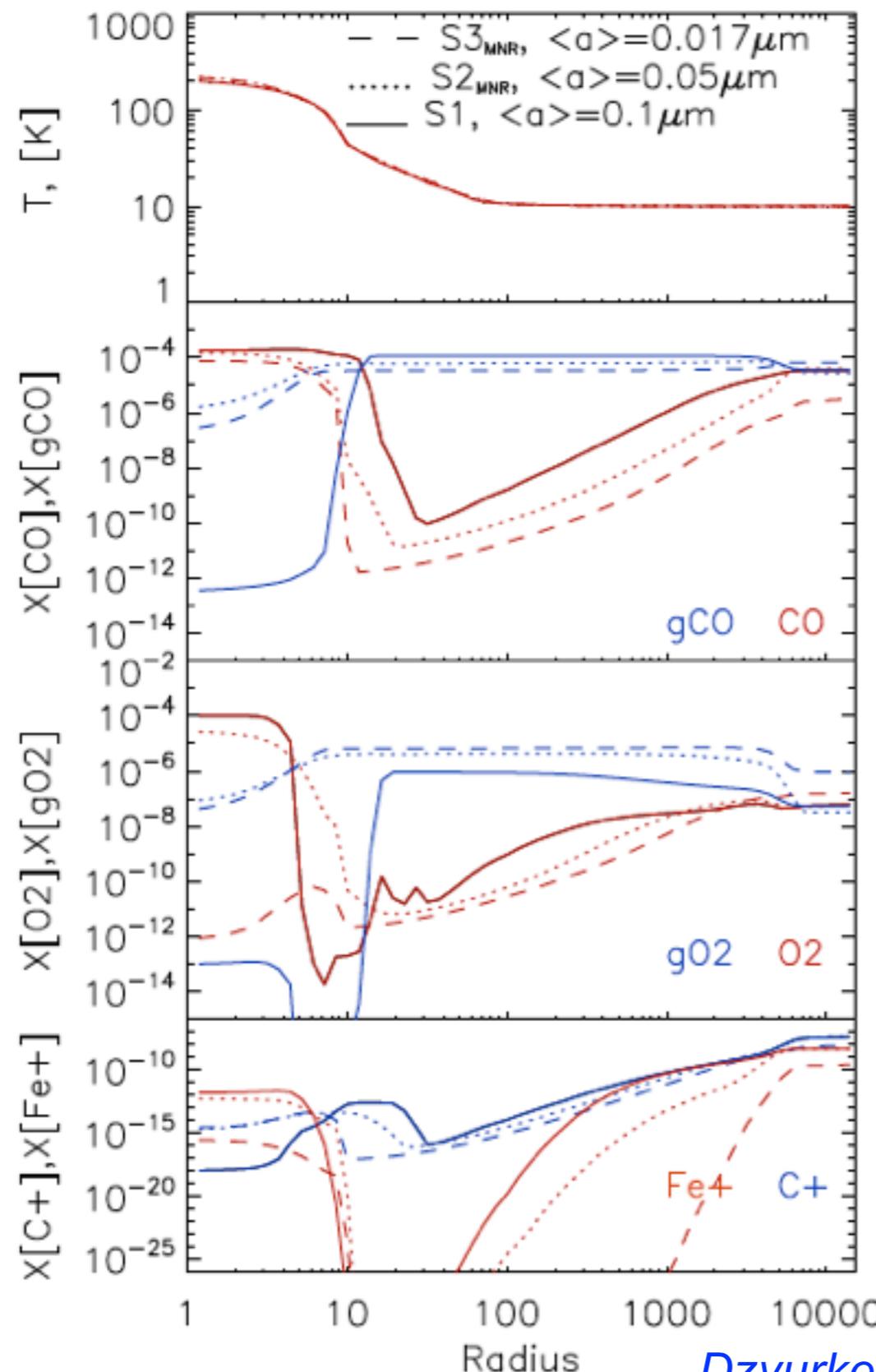


# Chemo-dynamical models

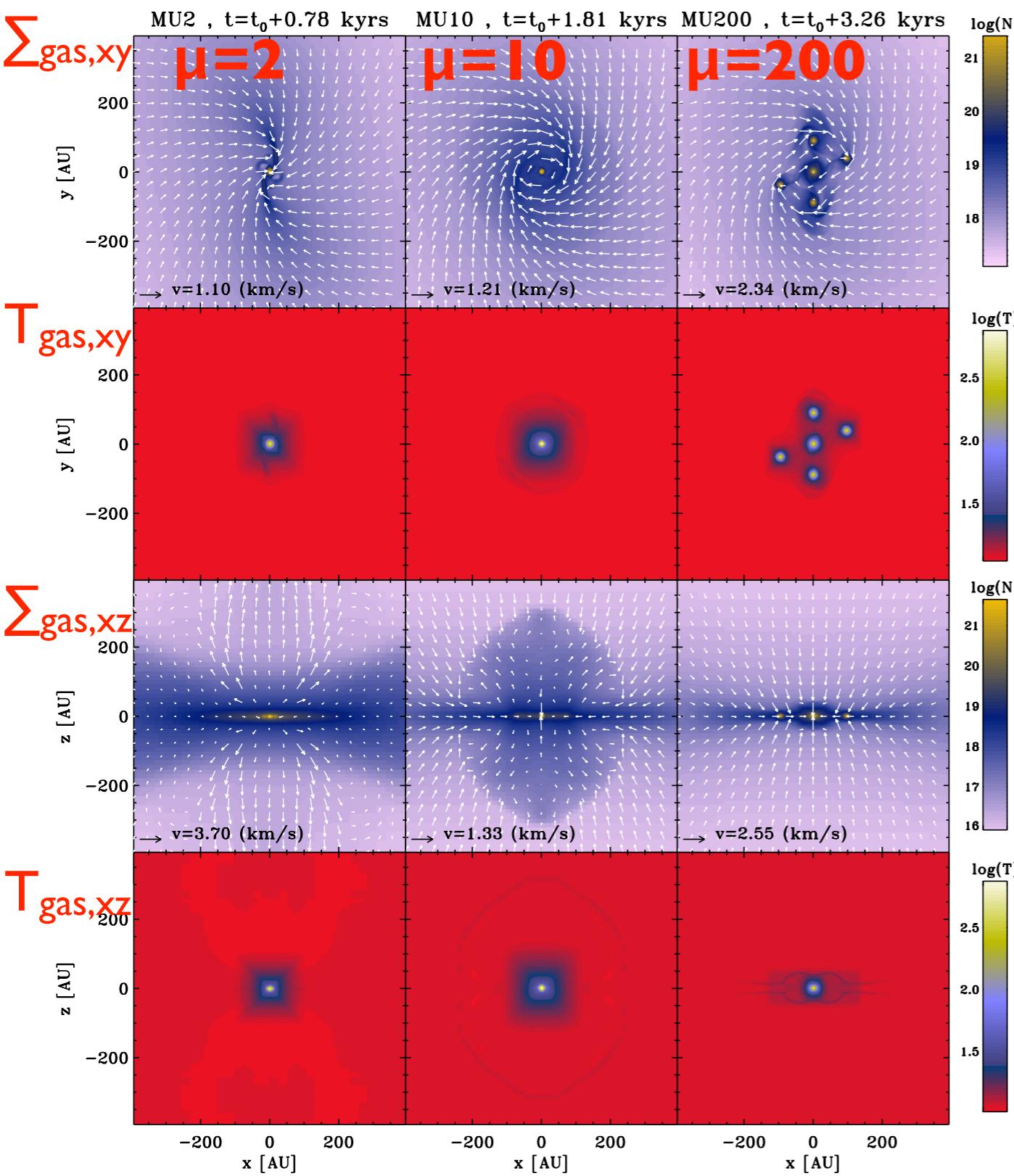
- reduced chemical network designed for H-C-O chemistry, from the **CHOC\_STAT** code (Lesaffre, Pineau des Forets, Flower et al.)
- chemical species are advected in **RAMSES** and chemistry is solved after each hydro timestep
- no retroaction of the chemistry on the dynamics yet...
- N=56 species (51 + 5 for the dust core refractory material)
- ~230 reactions: gas-phase, recombination, photodissociation and ionisation, CR desorption and ionisation, gas-grain interaction (adsorption, desorption, charge transfer)

H	H <sub>2</sub>	He	C	CH	CH <sub>2</sub>	CH <sub>3</sub>	CH <sub>4</sub>	O	O <sub>2</sub>	OH	H <sub>2</sub> O	CO	CO <sub>2</sub>	Fe
Neutral species														
H <sup>+</sup>	H <sub>2</sub> <sup>+</sup>	H <sub>3</sub> <sup>+</sup>	He <sup>+</sup>	C <sup>+</sup>	CH <sup>+</sup>	CH <sub>2</sub> <sup>+</sup>	CH <sub>3</sub> <sup>+</sup>	CH <sub>4</sub> <sup>+</sup>	CH <sub>5</sub> <sup>+</sup>	O <sup>+</sup>	O <sub>2</sub> <sup>+</sup>	OH <sup>+</sup>	H <sub>2</sub> O <sup>+</sup>	H <sub>3</sub> O <sup>+</sup>
CO <sup>+</sup>	HCO <sup>+</sup>	Fe <sup>+</sup>	Ionized species											
O <sup>**</sup>	Si <sup>**</sup>	Mg <sup>**</sup>	Fe <sup>**</sup>	C <sup>**</sup>	Core species									
H*	H <sub>2</sub> *	He*	C*	CH*	CH <sub>2</sub> *	CH <sub>3</sub> *	CH <sub>4</sub> *	O*	O <sub>2</sub> *	OH*	H <sub>2</sub> O*	CO*	CO <sub>2</sub> *	Fe*
Mantle species														
G	G <sup>+</sup>	G <sup>-</sup>	Grains											

# Spherical collapse: effects of dust grain size



# Towards synthetic observations



- 3 representative cases

**MU2**: pseudo-disc + outflow

**MU10**: disc + pseudo-disc + outflow

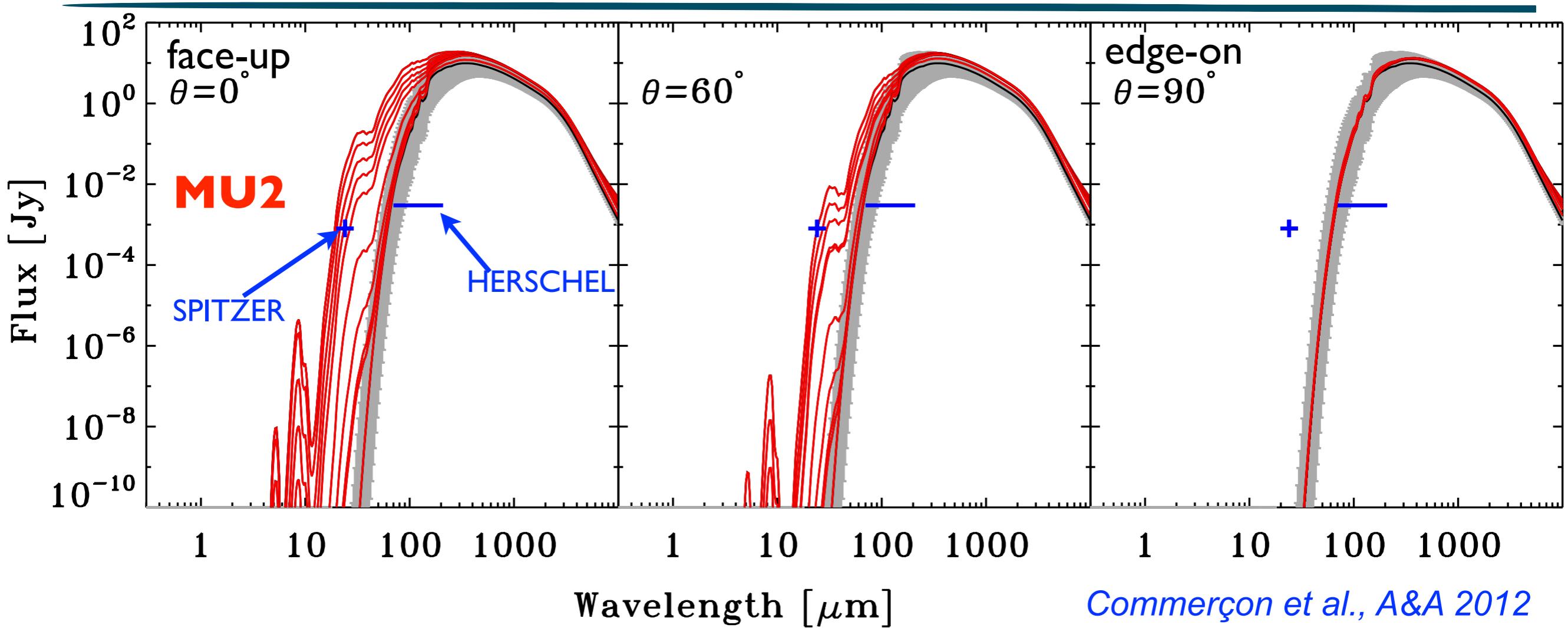
**MU200**: disc + fragmentation

- First core lifetime:

<b>MU2</b>	<b>MU10</b>	<b>MU200</b>
1.2 kyr	3 kyr	> 4 kyr

- Images & SED computed with the radiative transfer code **RADMC-3D**, developed by C. Dullemond (ITA Heidelberg)
- $T_{\text{dust}} = T_{\text{gas}}$  (given by the RMHD calculations)

# SED - Do we see a first core signature?

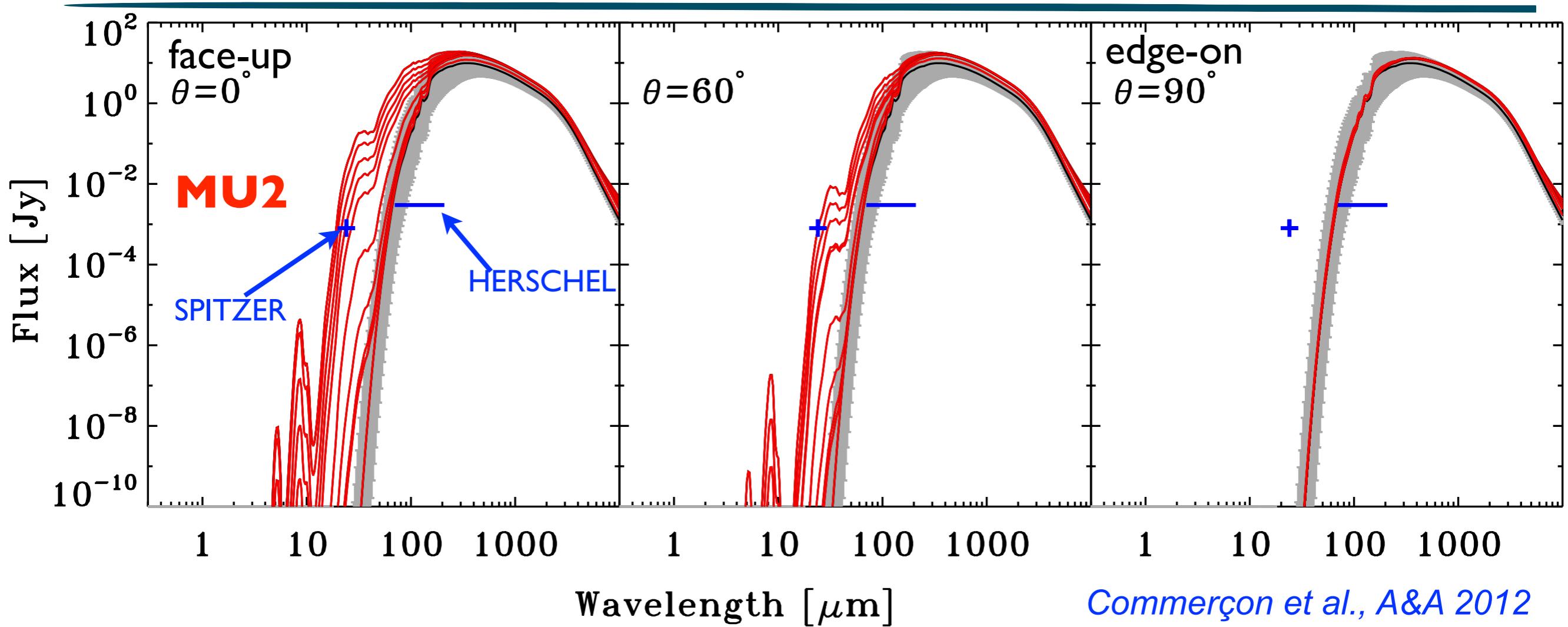


Commerçon et al., A&A 2012

- Objects at 150 pc, 3000 AU  $\times$  3000 AU region
- Prestellar core = initial conditions (black line)
- Emission in the FIR => **HERSCHEL, SPITZER**
- But similar SEDs in the MU200 model, i.e. **with a disc!**  
=> Issues in SED-fitting models for early Class 0?

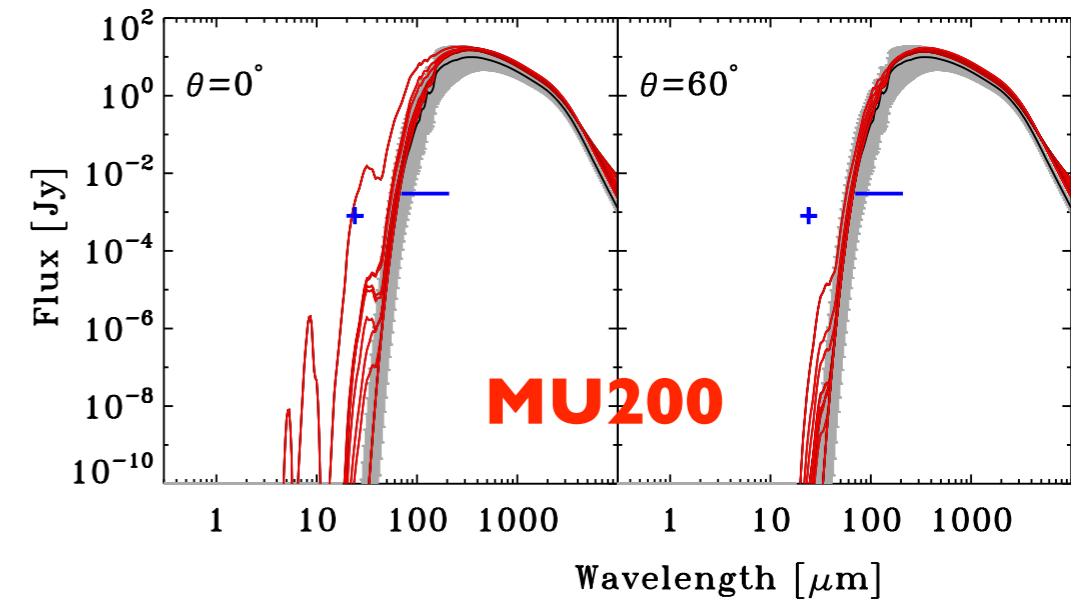
Help to select first core candidates & to distinguish  
starless cores and first cores

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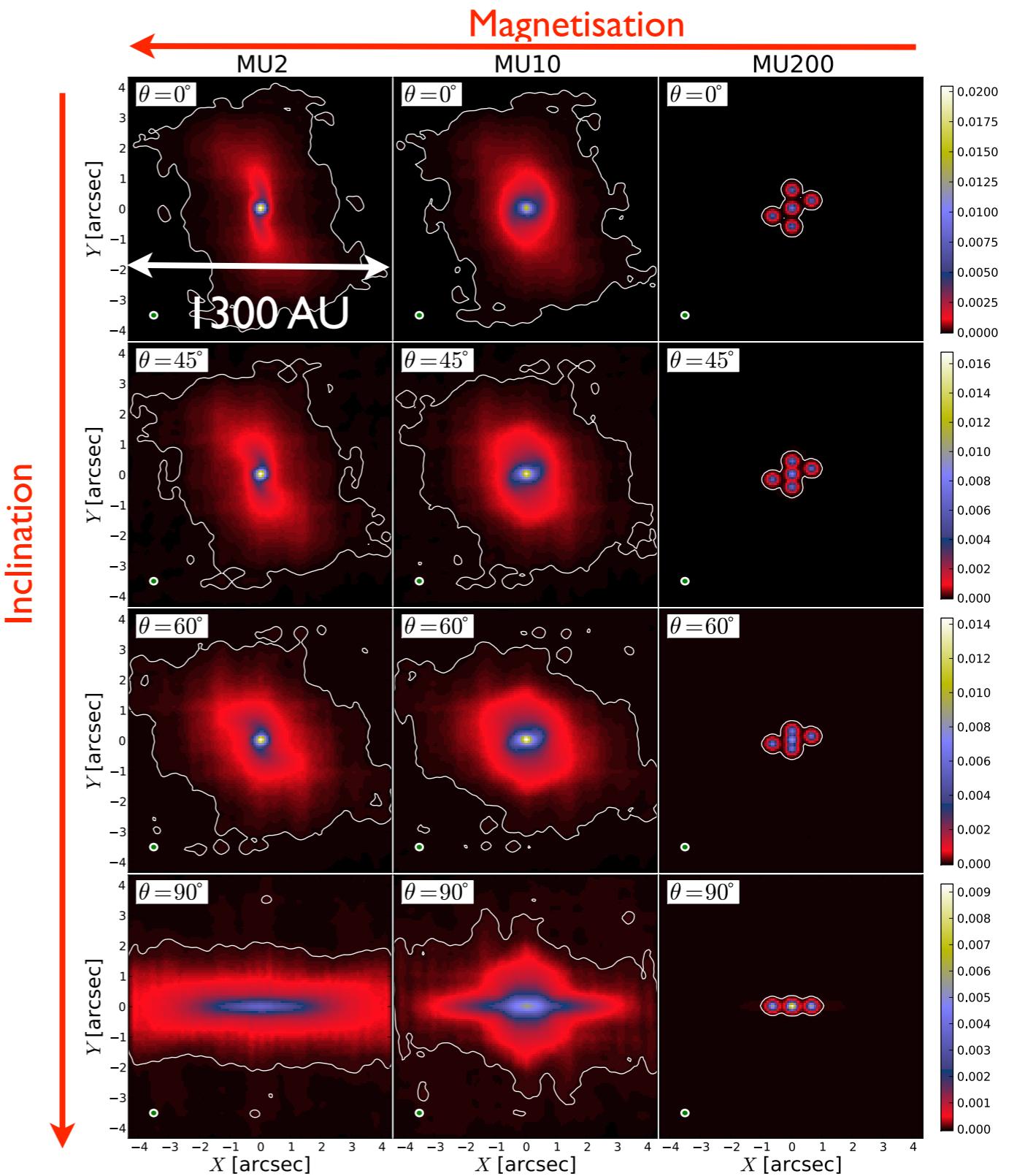
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# Synthetic ALMA dust emission maps

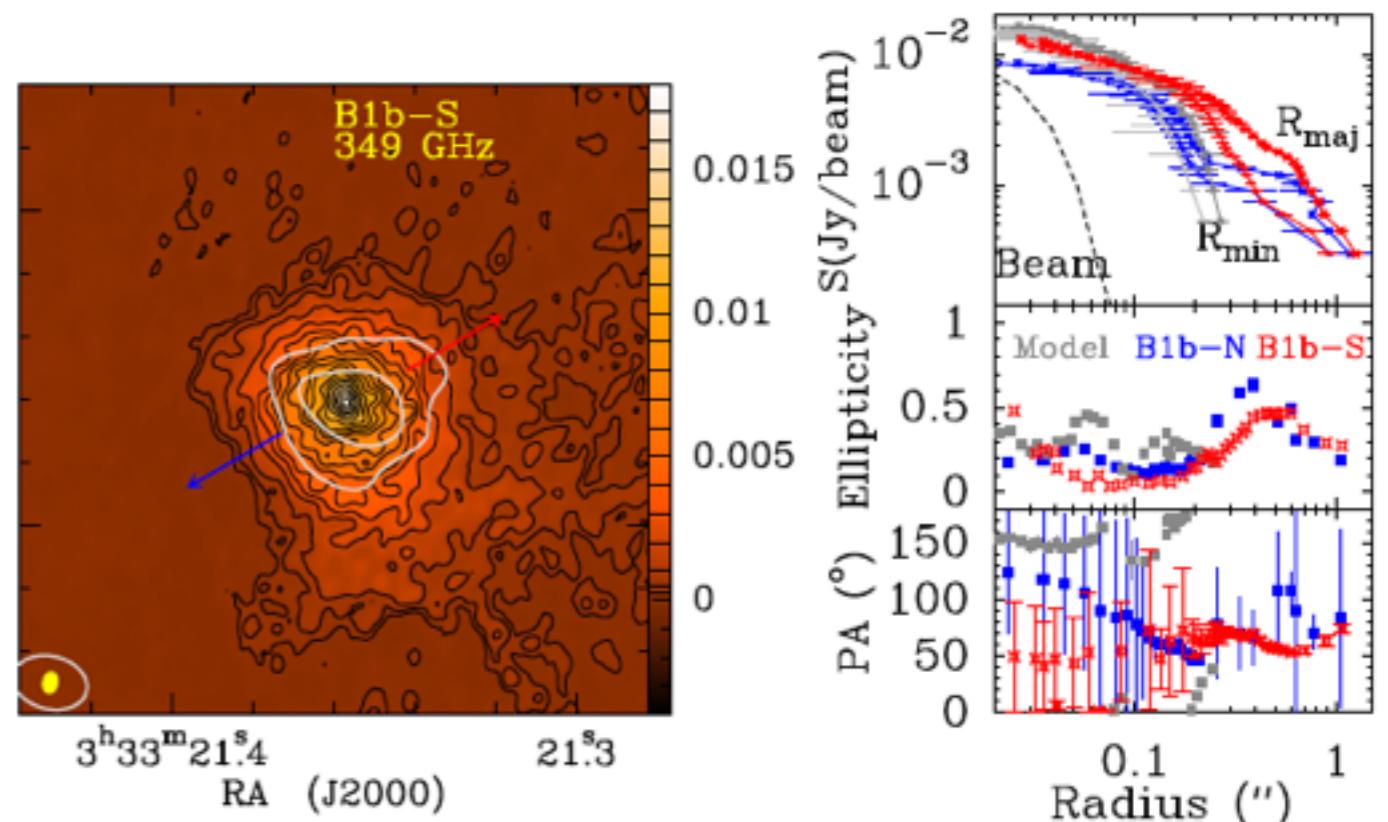
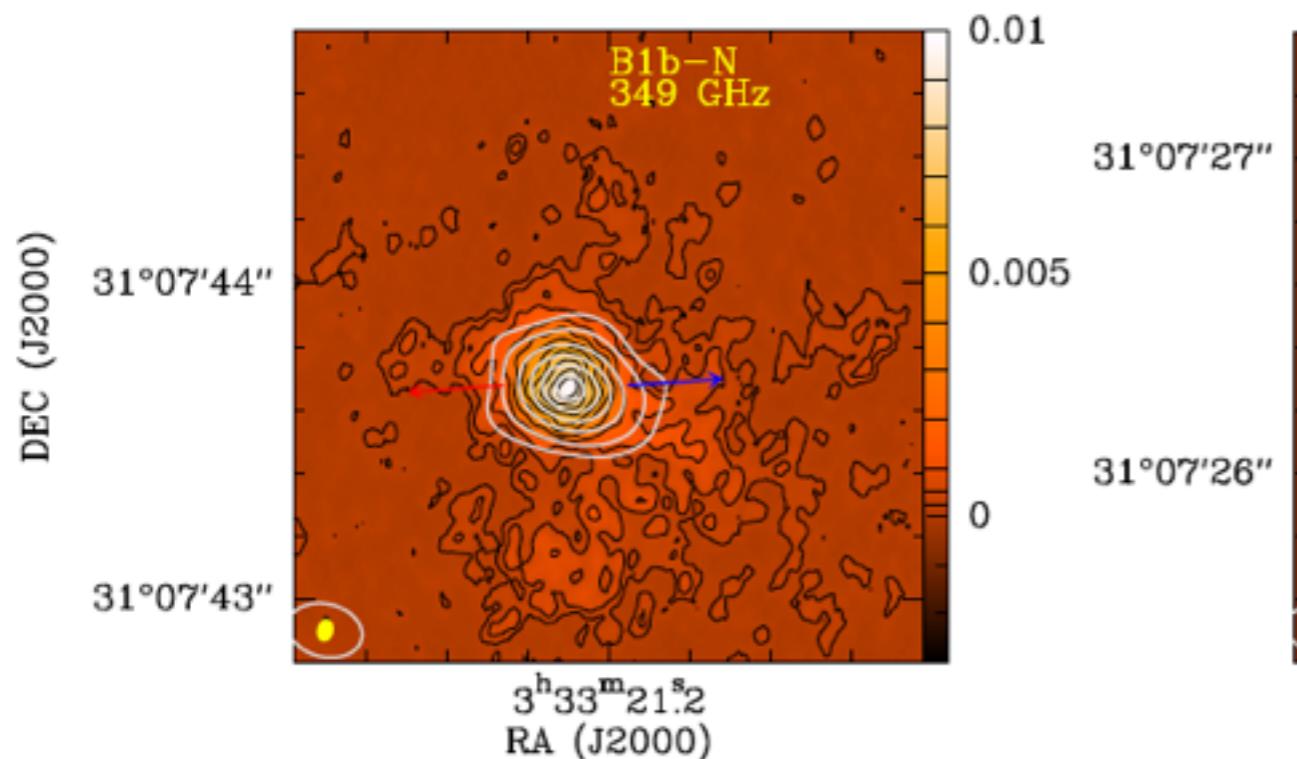
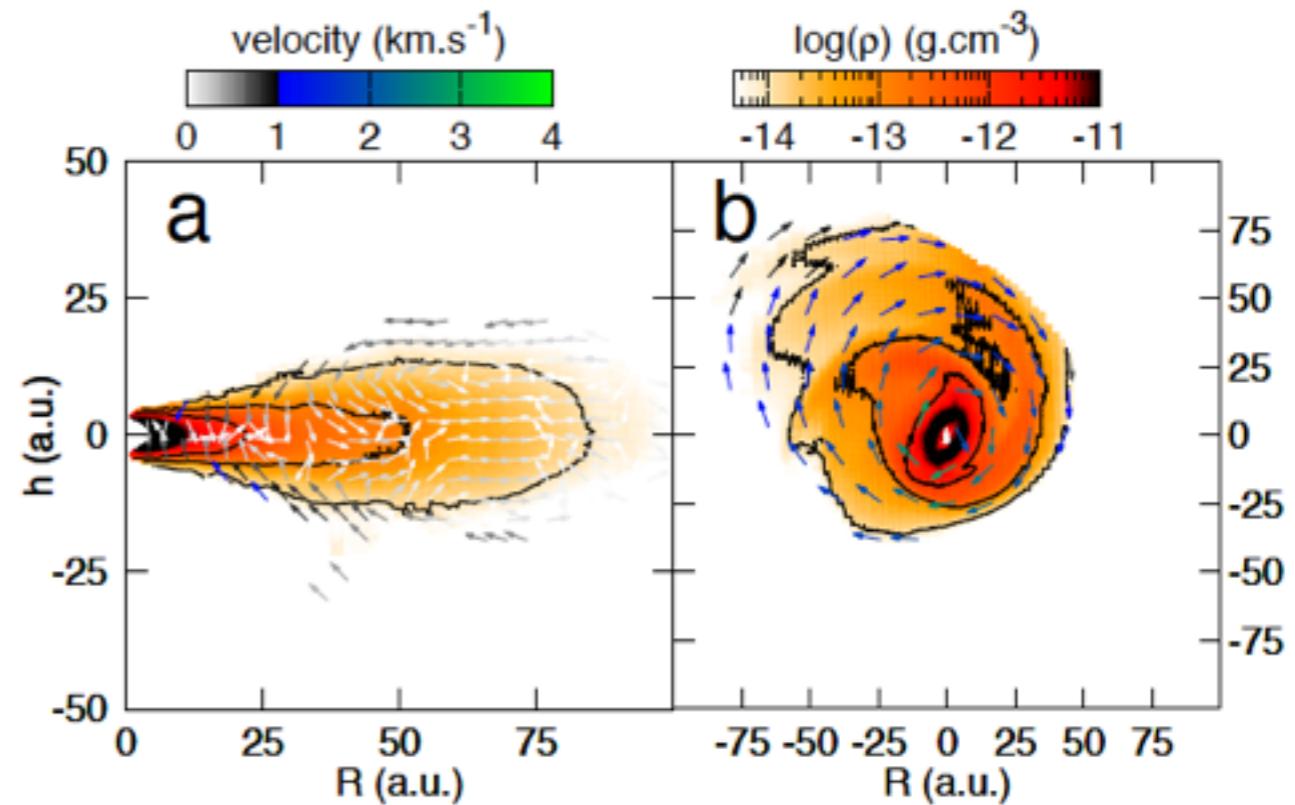
ALMA Band 3 Config 20 @150 pc

Commerçon, Levrier et al. A&A, 2012



# Comparison with real ALMA observations

- Source Barnard 1b-N: first core candidate
- ALMA 0.06''@ 350 GHz ( $\sim 15$  AU)
- data compatible with collapse model ( $\mathcal{M}=1.2$  ;  $\mu=2$ )
- data compatible with disc growth with time

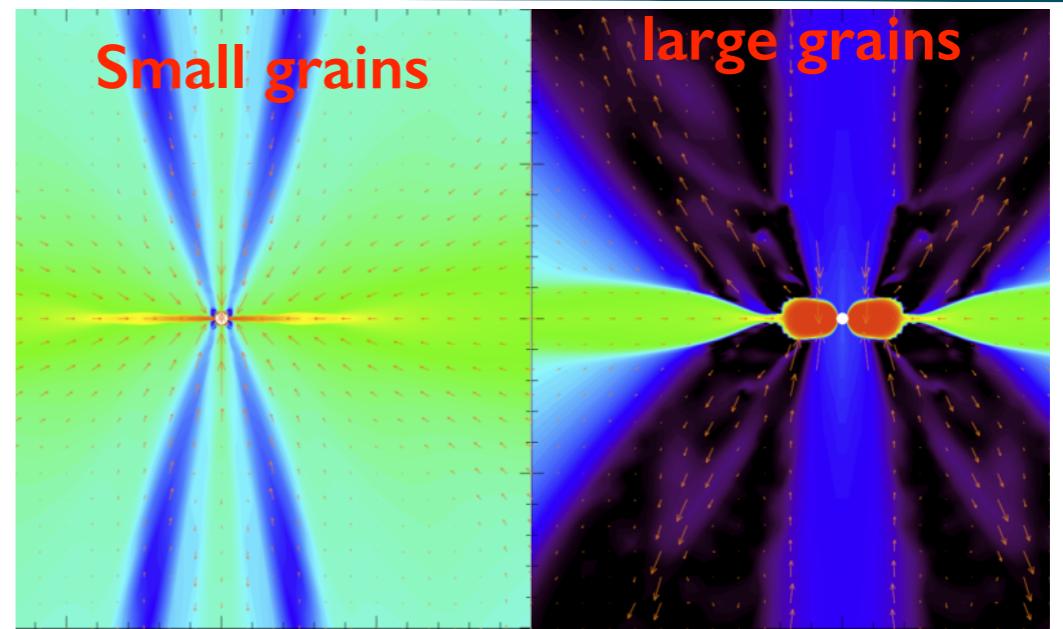


# What is next?

- Follow the dust dynamics at all scales

- dust growth
- dust charge
- gas-to-dust ratio

*Zhao et al (2016)*



- Couple the process

- magneto hydrodynamics: chemistry + dust + magnetic resistivities
- radiation hydrodynamics: chemistry + dust + opacities
- track cosmic rays ionisation
- inclusion more feedback processes (jets, wind, CR acceleration)

- Couple the scales

- galaxy evolution to molecular clouds (e.g., Renaud et al. 2013)
- self-regulated ISM, from diffuse ISM to collapsing dense cores (Hennebelle et al.)
- protoplanetary disc evolution with accreting envelop

# Take away

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## We are getting closer, but....

- large uncertainties on gas-grain chemistry for ionisation
- coupling with magnetic fields poorly constrained
- dust evolution?
- second Larson core: a challenge for computational astrophysics

## What we need:

- ✓ constraints on the dust
- ✓ systematic parameter studies
- ✓ synthetic observations: dust, line emission, polarisation

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**THANK YOU**

# Astrosim school

Ecole numerique pour l'astrophysique

<https://astrosim.sciencesconf.org/?forward-action=index&forward-controller=index&lang=en>

## Astrosim : Ecole numérique pour l'astrophysique

26 juin - 7 juillet 2017, Lyon, France

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### MAIN MENU

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- Planning
- Practical informations
- Registration
- List of Participants

### HELP

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### OBJECTIVES OF THE SCHOOL

Numerical simulations are playing a key role in many areas of modern sciences including astrophysics as well as in the industry. It is not unavoidable and is complementary of observations and theory. Without numerical simulations our understanding of astrophysical systems would be significantly less than what it is today.

However, performing numerical simulations for astrophysics requires a large ensemble of specific skills in several different areas. First there are generic aspects common to many simulations such as massively parallel calculations, numerical methods of applied mathematics and algorithms as well as analysis of large volumes of data. Second several programs called codes have been developed by groups of developers during the last decades to treat various astrophysical problems. Running and developing these codes is a necessity for advanced researchers as well as PhD students, however this represents sometimes such an effort and an expertise that a specific training is needed.

The goal of the school will be to present several codes that are playing a key role in today astrophysics. Both theoretical aspects regarding the methods used and the practical ones, that is to say how to use the codes will be described. In particular practical sessions will be organised during the afternoons.

### PROGRAM AND SPEAKERS

The organisation of the school will be as follows:

2 theoretical lectures will be given every morning during which essential

### SCIENTIFIC ORGANISING COMMITTEE

Benoit Commerçon (CRAL, Lyon), chair  
Patrick Hennebelle (SAp CEA Saclay), chair

Guillaume Aulanier (LESIA, Meudon)  
Jérémie Blaizot (CRAL, Lyon)  
Boris Dintrans (IRAP, Toulouse)  
Guillaume Dubus (IPAG, Grenoble)  
Sébastien Fromang (SAp CEA, Saclay)  
Franck Le Petit (LERMA, Paris)  
Aurélie Marchaudon (IRAP, Toulouse)

### LOCAL ORGANISING COMMITTEE

Benoit Commerçon  
Patrick Hennebelle  
Jérémie Blaizot  
Emmanuel Quemener